
Experimental studies of the diagram of interacting matter

- ▶ Strangeness at SPS energies
- ▶ Beam energy and system size scan of K^\pm production
- ▶ $\langle K^+ \rangle + \langle K^- \rangle \stackrel{?}{=} 2\langle K_S^0 \rangle$

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Strangeness as a probe of deconfinement

- ▶ No strangeness content in colliding nuclei.
- ▶ Sensitive to the state of matter created in the fireball.

confined matter

K mesons

$$g_K = 4$$

$$2M \approx 2 \cdot 500 \text{ MeV}$$

$$T_C \approx 150 \text{ MeV}$$



Phase transition

quark-gluon plasma

(anti-)strange quarks

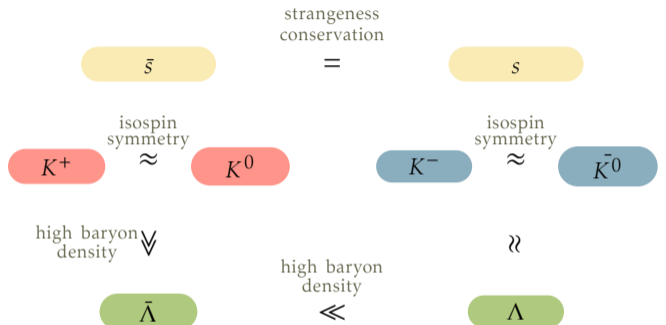
$$g_s = 12$$

$$2m \approx 2 \cdot 100 \text{ MeV}$$

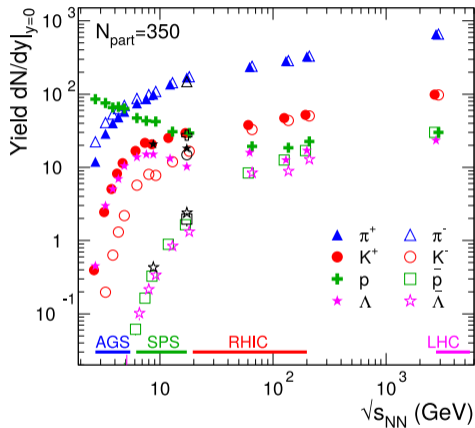
Lightest strangeness carriers:

- ▶ relatively heavy kaons ($M > T_C$) in the confined phase,
- ▶ relatively light strange quarks ($m \lesssim T_C$) in QGP.

Main strangeness carriers in A+A collisions at high μ_B



- – sensitive to strangeness content only
- ● – sensitive to strangeness content and baryon density



[Int.J.Mod.Phys.A:29,1430047,2014]

Strange definitions

Strangeness production $\langle N_{s\bar{s}} \rangle$ – number of $s\bar{s}$ pairs produced in a collision.

$$2 \cdot \langle N_{s\bar{s}} \rangle = \langle \Lambda + \bar{\Lambda} \rangle + \langle K + \bar{K} \rangle + \langle \phi \rangle + \dots$$

Strange definitions

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$$2 \cdot \langle N_{s\bar{s}} \rangle \approx \langle \Lambda \rangle + \langle K^+ + K^- + K^0 + \bar{K}^0 \rangle$$

Entropy production $\propto \langle \pi \rangle$

The experimental ratio of strangeness to entropy can be defined as:

$$E_S = \frac{\langle \Lambda \rangle + \langle K + \bar{K} \rangle}{\langle \pi \rangle} \approx \frac{2 \cdot \langle N_{s\bar{s}} \rangle}{\langle \pi \rangle}$$

$$\langle N_{s\bar{s}} \rangle \approx \langle K^+ \rangle + \langle K^0 \rangle \approx 2 \cdot \langle K^+ \rangle, \quad \langle \pi \rangle \approx \frac{3}{2} (\langle \pi^+ \rangle + \langle \pi^- \rangle)$$

$$\frac{\langle N_{s\bar{s}} \rangle}{\langle \pi \rangle} \approx \frac{2}{3} \frac{\langle K^+ \rangle}{\langle \pi^+ \rangle}, \quad E_S \approx \frac{4}{3} \frac{\langle K^+ \rangle}{\langle \pi^+ \rangle}$$

Models of strangeness production

There are multiple approaches to describe the strangeness production in HIC.

Some examples include:

- ▶ Statistical Models:

- ▶ Hadron Resonance Gas
- ▶ Statistical Hadronization Model
- ▶ **Statistical Model of Early Stage**

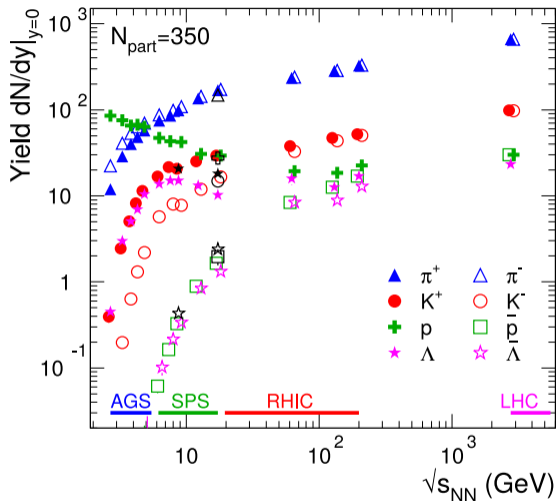
- ▶ Dynamical Models:

- ▶ Rafelski-Müller toy model
- ▶ **Parton-Hadron String Dynamics**

include deconfinement
explicitly



Particle yields – input to HRG model



The energy dependence of experimental hadron yields at mid-rapidity for various species produced in central nucleus-nucleus collisions.

Hadron Resonance Gas

Recipe for interpreting K^+/π^+ within HRG:

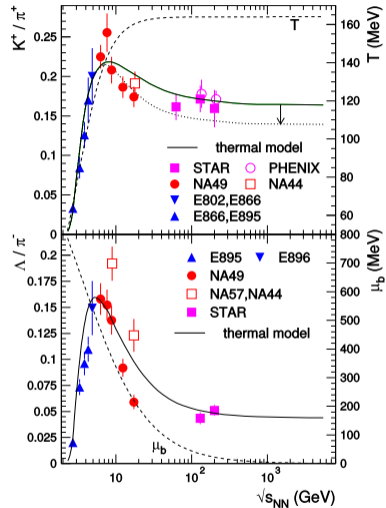
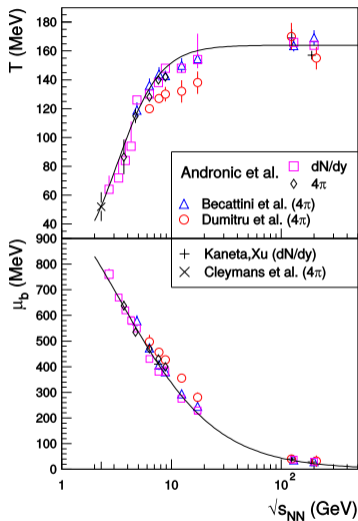
- 1 Fit V, T, μ_B to experimentally measured yields
- 2 Parametrize the T, μ_B dependence on s_{NN}
- 3 Compare to the experimentally measured K^+/π^+

Expected:

- ▶ Smoother than data
- ▶ Approximately reproduces experimental data (because it was the input)

Notable:

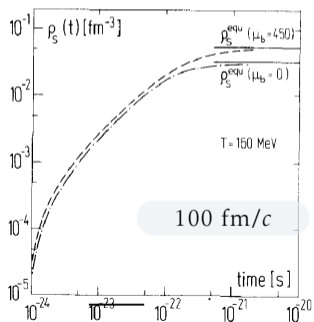
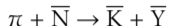
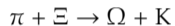
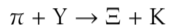
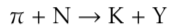
- ▶ Fitted T, μ_B evolve smoothly with s_{NN}
- ▶ Addition of σ meson and heavier resonances “enhances” the horn-like shape in the K^+/π^+ dependence on s_{NN} (dotted line)



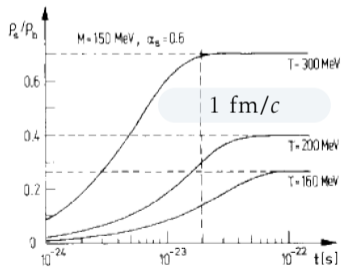
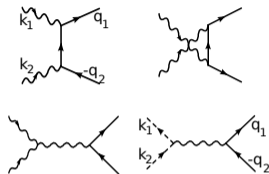
(Andronic, Braun-Munzinger, Stachel; Nucl.Phys. A834 (2010) 237C-240C)

No equilibrium? — dynamical Approach by Rafelski-Müller

strangeness production in confined matter



strangeness production in QGP



(Rafelski, Müller, Phys. Rev. Lett. 48 (1982) 1066)

Statistical Hadronization – γ_s, γ_q

Results on strangeness in equilibrium HRG were not satisfactory.

Parameter of "phase-space occupancy" γ_s introduced to improve the fits:

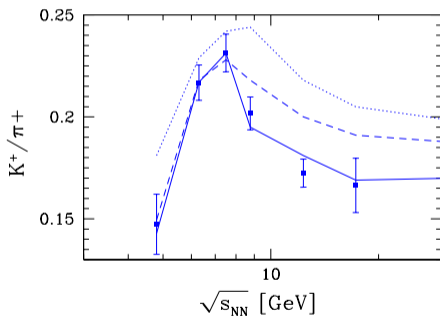
$$\langle \frac{N_s}{V} \rangle = \langle \rho_s \rangle = \int \frac{d^3p}{(2\pi)^3} \frac{1}{\lambda_s^{-1} \gamma_s^{-1} e^{E(p)/T} + 1}, \quad \langle \frac{N_{\bar{s}}}{V} \rangle = \langle \rho_{\bar{s}} \rangle = \int \frac{d^3p}{(2\pi)^3} \frac{1}{\lambda_s \gamma_s^{-1} e^{E(p)/T} + 1}$$

Due to larger mass of s quark it requires more time to saturate and so it doesn't reach equilibrium value.

→ $\gamma_s < 1$ at lower collision energies (AGS, SPS).

→ $\gamma_s = 1$ at higher energies (from RHIC).

Similarly, γ_q factor can be introduced to reflect the undersaturation of u, d quarks.



dotted: $\gamma_q, \gamma_s = 1$
dashed: $\gamma_q = 1, \gamma_s < 1$
solid: $\gamma_q, \gamma_s < 1$

but is it still a statistical model?

(J. Rafelski; Eur.Phys.J.ST 155 (2008) 139-166)

Strangeness in Statistical Model of Early Stage

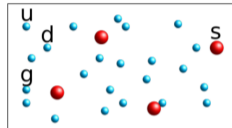
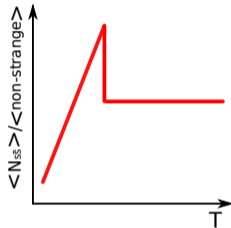
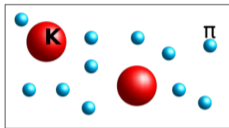
$$\langle n \rangle = \frac{gV}{(2\pi)^3} \int d^3p \frac{1}{e^{E/T} \pm 1}$$

$$\approx gV \left(\frac{MT}{2\pi} \right)^{3/2} e^{-M/T}$$

$$\approx gV \frac{2\pi^2}{4.45} T^3$$

for heavy particles

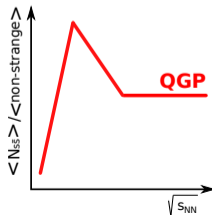
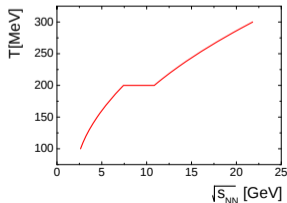
for light particles



$$\frac{\langle K \rangle}{\langle \pi \rangle} \propto \frac{MT^{3/2}}{T^3} \cdot e^{-M/T}$$

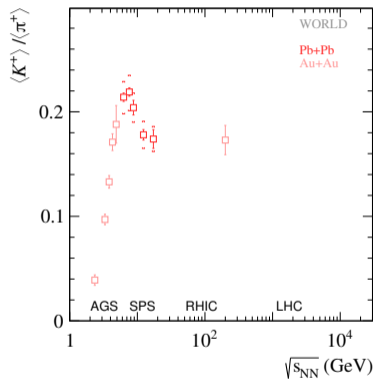
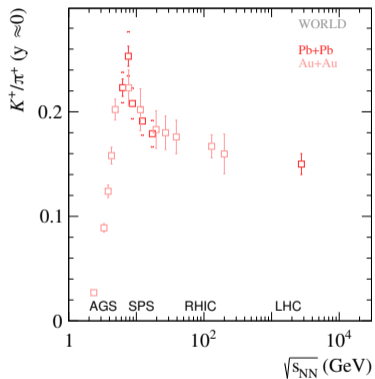
$$\frac{\langle s \rangle}{\langle u + d + g \rangle} \propto \frac{T^3}{T^3} = \text{const}(T)$$

Temperature dependence on collision energy in SMES

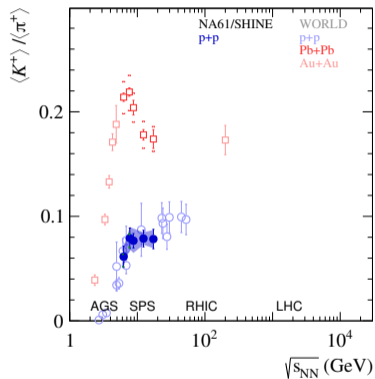
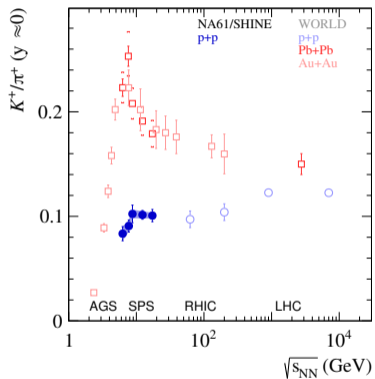


Strange/non-strange particle ratio:

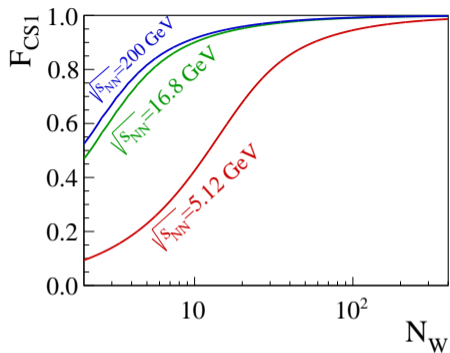
K^+/π^+ ratio dependence on collision energy



K^+/π^+ ratio dependence on collision energy

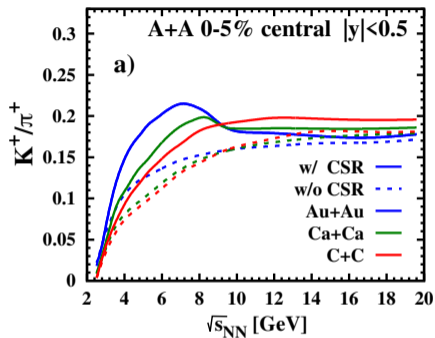


System size dependence in statistical and dynamical models



- ▶ Arises due to differences between GC and C formulation.
- ▶ Local conservation of quantum numbers severely reduces the phase space available for particle production.

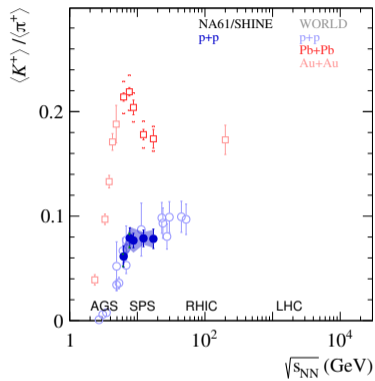
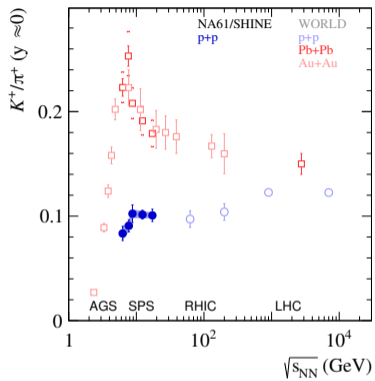
(Tounsi, Redlich; Nucl.Phys.A 715 (2003) 565c-568c)



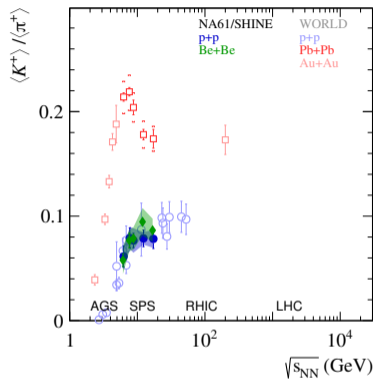
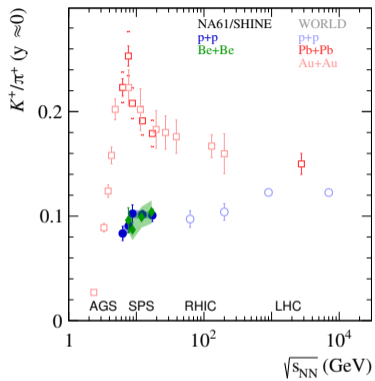
- ▶ PHSD features the onset of deconfinement.
- ▶ Predicts increase of strangeness production with system size at low collision energies (<10 GeV) and decrease at high collision energies (>10 GeV).

(Palmese et al. , PRC94 (2016) 044912)

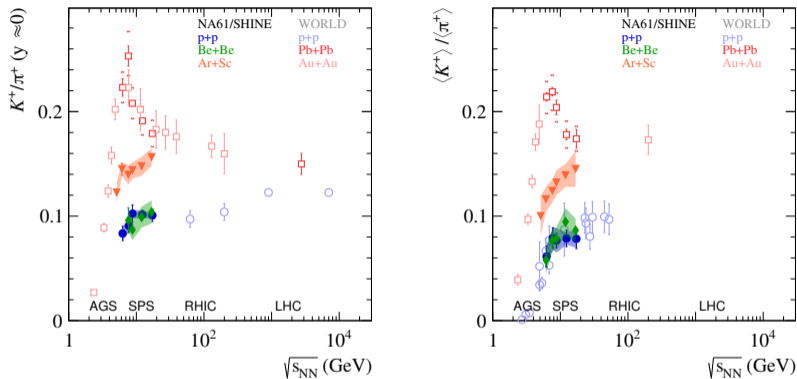
System size dependence of strangeness production



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System size dependence of strangeness production

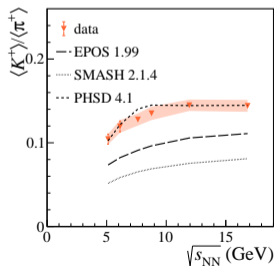
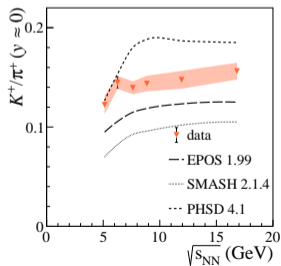
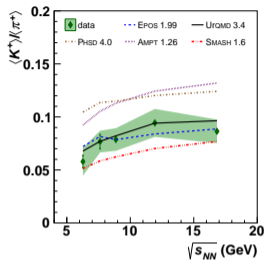
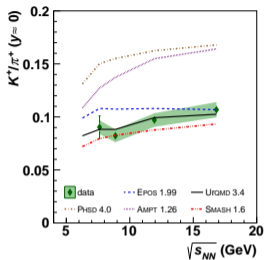


$p+p \approx \text{Be+Be} \neq \text{Ar+Sc} \ll \text{Pb+Pb}$

- ▶ No horn-like structure in Ar+Sc
- ▶ Be+Be close to p+p in K^+/π^+

- ▶ Good measure of the strangeness to entropy ratio...
- ▶ ...which is different in the confined phase (hadrons) and the QGP (quarks, anti-quarks and gluons).
- ▶ → probe of the **onset of deconfinement**.

Be+Be, Ar+Sc: K^+/π^+ ratio vs models



► K^+/π^+ ratio in midrapidity:

- reasonably well described for Be+Be by UrQMD and SMASH,
- none of the models works well for Ar+Sc.

► $\langle K^+ \rangle / \langle \pi^+ \rangle$:

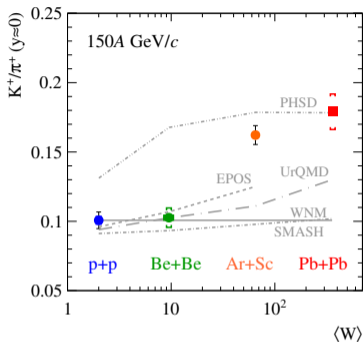
- Be+Be data well reproduced by UrQMD and EPOS, underestimated by SMASH and overestimated by AMPT and PHSD,
- only PHSD reproduces the Ar+Sc measurements.

Eur.Phys.J.C 81 (2021) 1, 73

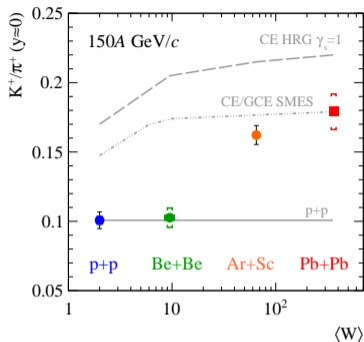
Eur.Phys.J.C 84 (2024) 4, 416

K^+/π^+ and T vs the system size at 150A GeV/c

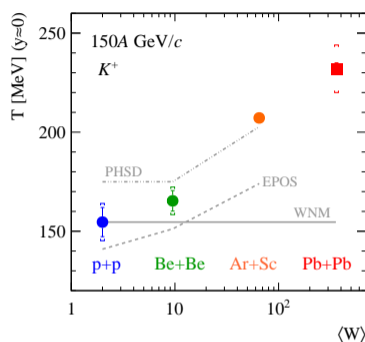
dynamical models



statistical models



dynamical models



- ▶ Beginning of the creation of large clusters of strongly interacting matter?

and large ones (Pb+Pb).
to intermediate (Ar+Sc)

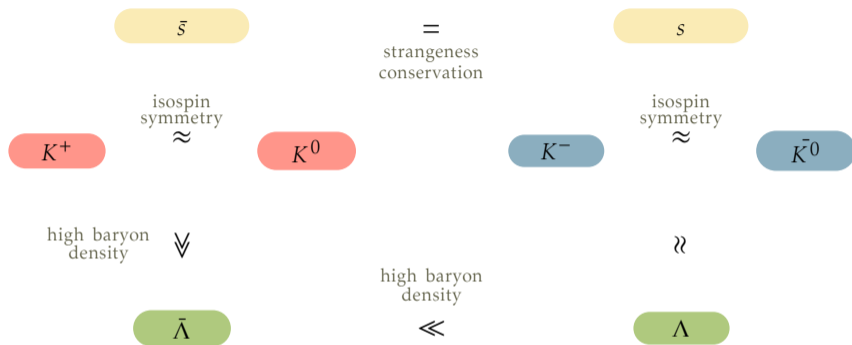
Rapid change of observables when going from small ($p+p$, Be+Be)

- ▶ None of the models reproduce K^+/π^+ ratio nor T for whole $\langle W \rangle$ range

PHSD: Eur.Phys.J.A 56 (2020) 9, 223, arXiv:1908.00451 and private communication;
SMASH: J.Phys.G 47 (2020) 6, 065101 and private communication;
UrQMD and HRG: Phys. Rev. C99 (2019) 3, 034909
SMES: Acta Phys. Polon. B46 (2015) 10, 1991 - recalculated

p+p: Eur. Phys. J. C77 (2017) 10, 671
Be+Be: Eur. Phys. J. C81 (2021) 1, 73
Ar+Sc: NA61/SHINE preliminary
Pb+Pb: Phys. Rev. C66, 054902 (2002)

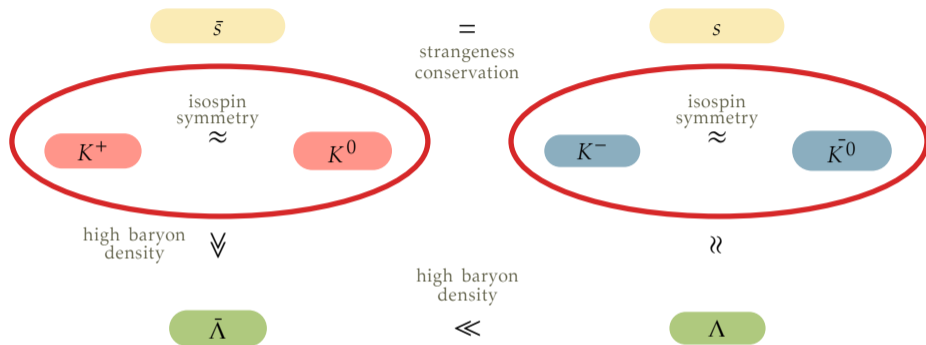
The new story: excess of charged over neutral kaons



– sensitive to strangeness content only

– sensitive to strangeness content and baryon density

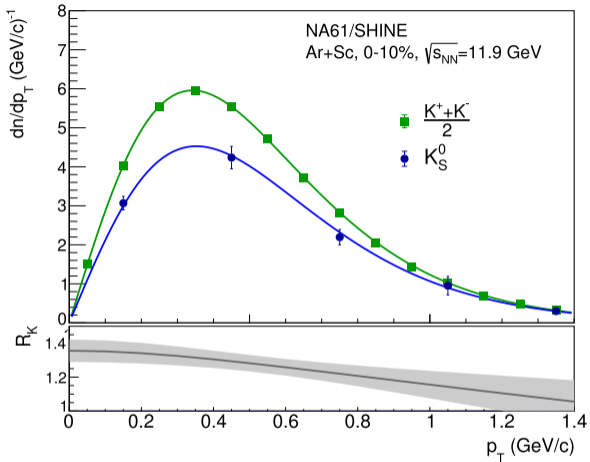
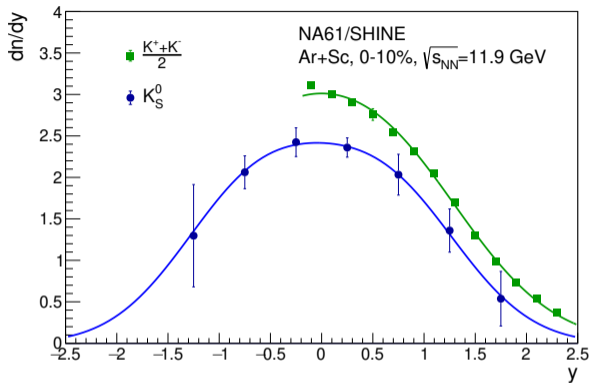
The new story: excess of charged over neutral kaons



– sensitive to strangeness content only

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The new story: excess of **charged** over **neutral** kaons



$$\frac{K^+ + K^-}{2 K_S^0} \quad \text{for } \frac{dn}{dy} \text{ at } y \approx 0 = 1.233 \pm 0.055$$

$$\frac{K^+ + K^-}{2 K_S^0} \quad \text{for integrated in } y > 0 = 1.347 \pm 0.116$$

- ~four additional charged K mesons per central Ar+Sc collision (extrapolating to 4π)

(Eur.Phys.J.C 84 (2024) 4, 416)
(arxiv:2312.06572)

Why is it surprising?

Strong interactions are **independent of flavor** in the limit of massless quarks.

$$m_u = 2.16_{-0.26}^{+0.49} \text{ MeV}, \quad m_d = 4.67_{-0.17}^{+0.48} \text{ MeV} \quad \text{and} \quad m_s = 93.4_{-3.4}^{+8.6} \text{ MeV}$$

Assuming the two colliding nuclei are made of an **equal number of protons and neutrons**:

→ equal number of valence u and d quarks *in the initial state*

→ closely equal abundances of u and d (\bar{u} and \bar{d}) quarks *in the final state*

These symmetries should (?) translate to particle production:

$$K^+(u\bar{s}) \text{ and } K^0(d\bar{s}), \quad K^-(s\bar{u}) \text{ and } \bar{K}^0(s\bar{d})$$

What can affect the particles yields?

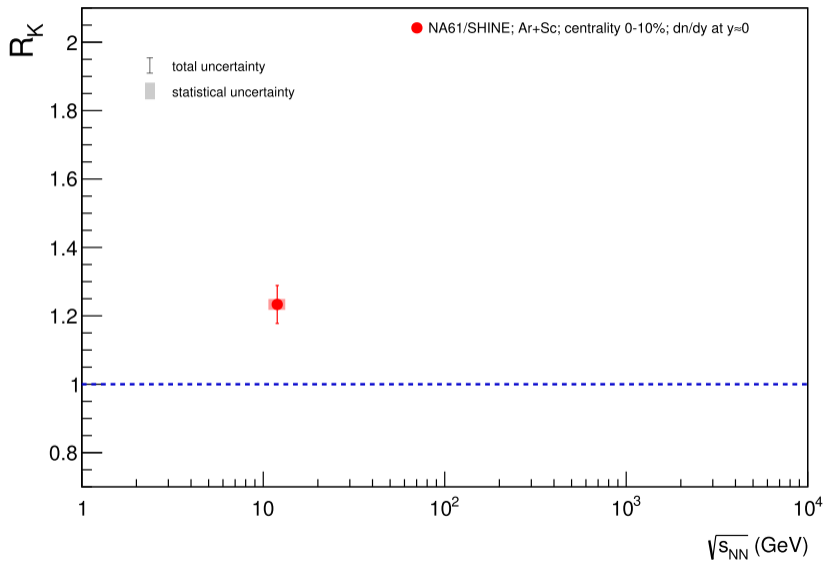
- ▶ Ar+Sc: 39 protons and 46 neutrons — 5.5% excess of d over u quarks
- ▶ Uncertainty of the mean K_S^0 lifetime \rightarrow inadequate correction for the losses
- ▶ Mass difference of quarks
- ▶ Mass difference of kaons: $m_{K^+} = m_{K^-} = 493.677 \pm 0.016$ MeV, $m_{K^0} = m_{\bar{K}^0} = 497.611 \pm 0.013$ MeV
- ▶ $\phi(1024)$ meson — decays twice as frequently to **charged kaons** as into **neutral ones**

All of the above (and more) studied quantitatively by Bryliński et al in [arxiv:2312.07176](#):

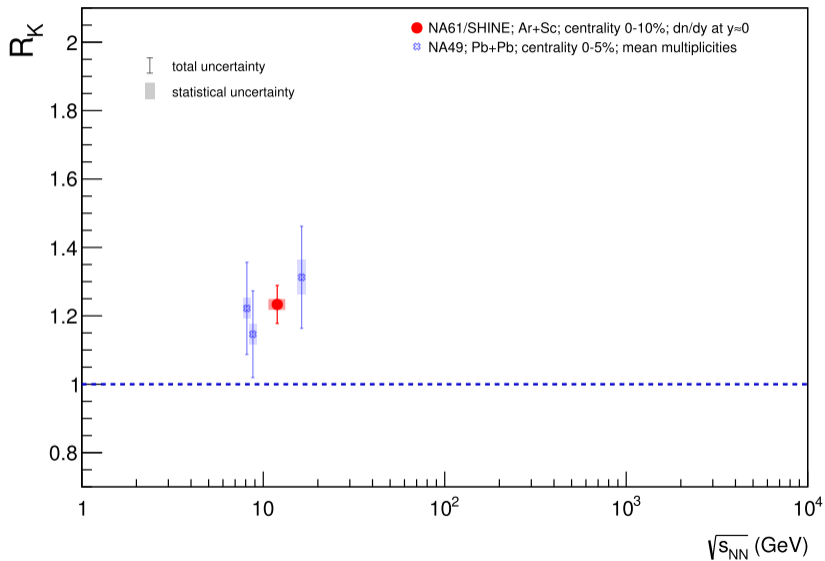
\rightarrow “at **energies larger than 10 GeV**, the mass difference between charged and neutral kaons, implying isospin symmetry-breaking processes, increases the R_K ratio by **about 0.03**”

Warning! Other effects may apply (e.g. available phase space)

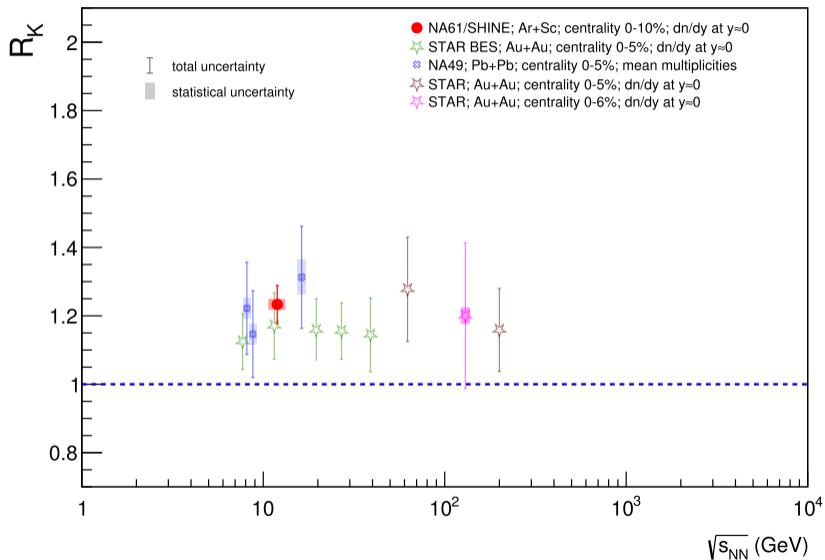
Significance of the measurement



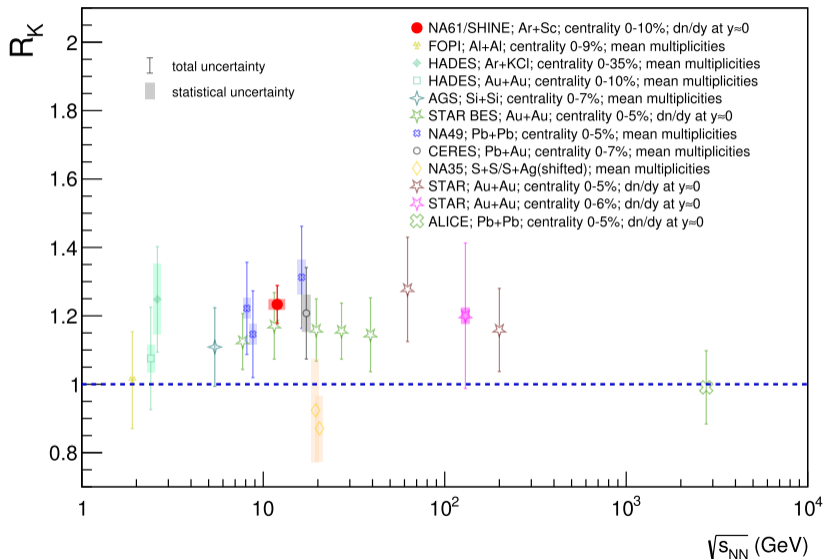
Significance of the measurement



Significance of the measurement



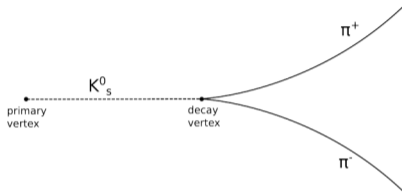
Significance of the measurement



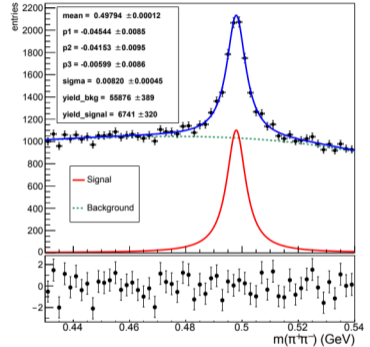
Summary

- ▶ Studying the properties of hadron production at SPS energies remains an interesting and poorly modelled topic
- ▶ New data from NA61/SHINE system size scan show unexpected features:
 - ▶ No *horn* in $^{40}\text{Ar}+^{45}\text{Sc}$!
 - ▶ **Threshold-like behavior** when going from small ($p+p$, Be+Be) to intermediate (Ar+Sc) and large systems (Pb+Pb) visible in K^+/π^+ ratio
 - ▶ The significant **excess of charged kaons over neutral ones** (measured in Ar+Sc collisions at $\sqrt{s_{\text{NN}}} = 11.9$ GeV)
- ▶ Good amount of work ahead of Ludwik and his group in Wrocław!

BACKUP SLIDES



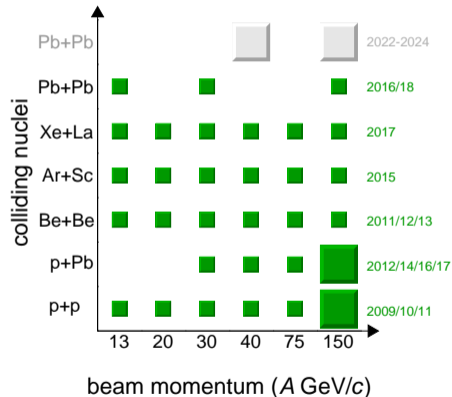
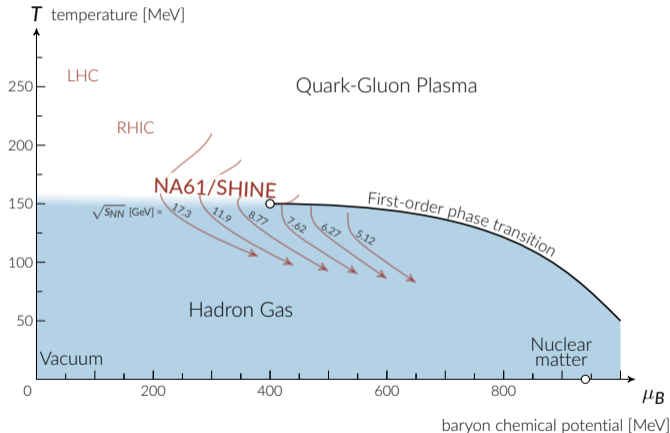
- Reconstruction based on decay topology
- K_S^0 decays into π^+ and π^- with BR $\approx 69.2\%$
- Breit-Wigner function is used to describe signal



$y \in (0.5, 1.0)$, $p_T \in (1.2, 1.5)$ GeV/c

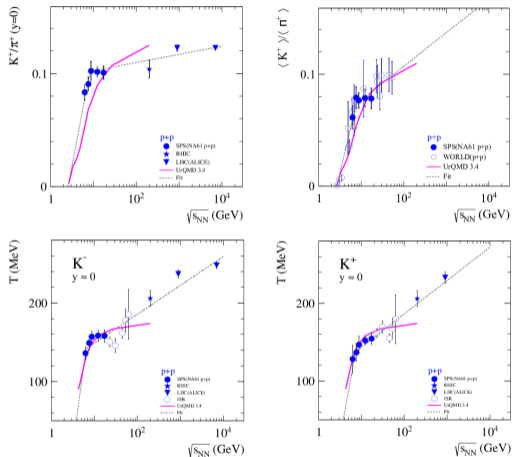
NA61/SHINE strong interactions program

Exploring the phase diagram of strongly interacting matter with a 2D scan in collision energy and system size



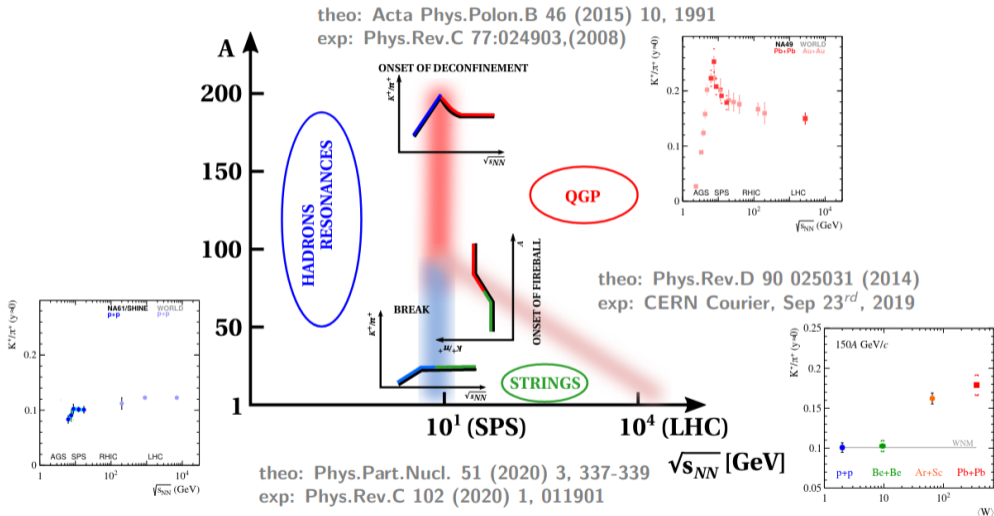
$$\sqrt{s_{NN}} \approx 5 - 17 \text{ GeV}$$

K^+/π^+ ratio and inverse slope parameter in p+p



- ▶ Rates of increase of K^+/π^+ and T change sharply in p+p collisions at SPS energies
- ▶ Models assuming change from resonances to string production mechanism follow similar trend

Uniqueness of ion results from NA61/SHINE



Model comparisons

- ▶ **EPOS** – the reaction proceeds from the excitation of strings according to Gribov-Regge theory to string fragmentation into hadrons.
- ▶ **UrQMD** starts with a hadron cascade based on elementary cross sections for resonance production which either decay (mostly at low energies) or are converted into strings which fragment into hadrons (mostly at high energies).
- ▶ **AMPT** – uses the heavy ion jet interaction generator (HIJING) for generating the initial conditions, Zhang's parton cascade for modeling partonic scatterings and the Lund string fragmentation model or a quark coalescence model for hadronization.
- ▶ **PHSD** is a microscopic offshell transport approach that describes the evolution of a relativistic heavy-ion collision from the initial hard scatterings and string formation through the dynamical deconfinement phase transition to the quark-gluon plasma as well as hadronization and the subsequent interactions in the hadronic phase.
- ▶ **SMASH** uses the hadronic transport approach where the free parameters of the string excitation and decay are tuned to match the experimental measurements in inelastic p+p collisions.

Selection of events in all model calculations follows the procedure for central collisions corresponding to the experimental results (selection based on forward spectator energy).