

# Angular Momentum in Heavy Ion Collisions via SMASH

**Nils Sass**

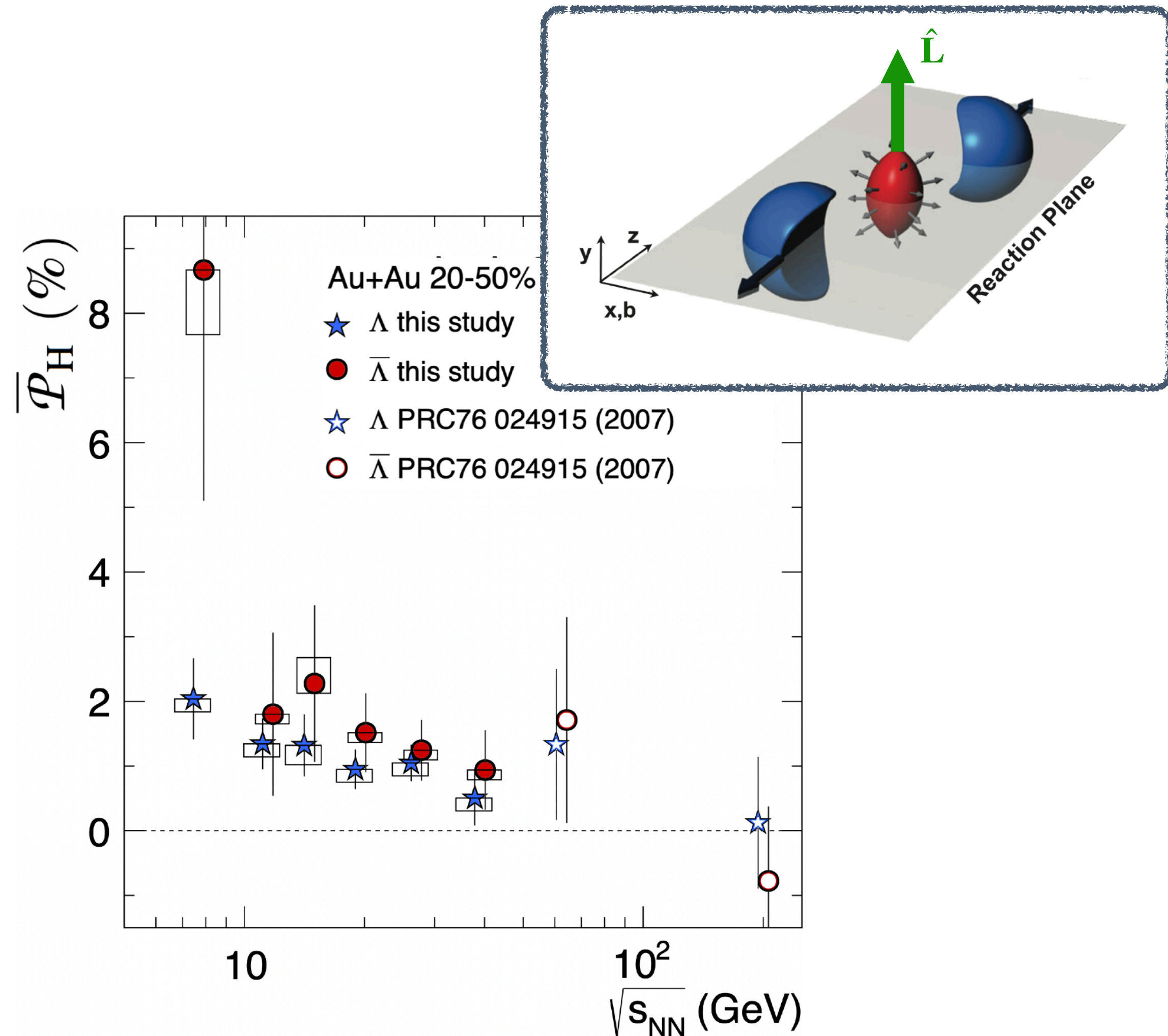
in collaboration with Oscar-Garcia Montero,  
Marco Müller and Hannah Elfner



# Signals of Polarization

L. Adamczyk *et al.* [STAR], *Nature* 548 (2017), 62-65

Snellings 2011 *New J. Phys.* 13 055008 (adoption)



## STAR Measurement

- Global spin-polarization of  $\Lambda$  hyperons in non-central Au+Au collisions at  $\sqrt{s_{NN}} = 3 - 200$  GeV and mid-rapidity
- Hyperon polarization is a direct hint of vorticity of the QGP
- Polarization decreases for lower beam energies

# Why Angular Momentum?

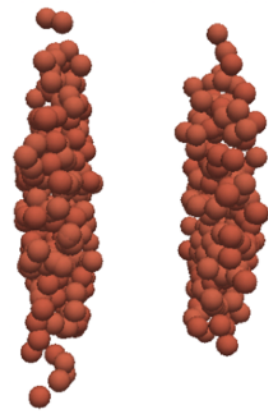
- Angular momentum of the nuclei is the **driver of spin polarization** in heavy-ion collisions by inducing vorticity
- To **model hyperon polarization**, the dynamic description of angular momentum transfer to the fireball is crucial
- Detailed understanding of the dynamics is important to identify **phase transition signals**

## Hadronic Transport Approach *smash* \*

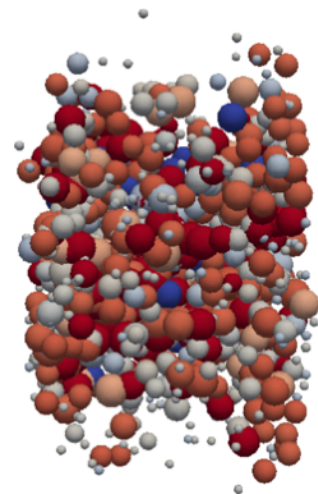
Weil et al., Phys. Rev. C 94 (2016)

Pb-Pb collision  
at  $E_{lab} = 40$  GeV

$t = -2.5$  fm

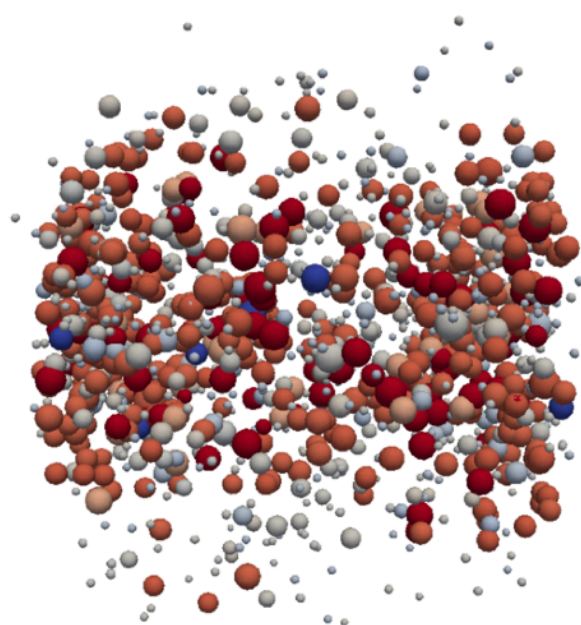


$t = 6$  fm



© Justin Mohs

$t = 12$  fm



<http://smash-transport.github.io>

- \***S**imulating **M**any **A**ccelerated **S**trongly-Interacting **H**adrons
- Dynamical non-equilibrium description of HICs at low beam energies (FAIR) and late stage rescattering at high beam energies (RHIC/LHC)
- Includes all hadrons up from the PDG to  $m \sim 2.35$  GeV

## SMASH Setup

- Effective solution of the relativistic Boltzmann equation

$$p^\mu \partial_\mu f_i(x, p) + m_i F^\alpha \partial_\alpha^p f_i(x, p) = C_{coll}^i$$

- Geometric collision criterion

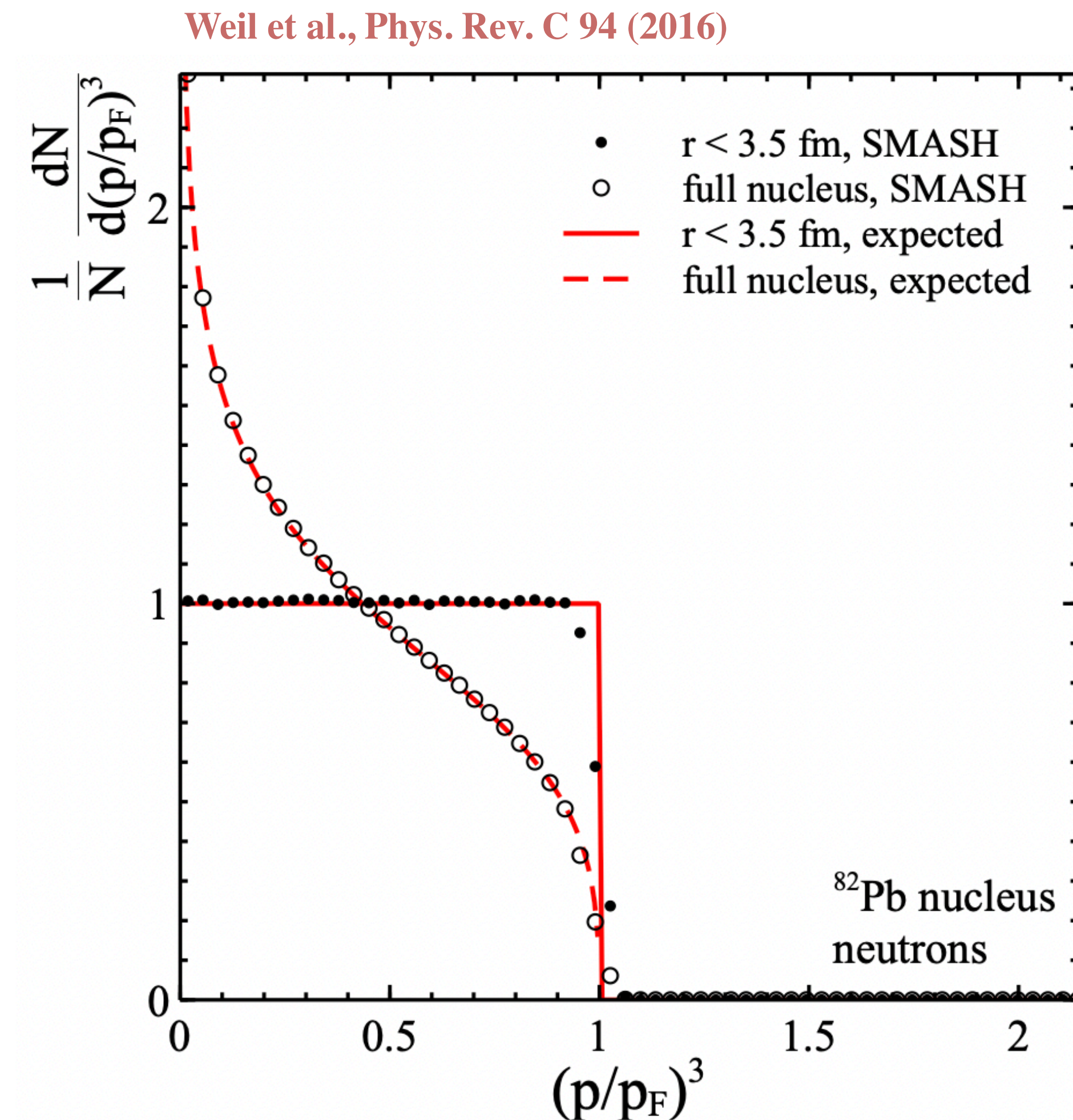
$$d_{trans} < d_{int} = \sqrt{\frac{\sigma_{tot}}{\pi}} \quad d_{trans}^2 = (\vec{r}_a - \vec{r}_b)^2 - \frac{((\vec{r}_a - \vec{r}_b) \cdot (\vec{p}_a - \vec{p}_b))^2}{(\vec{p}_a - \vec{p}_b)^2}$$

- Test particle method  $\sigma \rightarrow \sigma \cdot N_{test}^{-1}$ ,  $N \rightarrow N \cdot N_{test}$

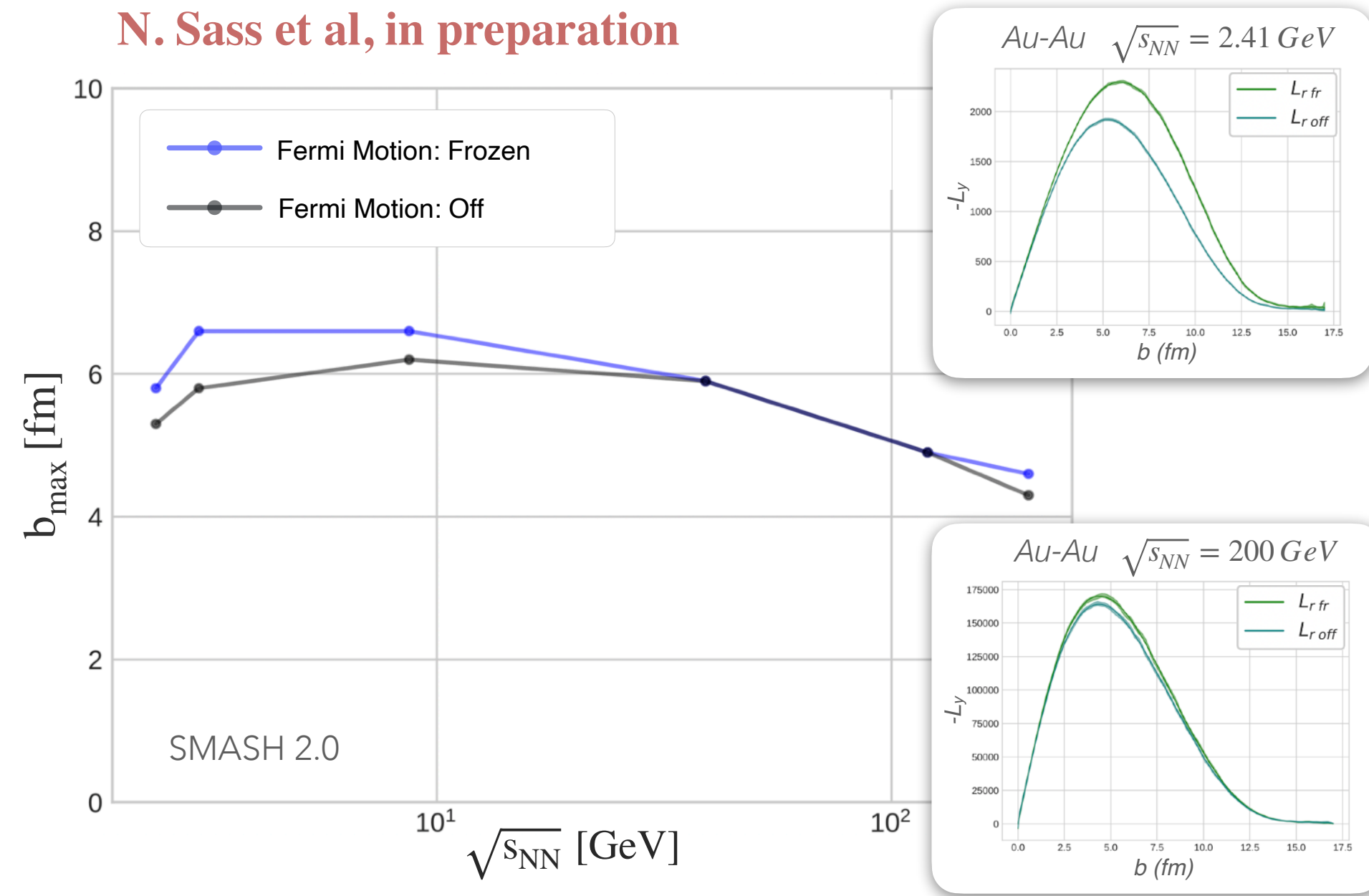
# Angular Momentum & Fermi Motion in SMASH

- SMASH accesses the full phase-space information of every particle and thus its angular momentum
- **Fermi motion:** nucleonic momentum distribution due to Pauli exclusion principle
- In the ground state nucleus, nucleon momentum distribution corresponds to a uniformly filled Fermi sphere with radius

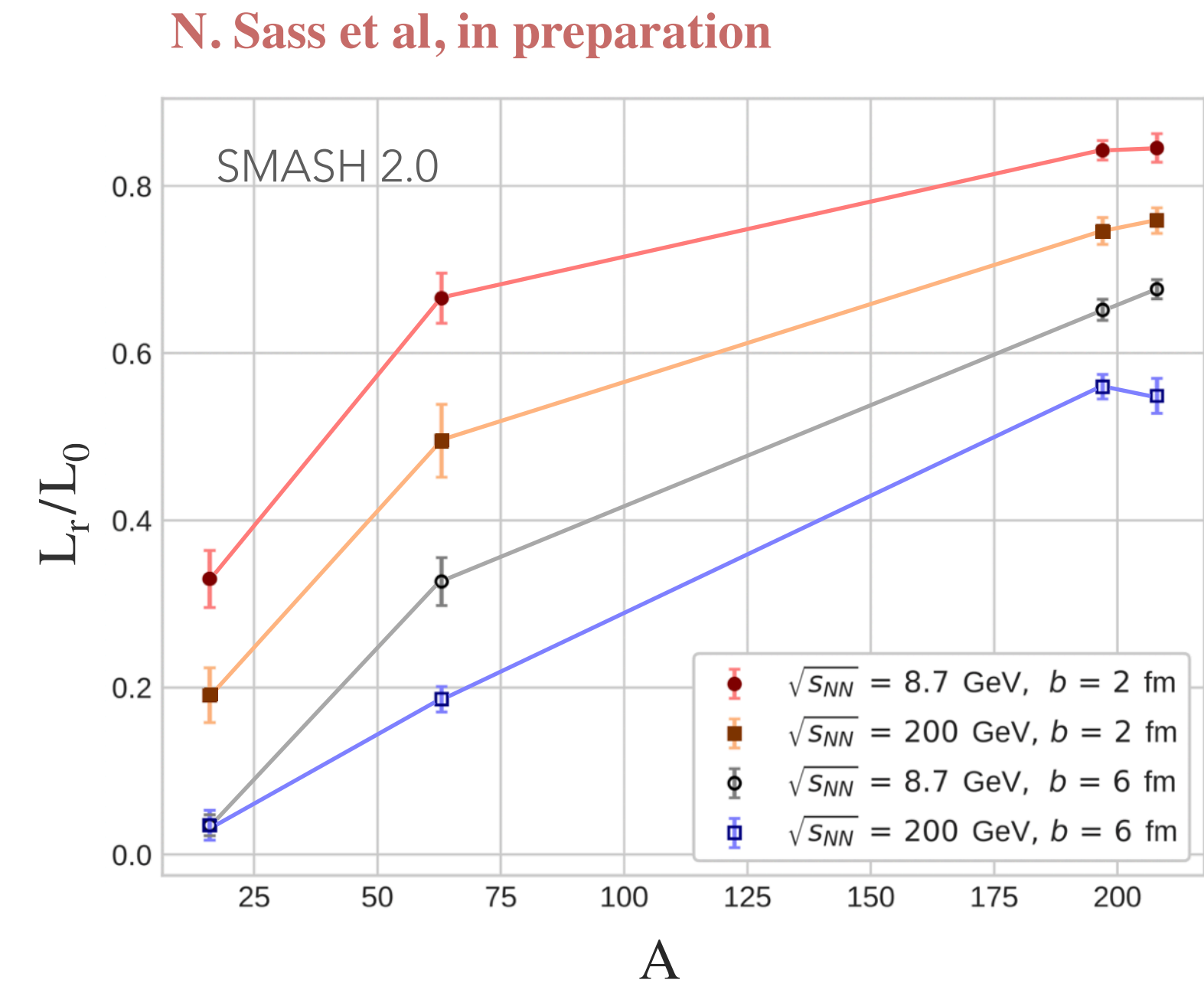
$$p_F(\vec{r}) = \hbar c \left( 3\pi^2 \rho(\vec{r}) \right)^{\frac{1}{3}}$$



# Angular Momentum & Fermi Motion in SMASH



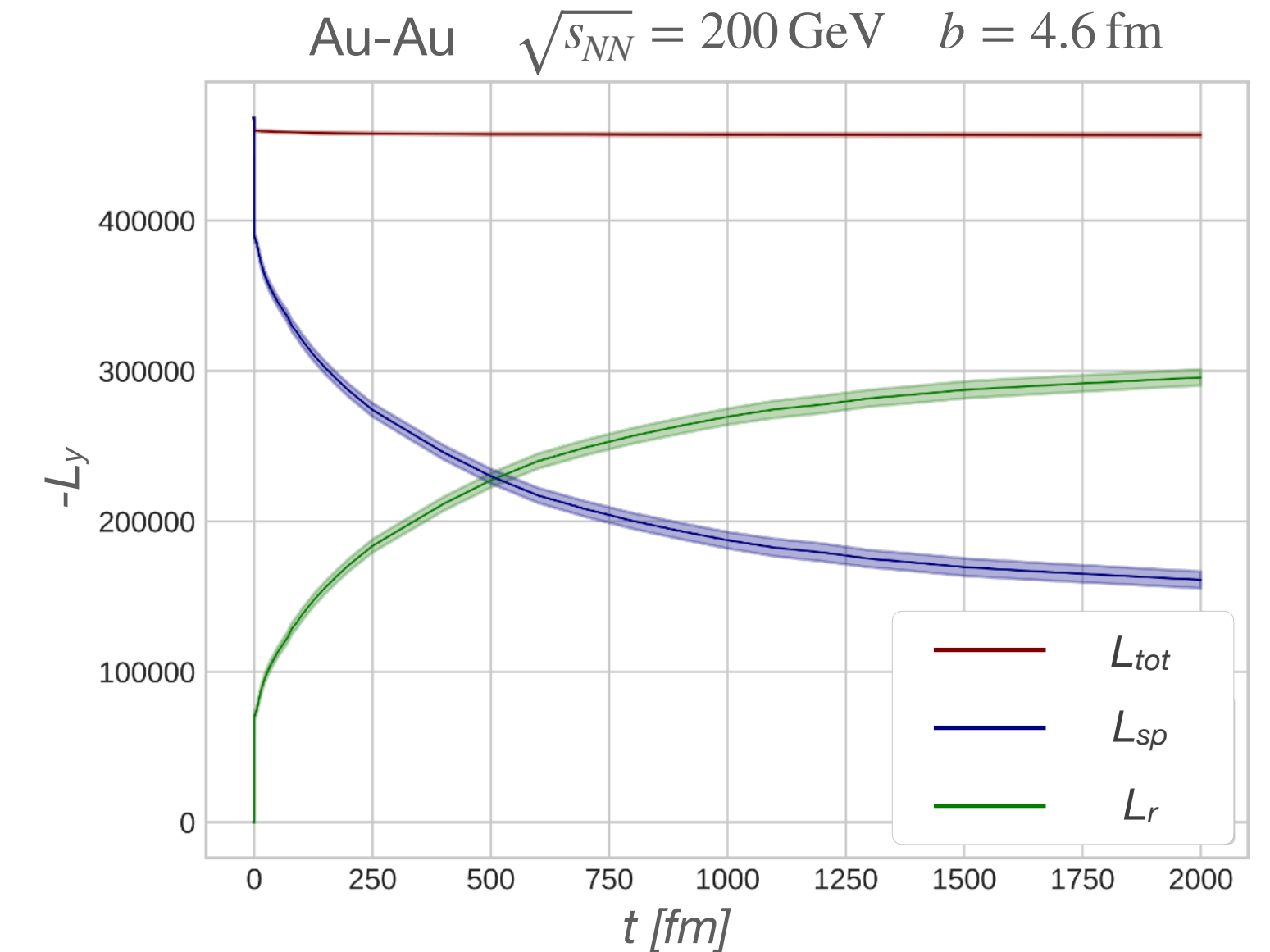
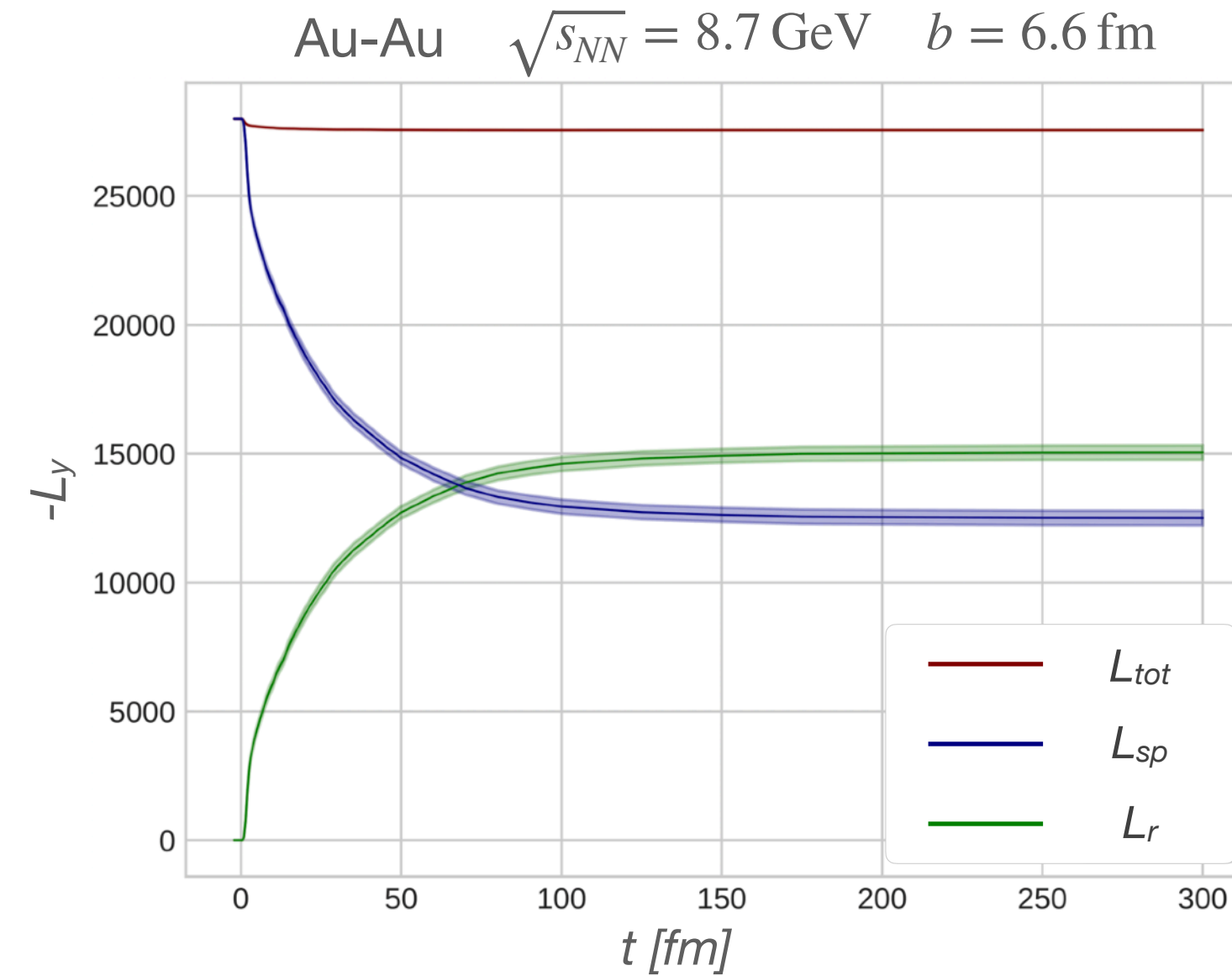
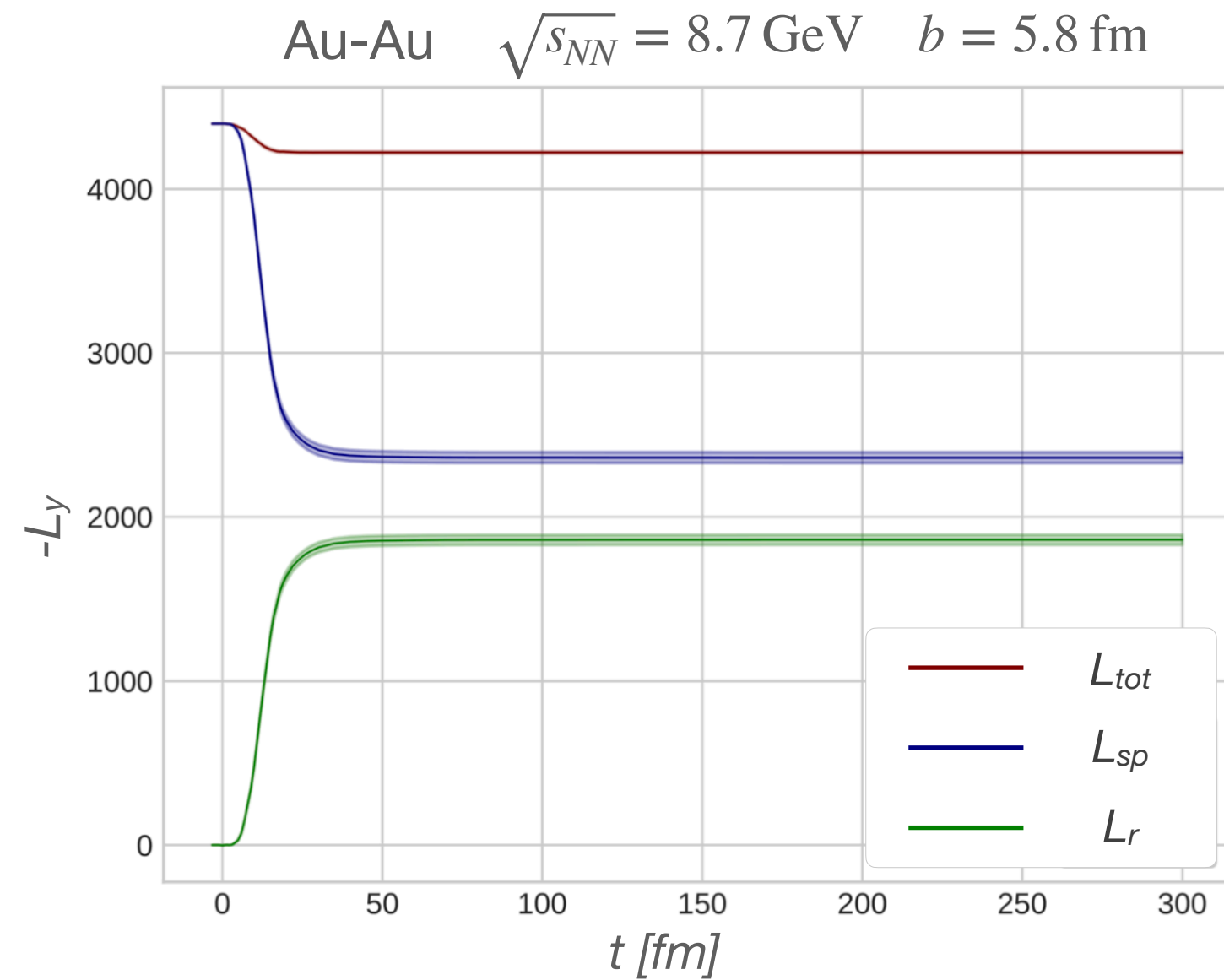
- **Energy dependence** of impact parameter  $b_{\text{max}}$  for which the remaining angular momentum  $L_r$  becomes maximal
- **Fermi motion** induces additional angular momentum into the system



- **System size dependence** of the ratio of the fireball's angular momentum over the initial angular momentum  $L_r / L_0$
- More angular momentum is deposited at mid rapidity in more central collisions and at lower beam energies

# Angular Momentum Evolution

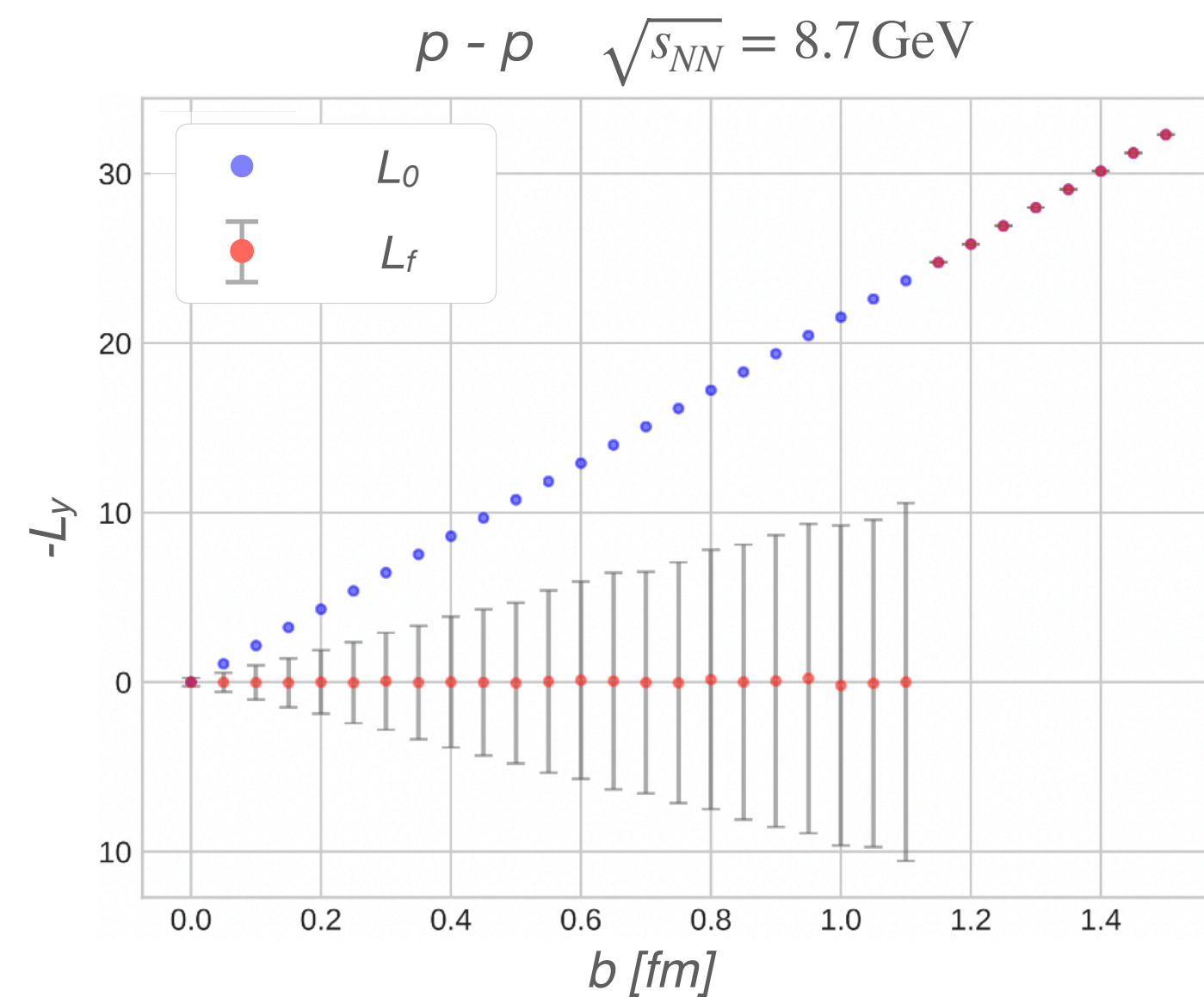
N. Sass et al, in preparation



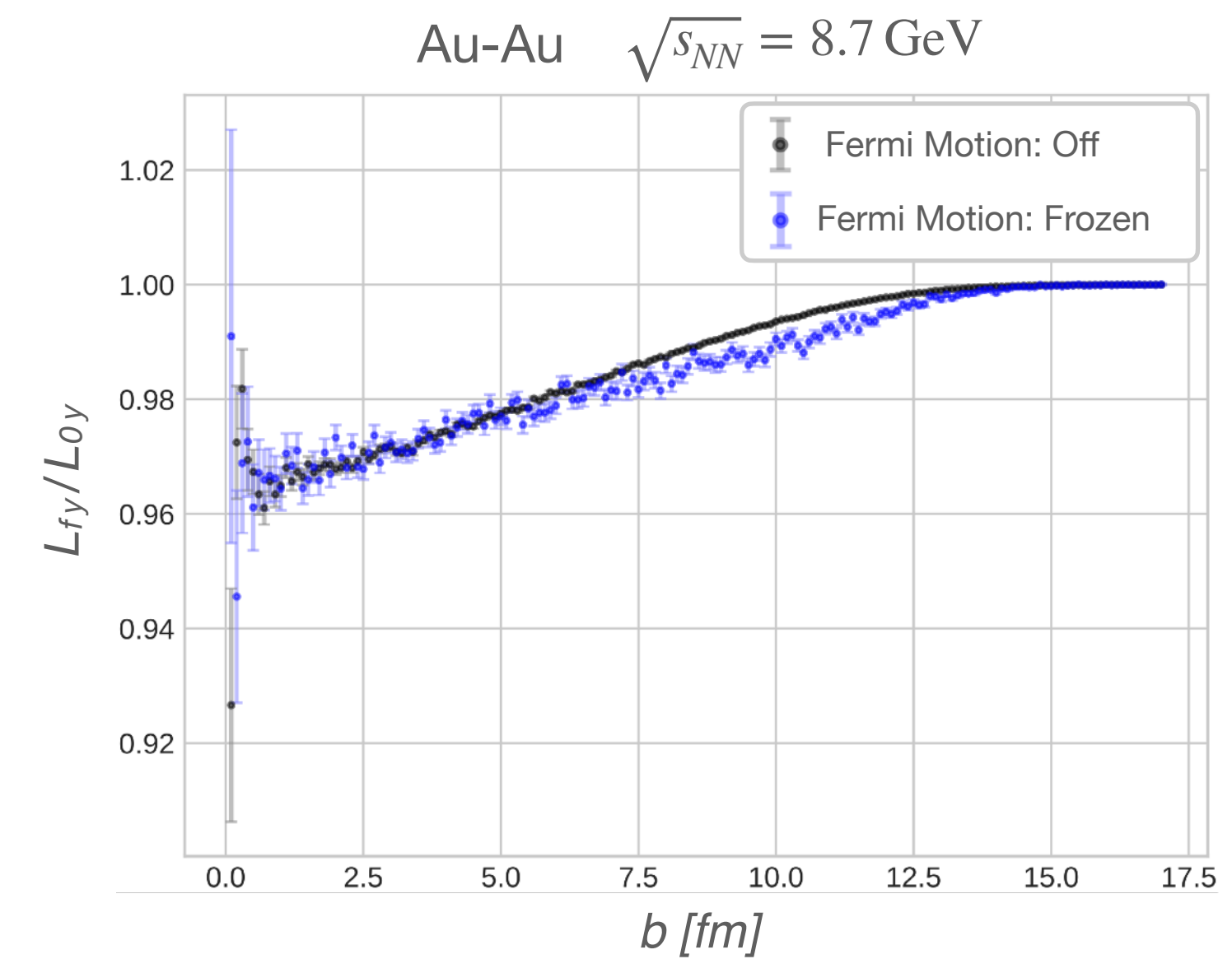
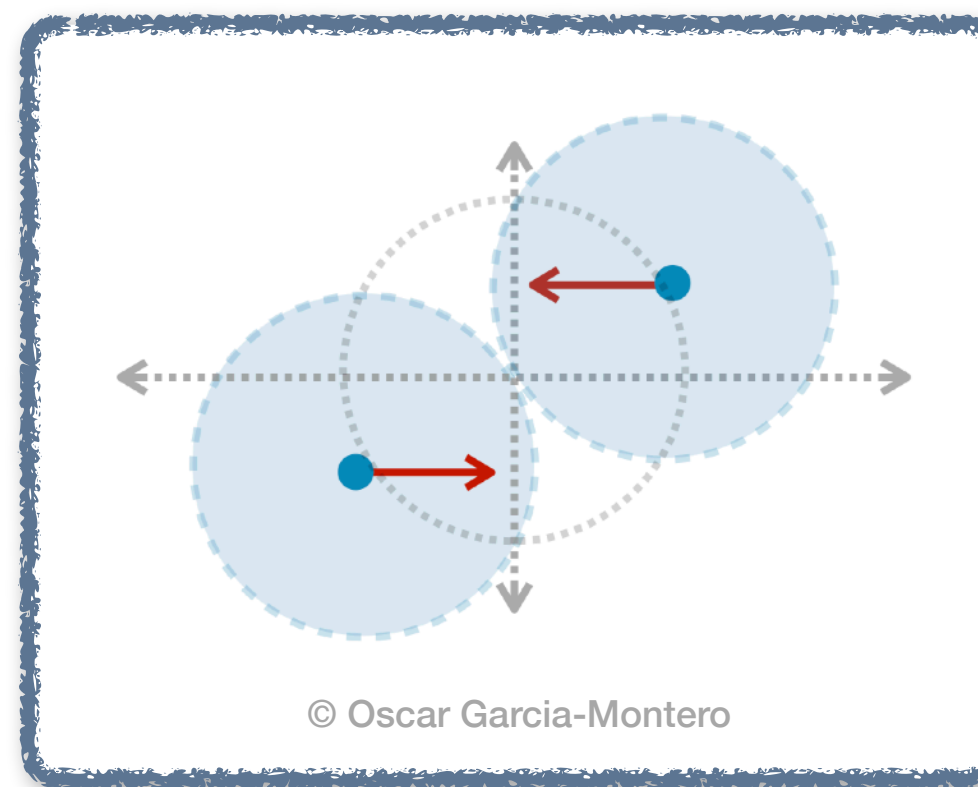
- Secondary collisions at higher beam energies shift the flattening of  $L_{sp}$  and  $L_r$  to later times
- We observe a kink in the total angular momentum at the time when both nuclei collide  
→ Broken angular momentum conservation
- For higher beam energies the kink occurs at smaller times due to faster time evolution

# Angular Momentum Conservation

- Collective „loss“ of angular momentum in Au-Au collisions amounts to 3.5% for small impact parameters
- Additional momenta by Fermi motion slightly increase non-conservation of angular momentum
- Geometrical Interpretation of the cross section breaks angular momentum conservation in binary in/elastic collisions



N. Sass et al, in preparation





# Treating Conservation in Elastic Scatterings

Calculate the change in angular momentum  $\Delta L$  and mass moment  $\Delta K$  for each binary collision:

$$\Delta \vec{L} = (\vec{x}_1 - \vec{x}_2) \times \vec{p} - (\vec{x}'_1 - \vec{x}'_2) \times \vec{p}'$$

$$\Delta \vec{K} = (t_1 - t_2)(\vec{p} - \vec{p}') - (\vec{x}_1 - \vec{x}'_1)E_1 - (\vec{x}_2 - \vec{x}'_2)E_2$$

Get the corrected positions of the scattered particles restricting collision trajectories to a plane and solving

$$\Delta \vec{L} = 0, \quad \Delta \vec{K} = 0$$

LINEAR SYSTEM

$$-p'_y x'_1 + p'_y x'_2 + p'_x y'_1 - p'_x y'_2 = \Delta_{[x,y]}$$

$$E'_1 x'_1 + E'_2 x'_2 = \Delta_x$$

$$p'_z x'_1 - p'_z x'_2 - p'_x z'_1 + p'_x z'_2 = \Delta_{[z,x]}$$

$$E'_1 z'_1 + E'_2 z'_2 = \Delta_z$$

$$-p'_z y'_1 + p'_z y'_2 + p'_y z'_1 - p'_y z'_2 = \Delta_{[y,z]}$$

$$E'_1 y'_1 + E'_2 y'_2 = \Delta_y$$

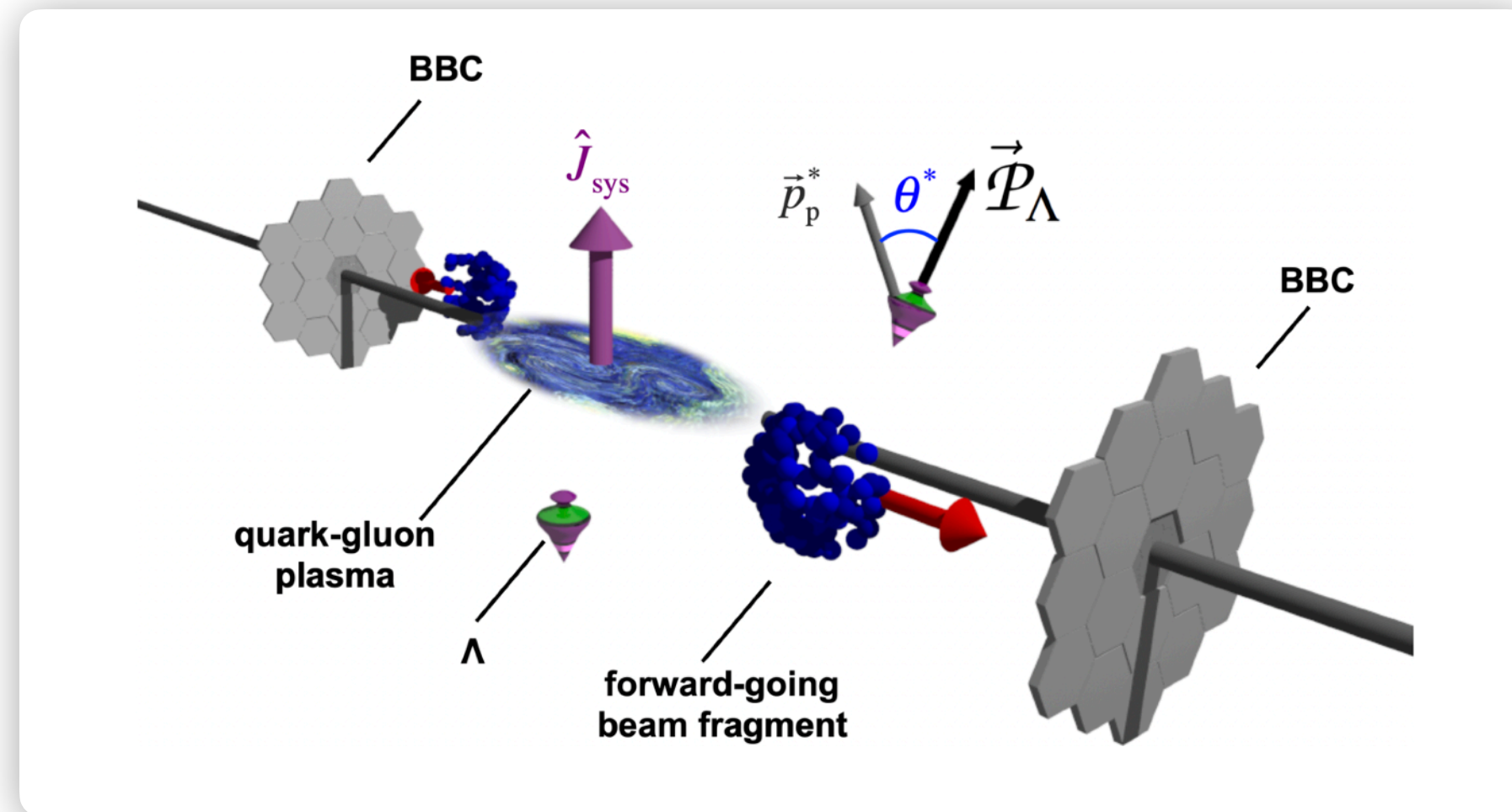
# Conclusion & Outlook

- Impact parameter  $b_{\max}$  for which the angular momentum of the fireball becomes maximal is nearly energy independent for a broad energy range  
→  $b_{\max} \in [ 4.5 \text{ fm}, 6.6 \text{ fm} ]$  for  $\sqrt{s_{\text{NN}}} \in [ 2.41 \text{ GeV}, 200 \text{ GeV} ]$
- Higher relative transfer of initial angular momentum to the fireball in more central collisions
- Fermi motion induces additional angular momentum
- Predictions for expectation of high angular momentum is important for future experimental measurements
- Detailed understanding of the dynamics is crucial for extracting phase transition signals
- Long-term goal: Implementing spin degrees of freedom to describe hadronic polarization within the transport approach

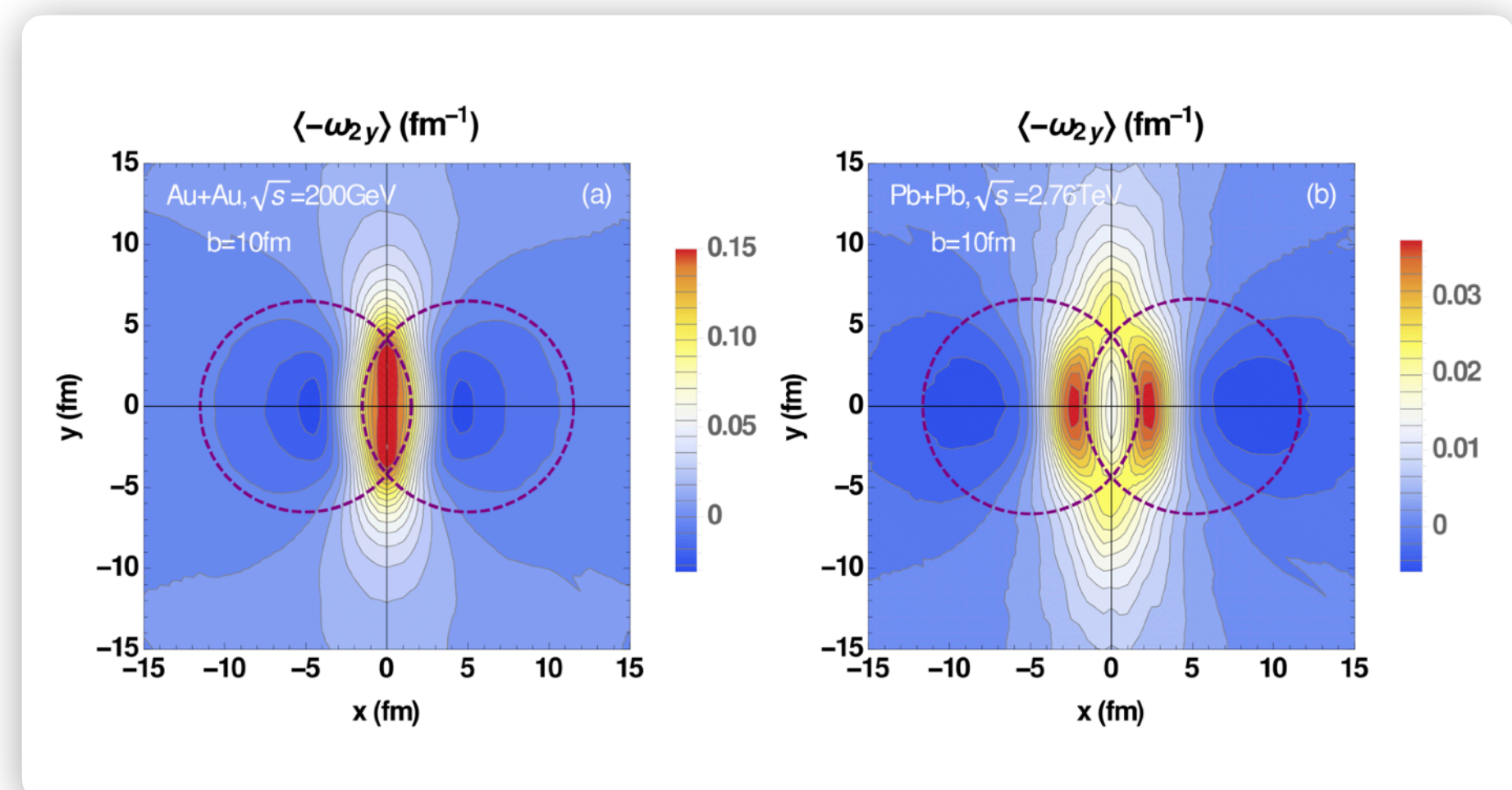
# Backup Slides

# Spin Polarization

L. Adamczyk *et al.* [STAR], Nature 548 (2017), 62-65



Deng and Huang, Phys. Rev. C 93 (2016) no.6, 064907



- Spin polarization: Alignment of particle spins with system's angular momentum
- Non-central heavy-ion collisions induce vorticity and orbital angular momentum in the QGP
- Studying polarization observables might give hints of magnetic fields as another source for polarization (Chiral Magnetic Effect)

Global polarization of quarks & anti-quarks due to spin-orbit coupling

Hadronization

Global polarization of  $\Lambda$  hyperons and other hadrons species

## Initial Conditions

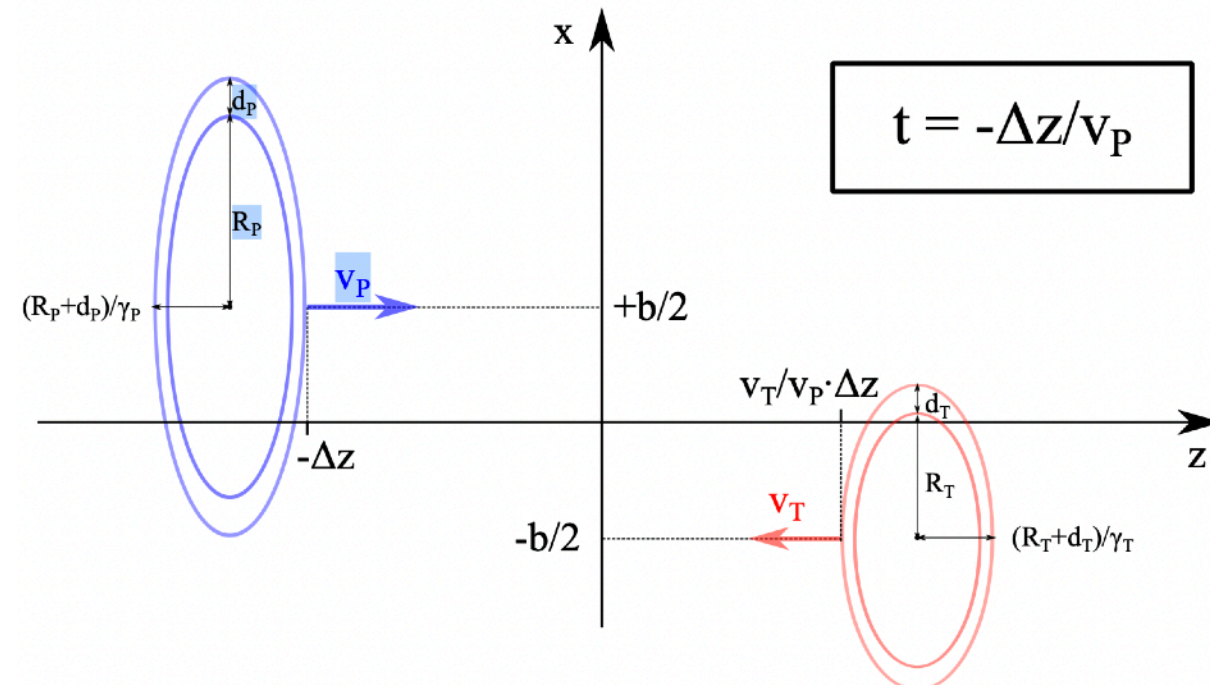
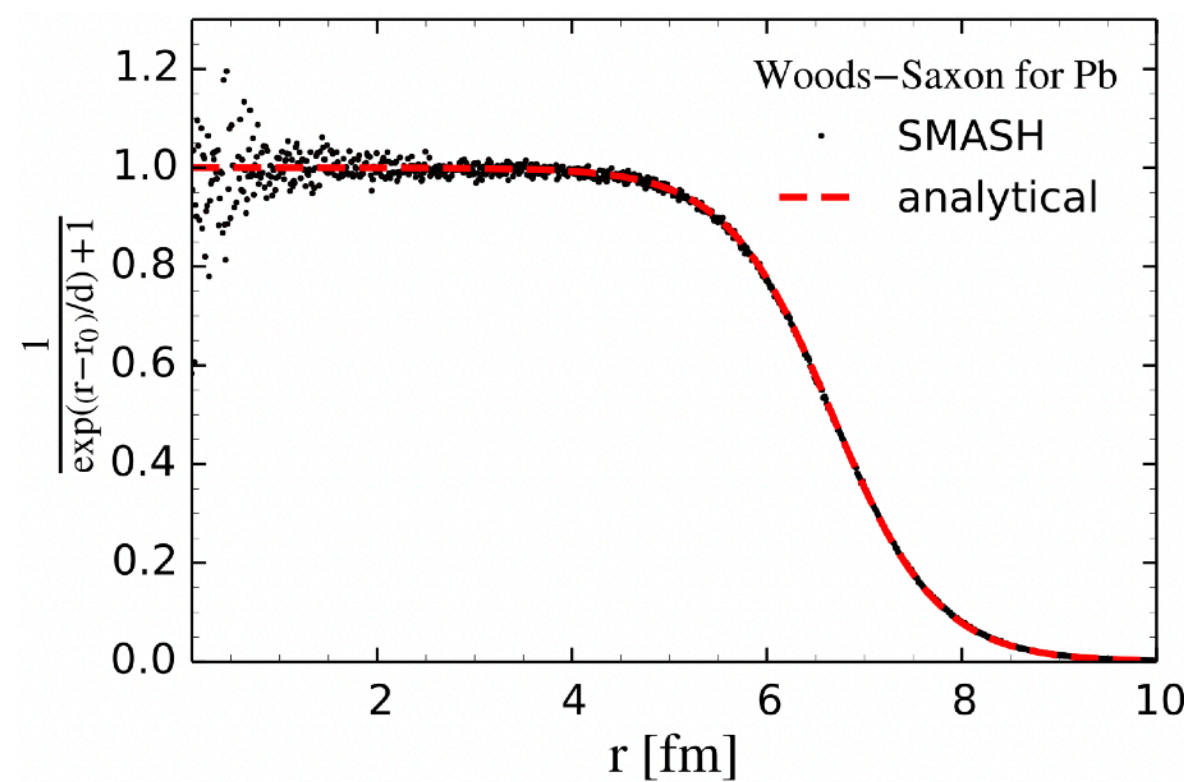
Sampling of the initial nuclei in coordinate space according to the Woods-Saxon distribution

$$\frac{dN}{d^3r} = \frac{\rho_0}{\exp\left(\frac{r-r_0}{d} + 1\right)}$$

$d$ : diffusiveness of the nucleus  
 $\rho_0$ : nuclear ground state density

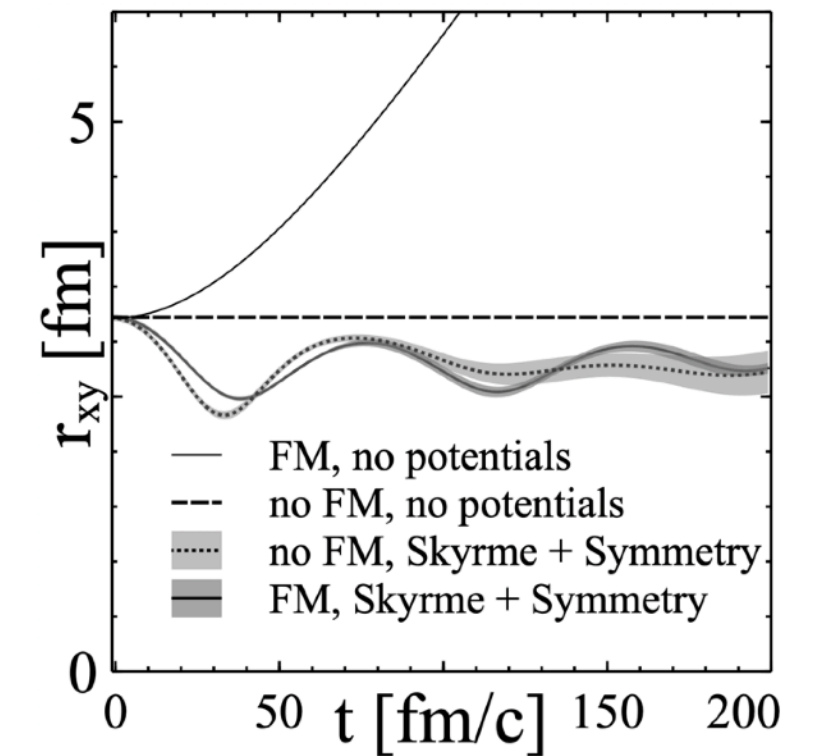
- Hard sphere limit:  $d \rightarrow 0$

J. Weil *et al.*, Phys.Rev.C 94 (2016) 5, 054905



## Fermi Motion

- Nuclei get additional momenta
- Nuclei are „stable“ if additional potentials are turned on
- „Frozen“ Fermi motion only considered for collision and turned off for propagation



## Resonances

- Particles with widths < 10 keV treated as stable
- Unstable particles assigned a relativistic Breit-Wigner spectral function

$$\mathcal{A}(m) = \frac{2\mathcal{N}}{\pi} \frac{m^2 \Gamma(m)}{(m^2 - M_0^2)^2 + m^2 \Gamma(m)^2}$$

$m$ : resonance mass  
 $M_0$ : pole mass  
 $\Gamma(m)$ : width function  
 $\mathcal{N}$ : normalization

- Decay width of two body decay  $R \rightarrow ab$  by treatment of Manley *et al.*

$$\Gamma_{R \rightarrow ab} = \Gamma_{R \rightarrow ab}^0 \frac{\rho_{ab}(m)}{\rho_{ab}(M_0)}$$

$\rho_{ab}(m)$ : mass integrals over resonance spectral functions

$$\Gamma_{R \rightarrow ab}^0 = \Gamma_{R \rightarrow ab}(M_0)$$

# Angular Momentum And Impact Parameter

Becattini et al, Phys. Rev. C77:024906, 2008

- Angular Momentum as function of the impact parameter shows a distinct maximum at a single  $b_{\max}$
- Qualitative agreement with predictions from geometrical Glauber model

