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# OUTLINE

- Key stages of the development of the MC generator by group from Wroclaw
- I will cover the 2002-2006 period (my PhD project)
- In this period people developing the code:
  - C.Juszczak, K.Graczyk, JN and J. Sobczyk
- Motivations for a new generator
- Ideas how to approach key elements of the generator



# INITIAL IDEA FOR NEW MC GENERATOR

- The original idea is hidden in the the beginning of XXI century.
  - NuInt workshops at KEK and UC Irvine
  - Composition of the group.
  - Encouragement from Danka Kielczewska
  - Use MC to compare new developments in modelling with data
- The state of the MC generators was rather grim in those days
  - NUEGEN
  - NUANCE
  - NEUT
  - GENEVE
  - NUX
- All generators were written for specific experiments with limitations of their applicability.



# THE FIRST IDEA FOR A NEW GENERATOR

- The original motivation: to improve NUX+FLUKA scheme (no resonance production)
- A new treatment of the resonance region
- Only ∆ resonance: nuclear effects should smear out other resonances and average treatment of them should be sufficient
   Quark-Hadron duality
- A tool to investigate nuclear effects (e.g spectral function, nuclear potential)

#### APPROACH

• The ingredients of the generators were obvious (CC)

$$\sigma_{\nu} = \sigma_{QE}^{CC} + \sigma_{SPP}^{CC} + \sigma_{DIS}^{CC} + \sigma_{QE}^{NC} + \sigma_{SPP}^{NC} + \sigma_{DIS}^{NC}$$

Primary vertex: 3 separate dynamical mechanisms

- Quasi-elastic scattering (Llewellyn-Smith)
- Single pion production
  - Smooth gluing  $\Delta$  excitation and DIS exclusive SPP channels for hadronic invariant mass  $W \in (1.3, 1.6)GeV$
  - Non-resonant background
- More inelastic (DIS)
  - Pythia fragmentation

# CCQE

- We started with a simple generator for CCQE + nuclear effects
  - QE as in Llewellyn Smith
  - Fermi Gas implementations from Smith-Monitz and Bodek-Ritchie
  - Local Density approximation with effective potential
  - Form factors, BBA03, BBBA05, Kelly



$$\frac{d\sigma^{\nu,\bar{\nu}}}{d|q^2|} = \frac{M^2 G^2 \cos^2 \theta_C}{8\pi E_{\nu}^2} \left[ A(q^2) \mp B(q^2) \frac{(s-u)}{M^2} + C(q^2) \frac{(s-u)^2}{M^4} \right]$$

#### **COMPREHENSIVE COMPARISONS TO DATA**

Comparisons to "old" data





# NUCLEAR MODELS - LDA

- It was always clear to us that the constant density Fermi Gas model cannot be sufficient to model the nucleus in neutrino interactions
- The Local Density Approximation (LDA) was previously used (e.g Oset et al.) but not in neutrino MC generators, AFAIK.
- We needed
  - Density of the nuclei
  - Nuclear potential
  - Four-momentum conservation

#### NUCLEAR DENSITY

The fermi momentum is related to the density

$$k_F = \left(\frac{3\pi^2}{2}\rho\right)^{1/3}$$

- The density of the nuclei were taken from C. W. De Jager, H. De Vries and C. De Vries, Atom. Data Nucl. Data Tabl. 36 (1987) 495
- This was the most difficult article to find: missing from Wroclaw, CERN and Fermilab libraries. Eventually I found it at INFN Milan.







#### EFFECTIVE POTENTIAL



Nucl. Phys. A 292 (1977) 445

Phys. Rev. C 38 (1988) 2101

- We used the Brieva, Dellafiore results and parametrized their momentum dependent potential.
- Only a few years later we compare it to the potential from BUU model and it seem to be extraordinarily similar.

$$V(k_F, p) = -\frac{(ak_F)^2 (k_F + b)}{c^4 + d^3 k_F + e^3 p^2 / k_F + p^4}, \qquad V(\vec{r}, \ \vec{p}) = A \frac{\rho(\vec{r})}{\rho_0} + B \left(\frac{\rho(\vec{r})}{\rho_0}\right)^\tau + \frac{2C}{\rho_0} g \int \frac{dp'}{(2\pi)^3} \frac{f(\vec{r}, \vec{p})}{1 + \left(\frac{\vec{p} - \vec{p'}}{\Lambda}\right)^2}$$

## NUCLEAR MODELS -LDA

 We hoped that the new approach would explain the results from K2K



• The 500MeV/c cut for K2K was to strong to see any effect of the LDA



Eur. Phys. J. C 39 (2005) 195



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# np-nh MODELS

- One of the first tasks for Jan was to recalculate the Marteau model np-nh. (main source was Marteu's thesis in French)
- I looked into modeling of CCQE events in NUX (I was reading thesis by F. Sartogo in Italian).
- We started using the idea of QE-like events and  $0\pi$  events



# PION PRODUCTION

- The pion production was modelled with excitation of  $\Delta$  only

$$\frac{d^2\sigma}{dWdQ^2} = G^2 \cos^2_C \frac{Wg(W)}{4\pi^4} ME^2 \left( -(Q^2 + m^2)W_1 + \frac{W_2}{M^2} (2(pk)(pk') - \frac{M^2}{2}(Q^2 + m^2)) + \frac{W_3}{M^2} \left( Q^2(kp) - 1/2(Q^2 + m^2)(pq) \right) + \frac{W_4}{M^2} \frac{m^2}{2} (Q^2) + m^2 - \frac{W_5}{M^2} m^2(kp) \right)$$

- Form factors taken from L. Alvarez-Ruso, S.K. Singh and M.J.Vincento Vascas, Phys. Rev. C59, 3386(1999)
- K.Graczyk performed analysis for  $\Delta$  excitation

# **DEEP INELASTIC SCATTERING 2004**

#### The DIS cross section is very easy

$$\frac{d^{2}\sigma^{\nu(\bar{\nu})}(E)}{dxdy} = \frac{G_{F}^{2}ME}{\pi} \left[ \left( xy^{2} + \frac{ym^{2}}{2ME} \right) F_{1}\left( x, Q^{2} \right) \qquad F_{1}\left( x, Q^{2} \right) \\
+ \left( 1 - y - \frac{Mxy}{2E} - \left( \frac{m}{2E} \right)^{2} - \frac{m^{2}}{2MEx} \right) F_{2}\left( x, Q^{2} \right) \qquad F_{1}\left( x, Q^{2} \right) \qquad F_{1}\left( x, Q^{2} \right) = \sum_{j} \left[ q_{j}\left( x, Q^{2} \right) + \bar{q}_{j}\left( x, Q^{2} \right) \right] \\
+ \left( 1 - y - \frac{Mxy}{2E} - \left( \frac{m}{2E} \right)^{2} - \frac{m^{2}}{2MEx} \right) F_{2}\left( x, Q^{2} \right) \qquad F_{3}\left( x, Q^{2} \right) = 2 \sum_{j} \left[ q_{j}\left( x, Q^{2} \right) - \bar{q}_{j}\left( x, Q^{2} \right) \right] \\
+ \left( xy - \frac{xy^{2}}{2} - \frac{ym^{2}}{4ME} \right) F_{3}\left( x, Q^{2} \right) \right]$$

- q<sub>i</sub> Parton Distribution Function(PDF).
- At first we used GRV94 with Bodek-Yang modifications
- Later we also implemented the GPV98 with Bodek-Yang modifications.
- Eur. Phys. J. C 5 (1998) 46, Nucl. Phys. Proc. Suppl. 112 (2002) 70).



#### "CHEAP" HADRONIZATION

- The fragmentation and hadronization are difficult so for the first approach we only use the SPP channels.
- We used Pythia to get four-vectors for states with the 1  $\pi$
- F<sup>SPP</sup> is a contribution of the single pion production channel in overall DIS cross section, reconstructed using LUND fragmentation algorithm.





## TRANSITION REGION

- Smooth transition from  $\Delta$  excitation to DIS single pion channels

$$\frac{d\sigma^{SPP}}{dW} = \frac{d\sigma^{\Delta}}{dW} \left(1 - \alpha(W)\right) + \frac{d\sigma^{DIS}}{dW} F^{SPP}(W)\alpha(W) \quad (9)$$

$$\begin{aligned} \alpha(W) &= \Theta(1.3GeV - W) \frac{W - W_{th}}{W_{min} - W_{th}} \alpha_0 \\ &+ \Theta(W_{max} - W) \Theta(W - W_{min}) \frac{W - W_{min} + \alpha_0(W_{max} - W)}{W_{max} - W_{min}} \\ &+ \Theta(W - W_{max}) \end{aligned}$$

 The idea is justified by the quark-hadron quality → smearing of the maxima from resonances due to nuclear effects.



• With a ready algorithm we perform simple fitting to get the parameters of the model.



J.Sobczyk, NuInt04, Gran Sasso















# NUINT 04

 At NuInt04 we presented the generator as WroNG (Wroclaw Neutrino Generator)

 If you remember that three out of four of the developers used to work in the string theory it is an improvement



#### FRAGMENTATION ALGORITHM

- Pythia can generate events only for Ev > 10 GeV.
- However, in fragmentation routines of PYTHIA lower energies are allowed -> We needed to redo the fragmentation
- Cross section is a sum of contribution from separate quarks
  - Cross section for scattering on quark gi (valance or sea quark)

$$\frac{d^2 \sigma^{\nu q_i \to \mu q_j}}{dW d\nu} \sim q_i K_i$$

- Ki kinematic factor for quark q.
- Probability of reaction on a quark is given as follows

$$P(q_i) = \frac{\frac{d\sigma^{q_i}(E)}{dWd\nu}}{\sum_{i} \frac{d\sigma^{q_i}(E)}{dWd\nu}}$$

$$P(q_i) = \frac{\frac{d\sigma^{q_i}(E)}{dWd\nu}}{\sum_{i} \frac{d\sigma^{q_i}(E)}{dWd\nu}}$$

$$E(GeV)$$



3/12/201

#### FRAGMENTATION ALGORITHM

Illustration of the scattering on parton inside nucleon for CC interaction





#### DEEP INELASTIC SCATTERING

• Charged-hadron multiplicity P  $(n_{ch}) = \sigma(n_{ch} / \sigma(n_{ch}))$ 



# TWO PION PRODUCTION

We also started looking into exclusive channels to test our approach



J. Nowak, Lancaster University, Early days of NuWro



## FINAL PRODUCT IN 2006

- In 2005 all the basic components were ready and implemented
- By 2006 we added missing elements: NC and antineutrinos
- We got the Lipari plots



