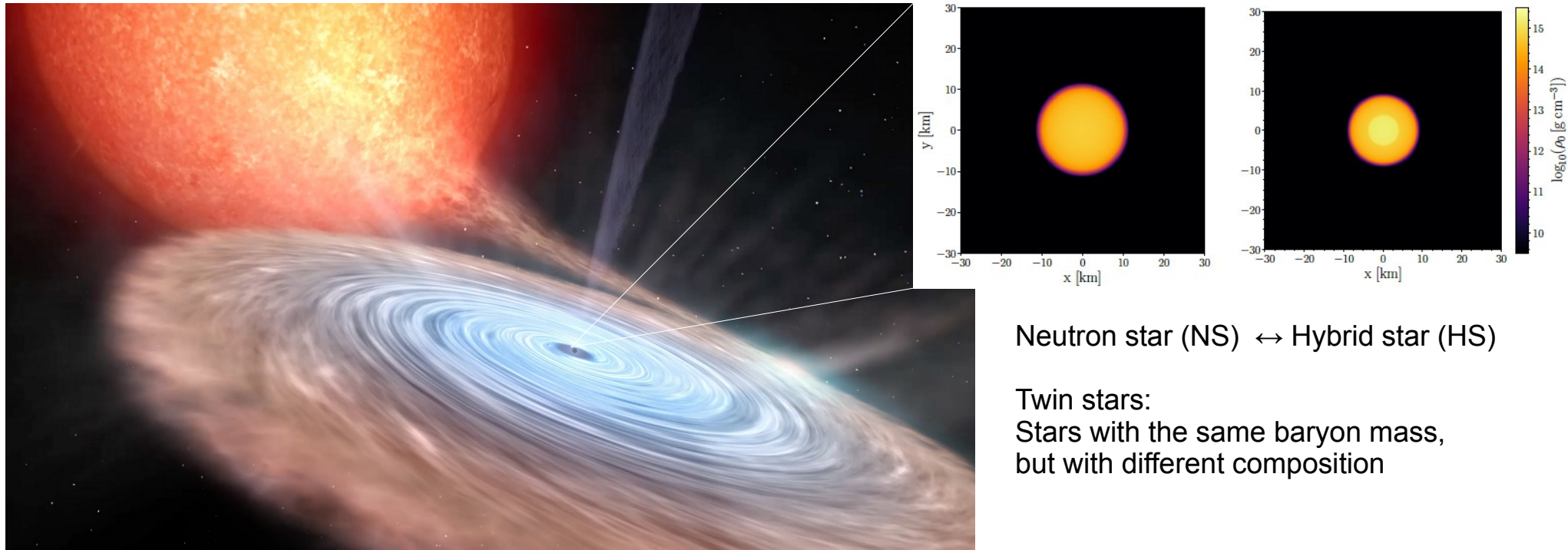


# Thermal twin stars

**David Blaschke**

University of Wroclaw, Poland & HZDR/CASUS Görlitz, Germany



Neutron star (NS) ↔ Hybrid star (HS)

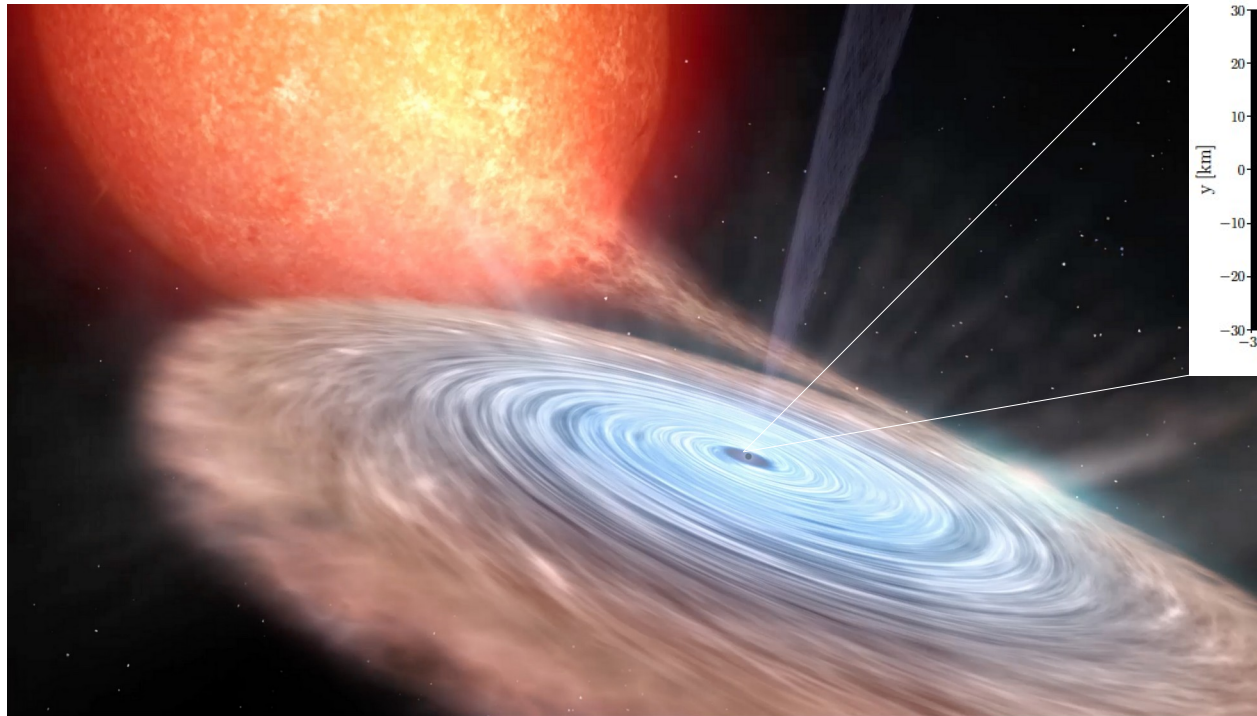
Twin stars:  
Stars with the same baryon mass,  
but with different composition

Artistic view of a neutron star accreting mass from a companion star in a low-mass X-ray binary (LMXB) system

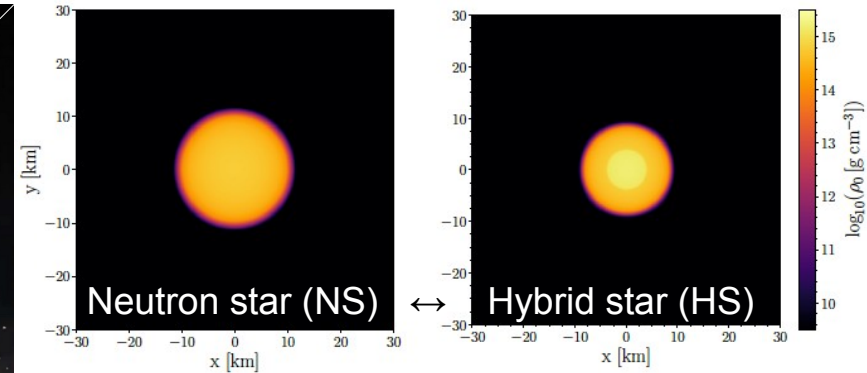
# Thermal twin stars

David Blaschke

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Artistic view of a neutron star accreting mass from a companion star in a low-mass X-ray binary (LMXB) system



## Plan:

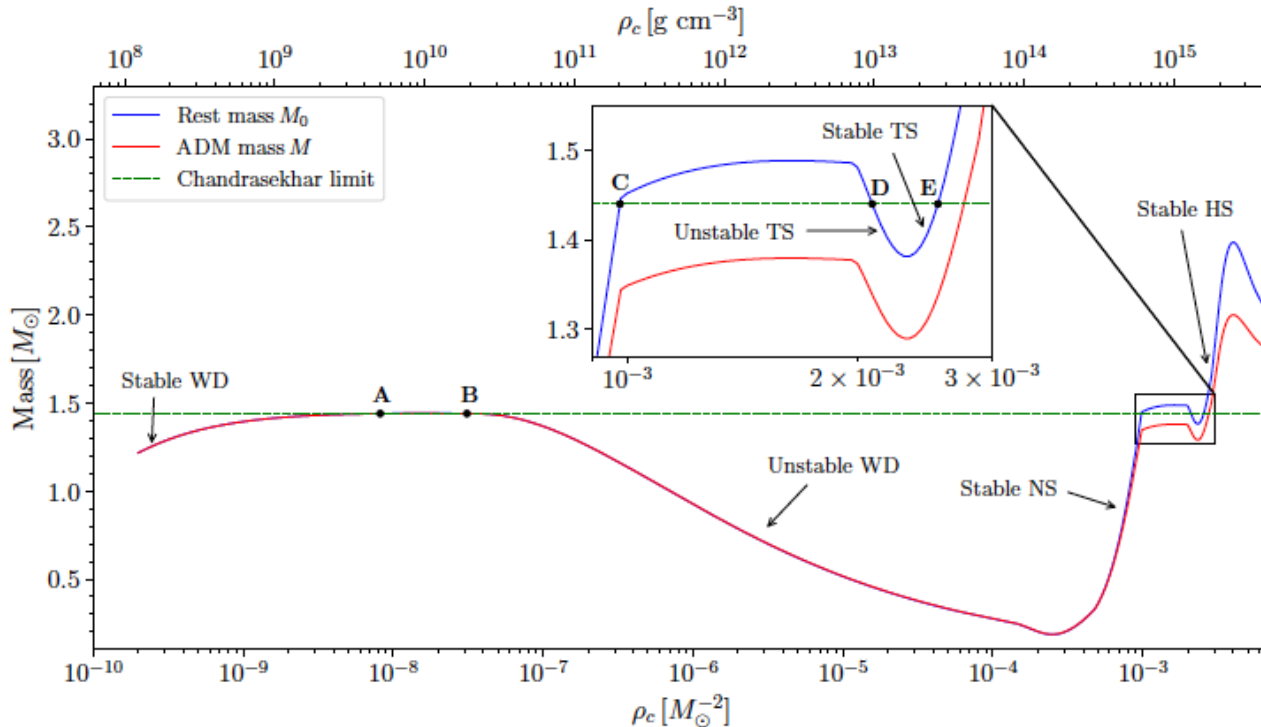
1. The idea:
  - Twins  $\rightarrow$  1st Order PT  $\rightarrow$  CEP
2. Twins in LMXB's
  - $\rightarrow$  eccentric and isolated MSP's
3. Thermal twins in CCSNe
  - $\rightarrow$  explodability of massive SG's
4. Discussion

# The idea

Three families of stable compact stars, separated by unstable configurations:

1. White Dwarfs (WD), 2. Neutron Stars (NS), 3. Hybrid Stars (HS)

Twin Stars (TS): subclass of HS for which a NS with same baryon mass exists

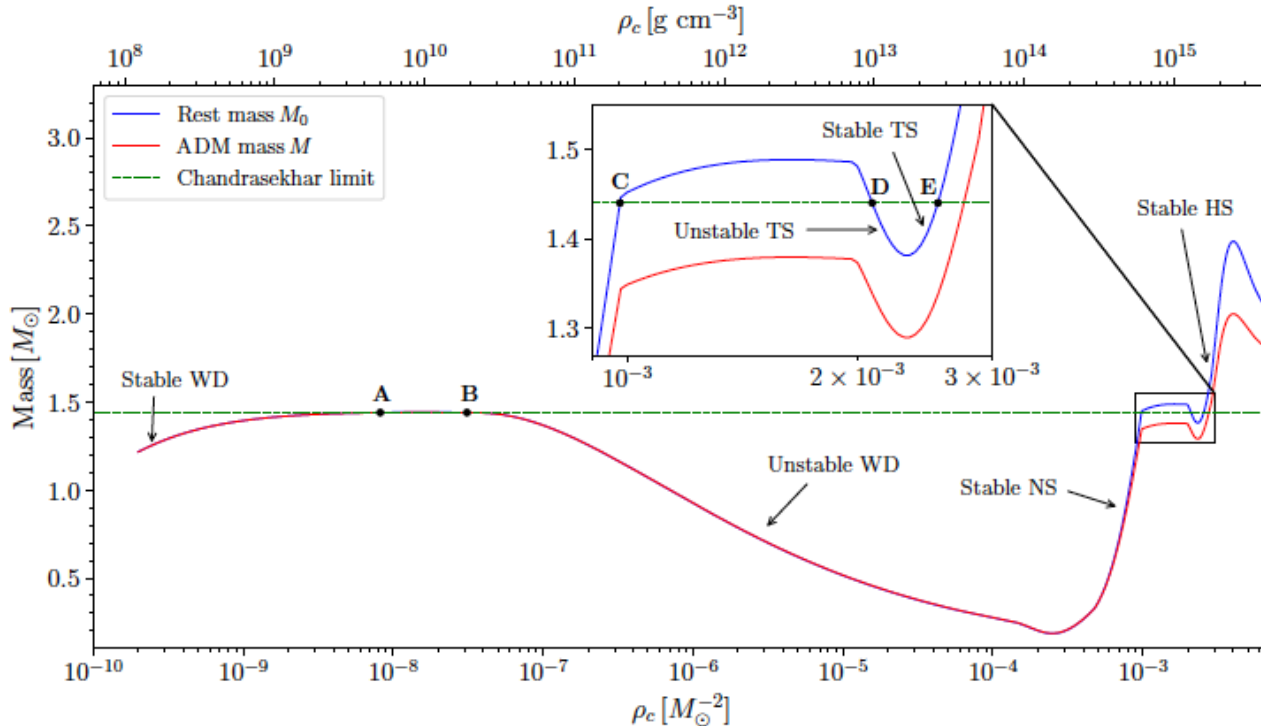


From: M. Naser, G. Bozzola, V. Paschalidis, arXiv:2406.15544

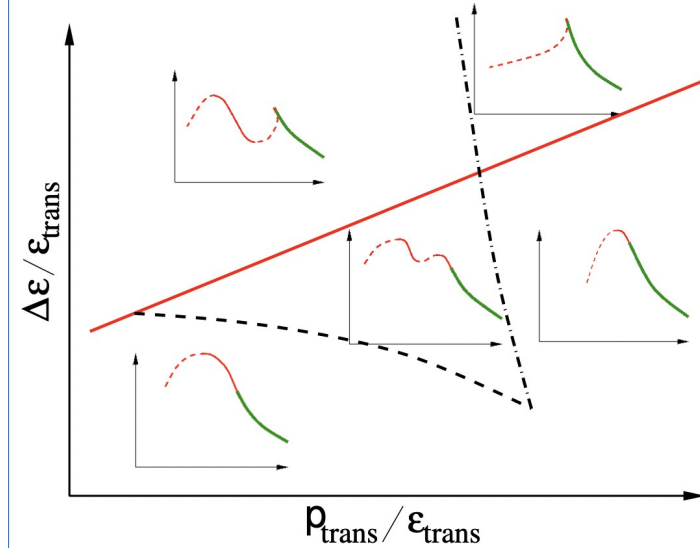
# The idea

Three families of stable compact stars, separated by unstable configurations:  
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Disconnected HS branch indicates a Strong (1st-order) phase transition



Seidov criterion for gravitational Instability (red line):

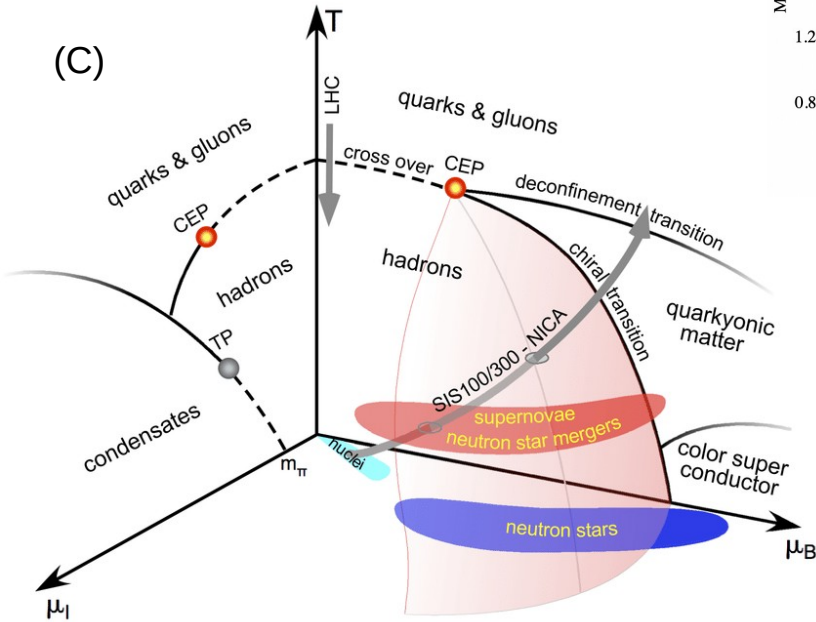
$$\frac{\Delta \epsilon_{\text{crit}}}{\epsilon_{\text{trans}}} = \frac{1}{2} + \frac{3 p_{\text{trans}}}{2 \epsilon_{\text{trans}}}$$

From: M. Naser, G. Bozzola, V. Paschalidis, arXiv:2406.15544

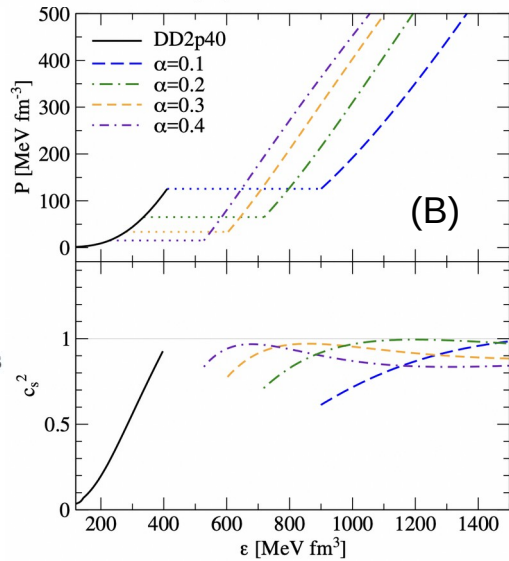
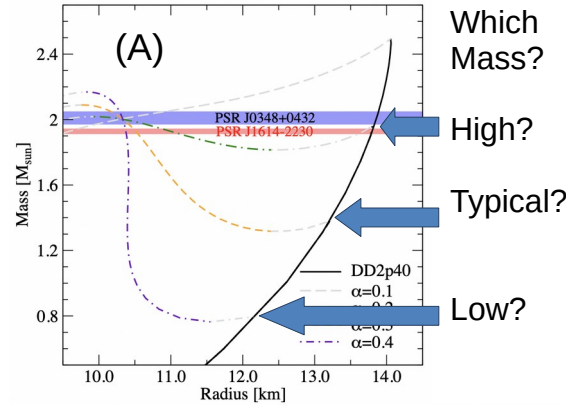
# The idea

Twin Stars (A)

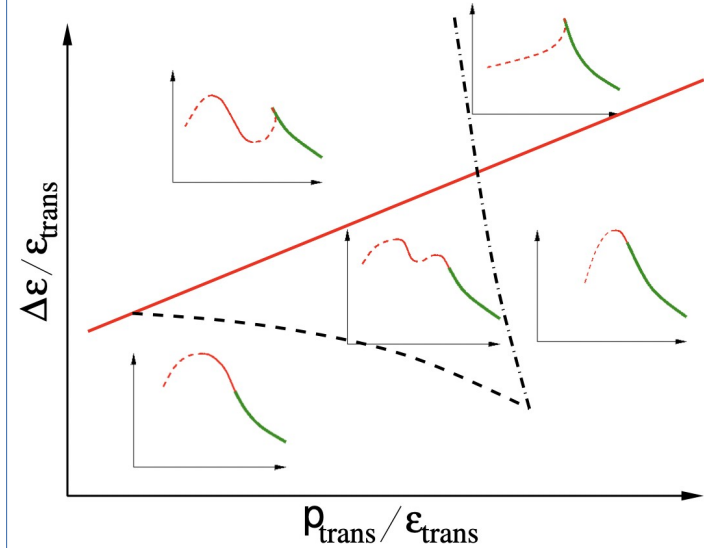
- Strong Phase Transition (B)
- Existence of CEP in Phase Diagram (C)



From: M. Kaltenborn, N. Bastian, D.B., PRD 96 (2017) 056024



Disconnected HS branch indicates a Strong (1st-order) phase transition

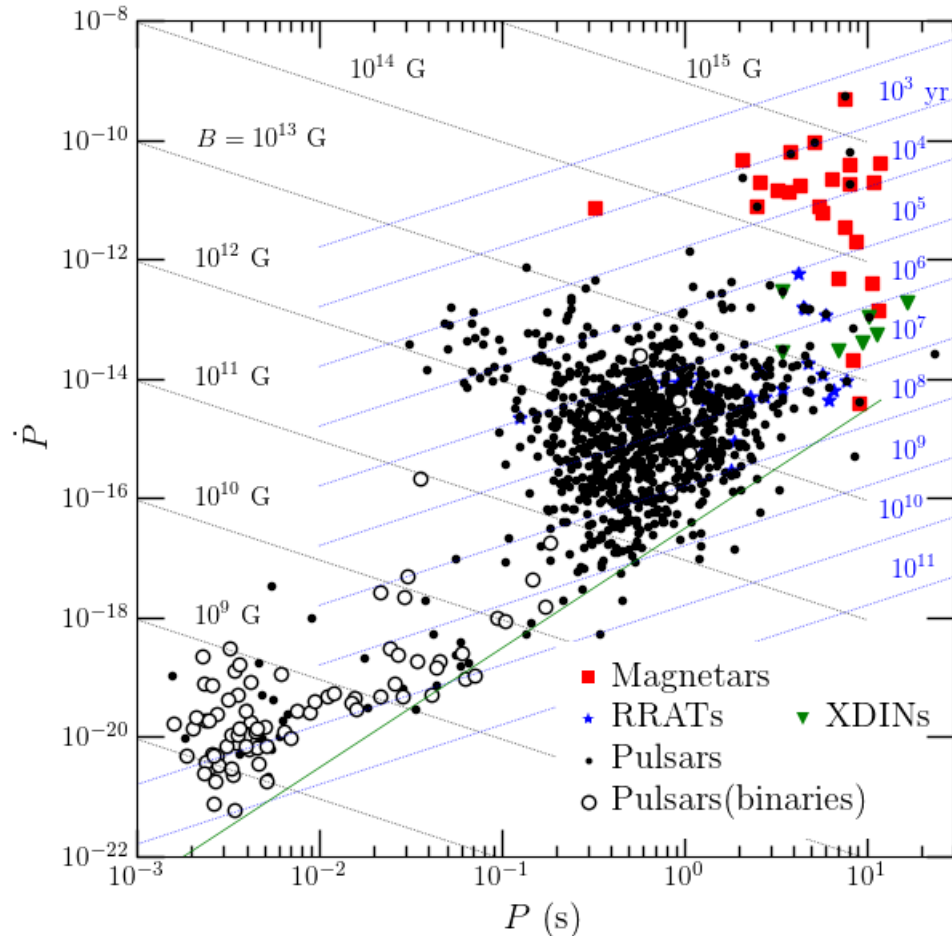


Seidov criterion for gravitational Instability (red line):

$$\frac{\Delta \epsilon_{\text{crit}}}{\epsilon_{\text{trans}}} = \frac{1}{2} + \frac{3 p_{\text{trans}}}{2 \epsilon_{\text{trans}}}$$

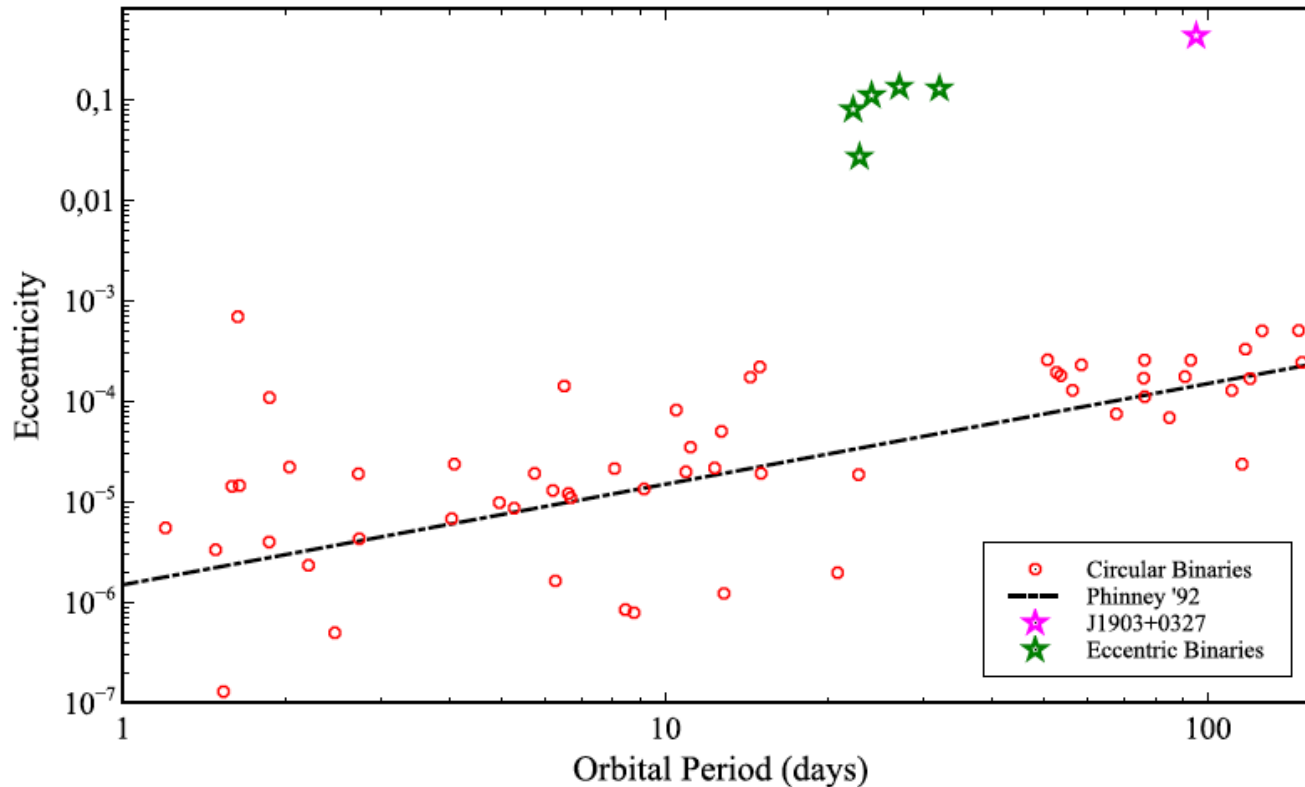


# Introduction: Millisecond Pulsars in the $\dot{P}$ -P Diagram



- Pulsars are born with periods  $P \sim 0.1 - 1.0$  seconds and magnetic fields  $B \sim 10^{12}$  G
- They spin down for millions of years and cross the „death-line“ (green) to the pulsar graveyard, where their dipole radiation is „switched off“
- Eventually, they accrete matter from a companion star in a binary system and spin-up to periods of milliseconds (MSPs)
- Presently  $\sim 600$  MSPs are known, most of them in binaries ( $\sim 500$ ) but some are isolated ( $\sim 20\%$ ) and 5 are a Puzzle!

# Introduction: The Puzzle of Eccentric MSPs



- Most MSPs are in binaries with circular orbits:  $e \sim 10^{-6} - 10^{-4}$

- Period gap 20 – 50 d, with 5 eccentric binaries with white dwarfs:  $e \sim 10^{-1}$

- One binary with a main sequence star (J1903+0327) with larger period, 100 d, and  $e \sim 1$

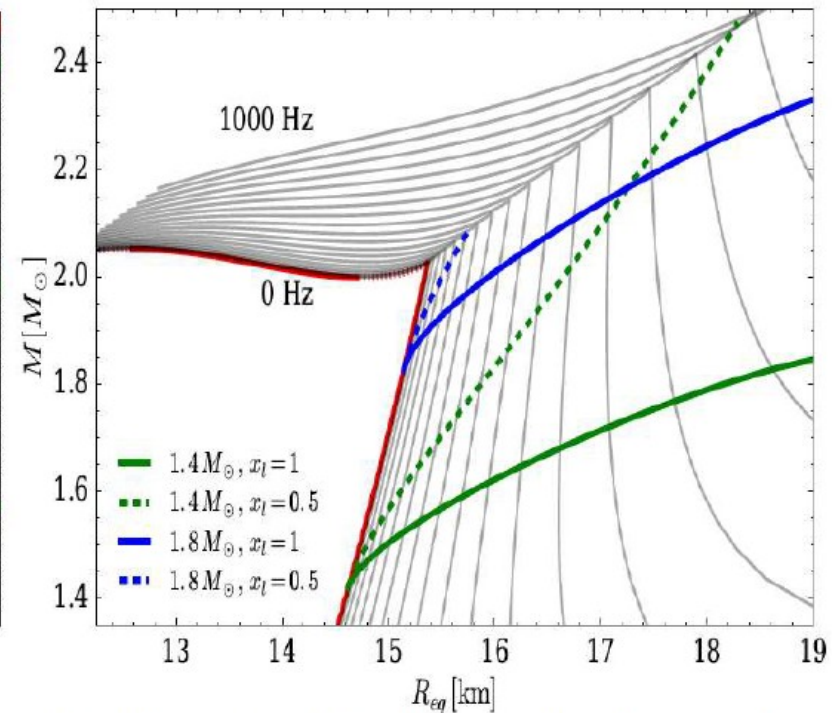
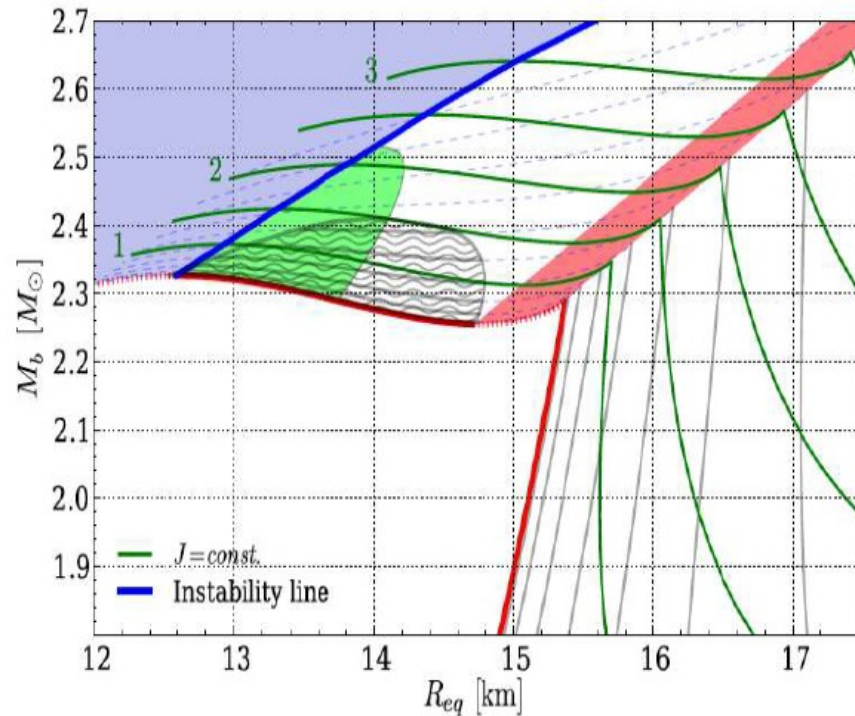
J. Antoniadis, *Astrophys. J.* 797, L24 (2014): „On the Formation of Eccentric Millisecond Pulsars with He-WD Companions“  
D. Alvarez-Castillo, J. Antoniadis, A. Ayriyan, D. Blaschke, V. Danchev et al., *Astron. Nachr.* 340 (2019) 878,  
„Accretion-induced collapse to third family compact stars as trigger for eccentric orbits of millisecond pulsars in binaries“

→ **Puzzle!**

# Let us discover the 3<sup>rd</sup> family of compact stars!

## Observation:

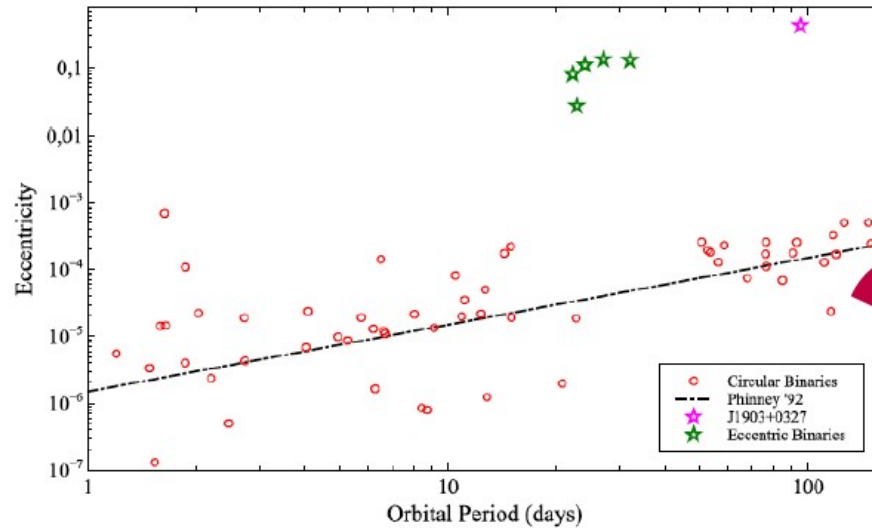
With a strong PT (mass twins), a sudden transition NS  $\rightarrow$  HS is possible, Triggered by accretion, under simultaneous conservation of  $M_b$  and  $J$





# Let us discover the 3<sup>rd</sup> family of compact stars!

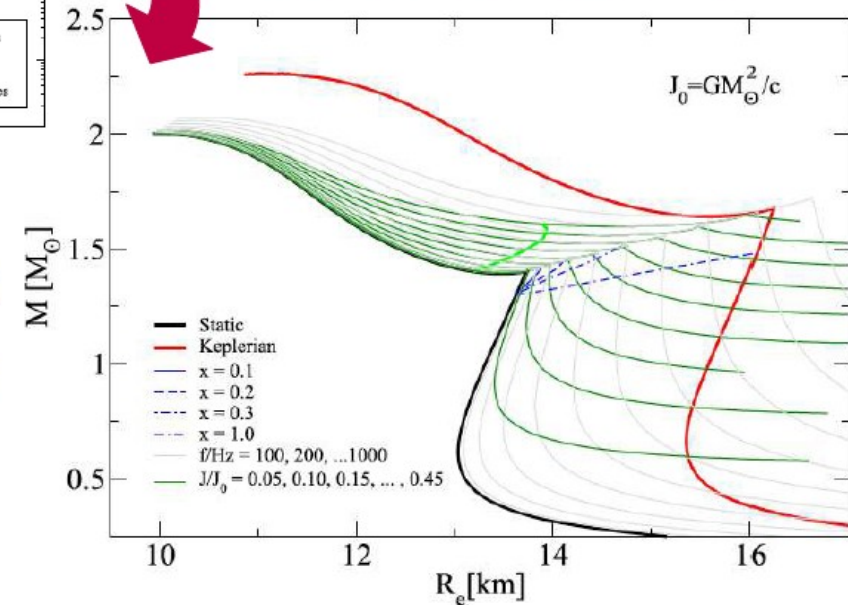
## Antoniadis-puzzle



J. Antoniadis, ApJ Lett. 797, L24 (2014)

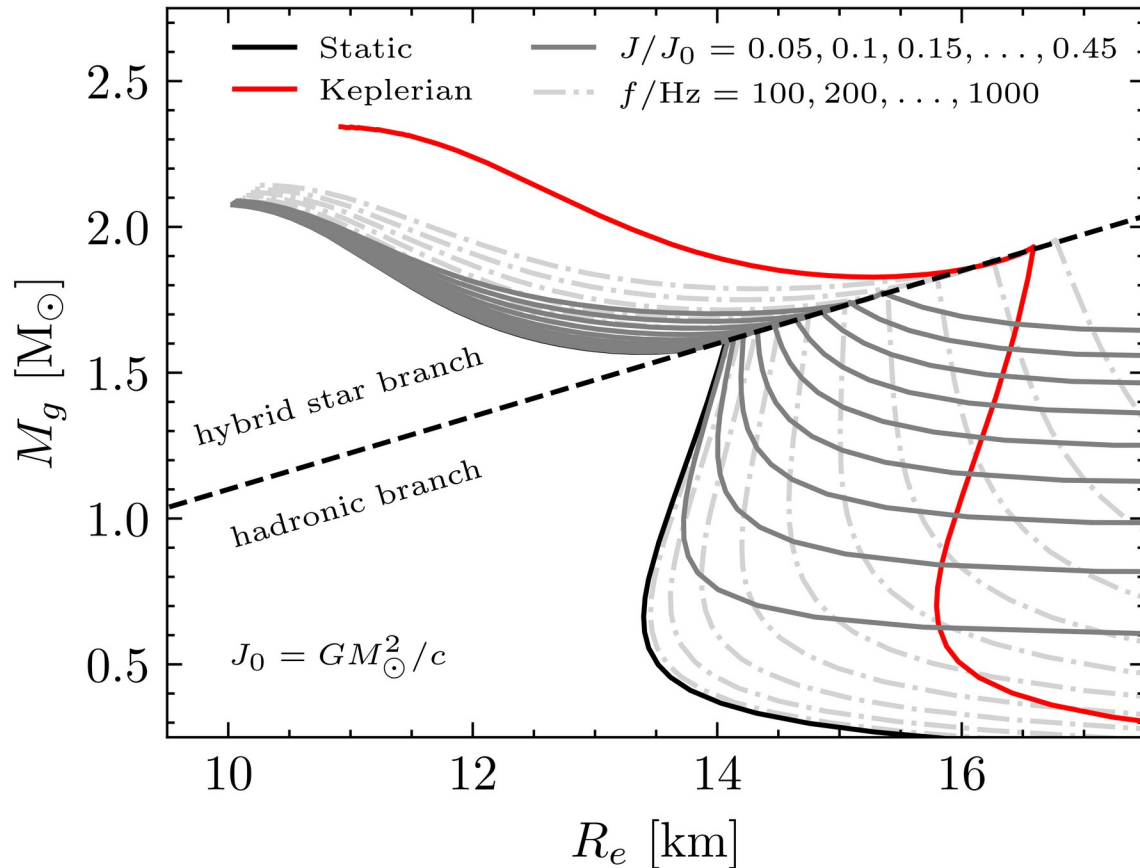
K. Stovall, P.C.C. Freire, J. Antoniadis,  
ApJ 870(2), 74 (2019)

How to relate this ?



D.E. Alvarez.Castillo, J. Antoniadis, A. Ayriyan,  
D. Blaschke, V. Danchev, H. Grigorian, N. Khosravi  
Largani, F. Weber,  
*Accretion-induced collapse to third family compact  
stars as trigger for eccentric orbits of  
Millisecond pulsars in binaries,*  
Astron. Nachr. 340 (2019) 878;  
arXiv:1912.08782 [astro-ph.HE]

# Mass Defect



- Multi-polytrope EoS [ACB-5]

$$P(n) = \kappa_i \left( \frac{n}{n_0} \right)^{\Gamma_i}$$

- Seidov criterion for instability:

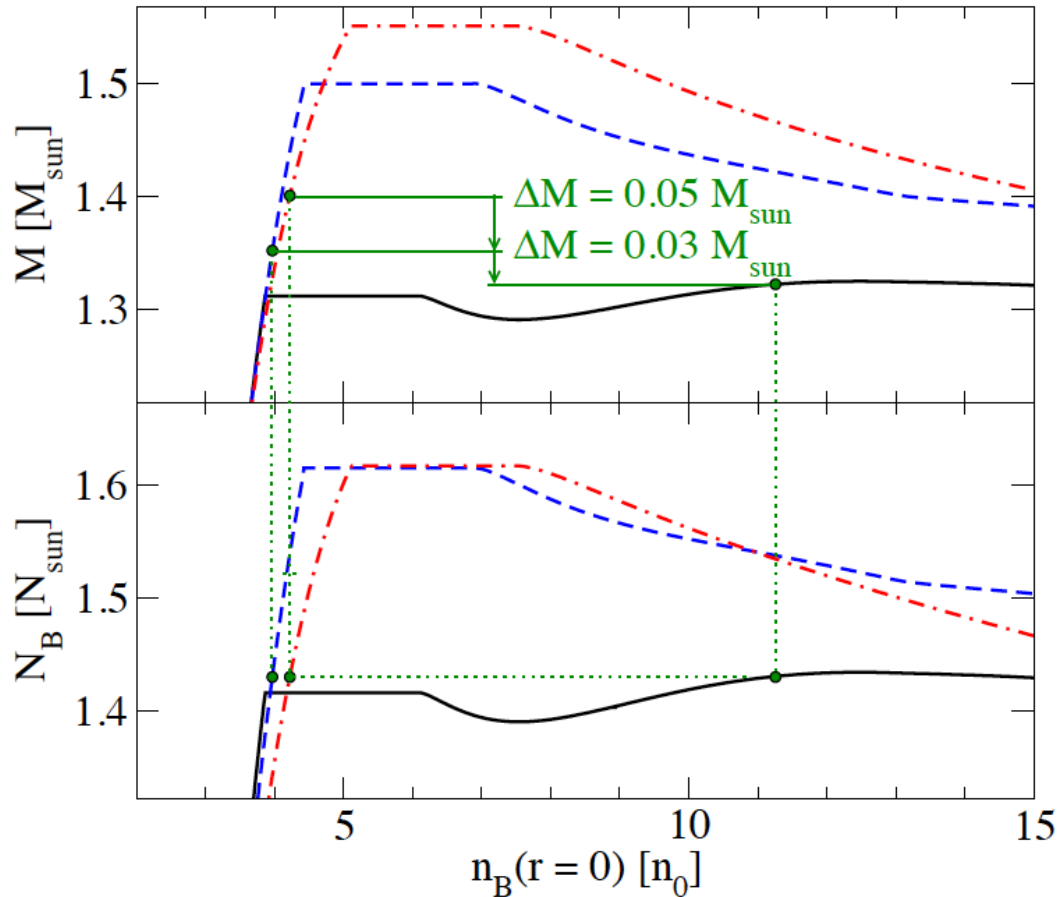
$$\Delta\varepsilon > \frac{\varepsilon_c + 3P_c}{2}$$

- Large jump in energy density (latent heat)  $\rightarrow$  instability  $\rightarrow$  3rd family of compact stars = mass twin stars

D.E. Alvarez Castillo, D. Blaschke, Phys. Rev. C 96 (2017) 045809 „High-mass twin stars with a multipolytrope equation of state“

V. Paschalidis, K. Yagi, D. Alvarez-Castillo, D. B., A. Sedrakian, Phys. Rev. D 97 (2018) 084038, „Implications from GW170817 and I-Love-Q relations for relativistic hybrid stars“

# Mass Defect

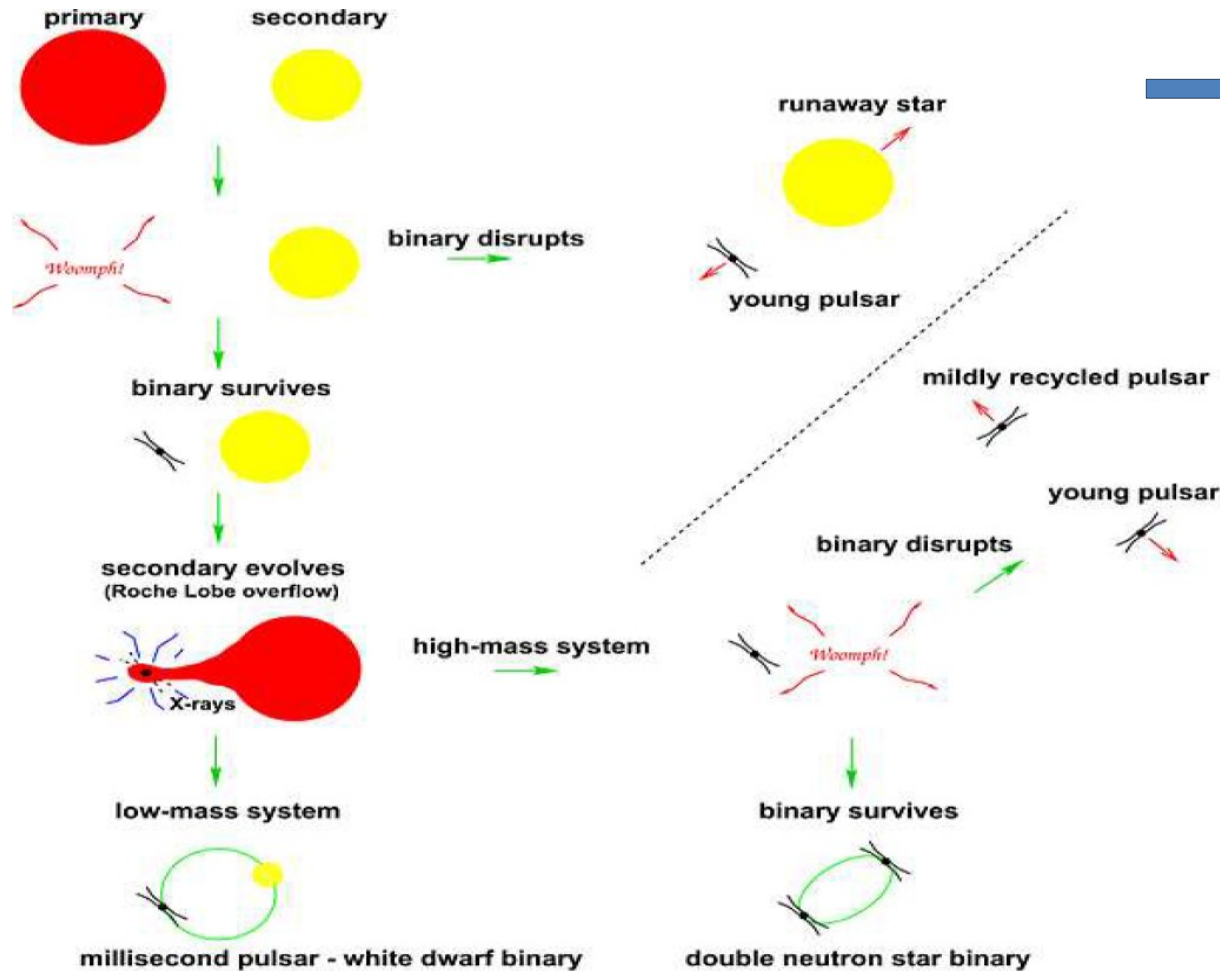


How to calculate the mass defect?

- Solve TOV equations for  $M(n_B(0))$  and  $N_B(n_B(0))$
- Consider transition at constant baryon mass  $N_B$  and constant angular momentum  $J$
- Compare the gravitational masses after the transition
- Account for neutrino trapping/untrapping by a finite chemical potential

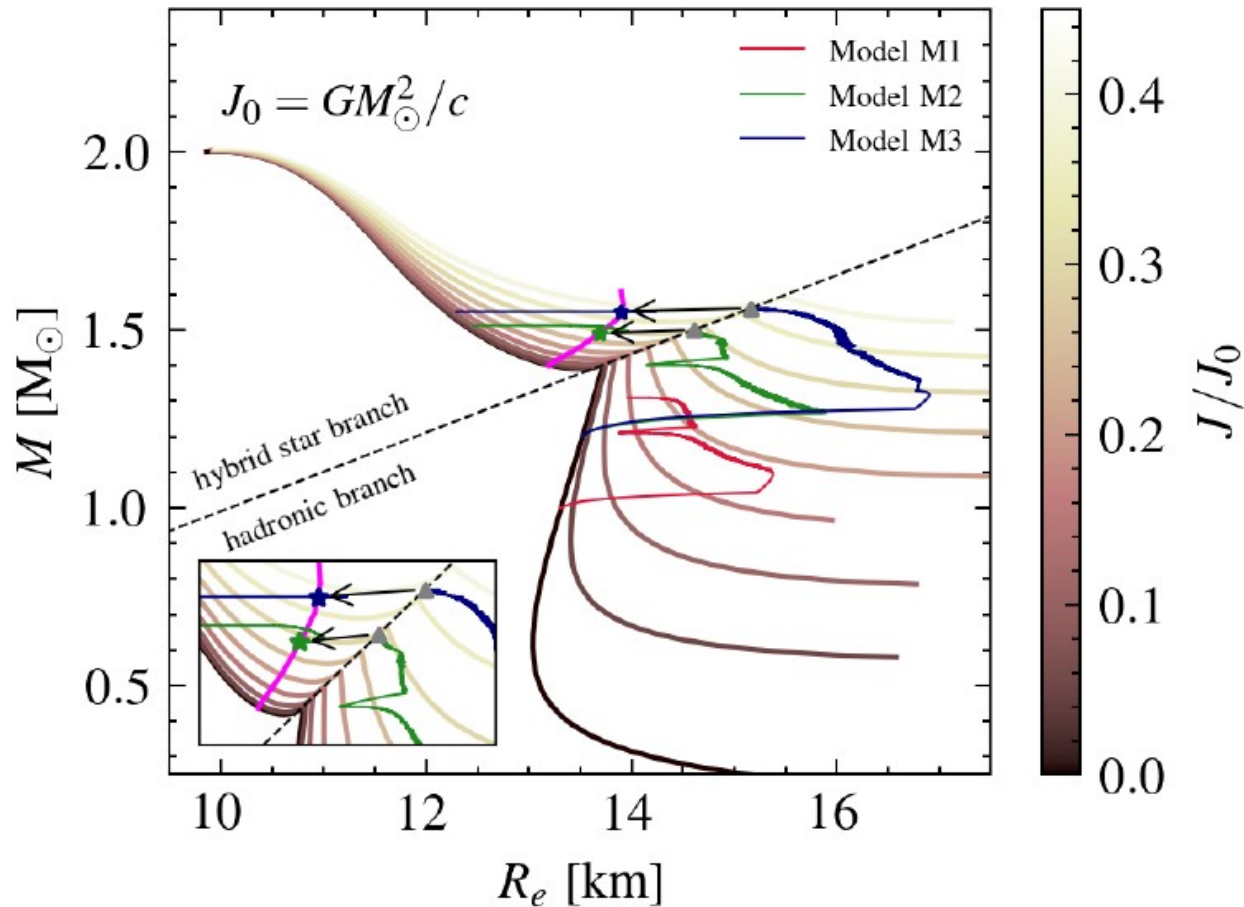
F. Sandin, D. Blaschke, Phys. Rev. D 75 (2007) 125013  
„The quark core of protoneutron stars in the phase diagram of quark matter“

# Another kick explanation: Strong QCD phase transition in NS evolution!



→ Disruption or anomalous eccentricity of a binary system due to mass defect (grav. binding) in NS catastrophic rearrangement ...

# Simulation of binary evolution



S. Chanlaridis, D. Ohse,  
J. Antoniadis, D. Blaschke,  
D.E. Alvarez-Castillo,  
V. Danchev, D. Misra and  
N. Langer:

„Formation of twin stars in  
low-mass X-ray binaries“

(in preparation for A&A)



# Simulation of binary evolution

$$\frac{a_f}{a_i} = \frac{1 - \Delta M/M}{1 - 2\Delta M/M - (w/v_{\text{rel}})^2 - 2 \cos \theta (w/v_{\text{rel}})},$$

$$v_{\text{rel}} = \sqrt{GM/a_i}$$

$w$  is the magnitude of the kick velocity,  
 $\theta$  is the kick angle

The eccentricity of the post-transition binary system is given by

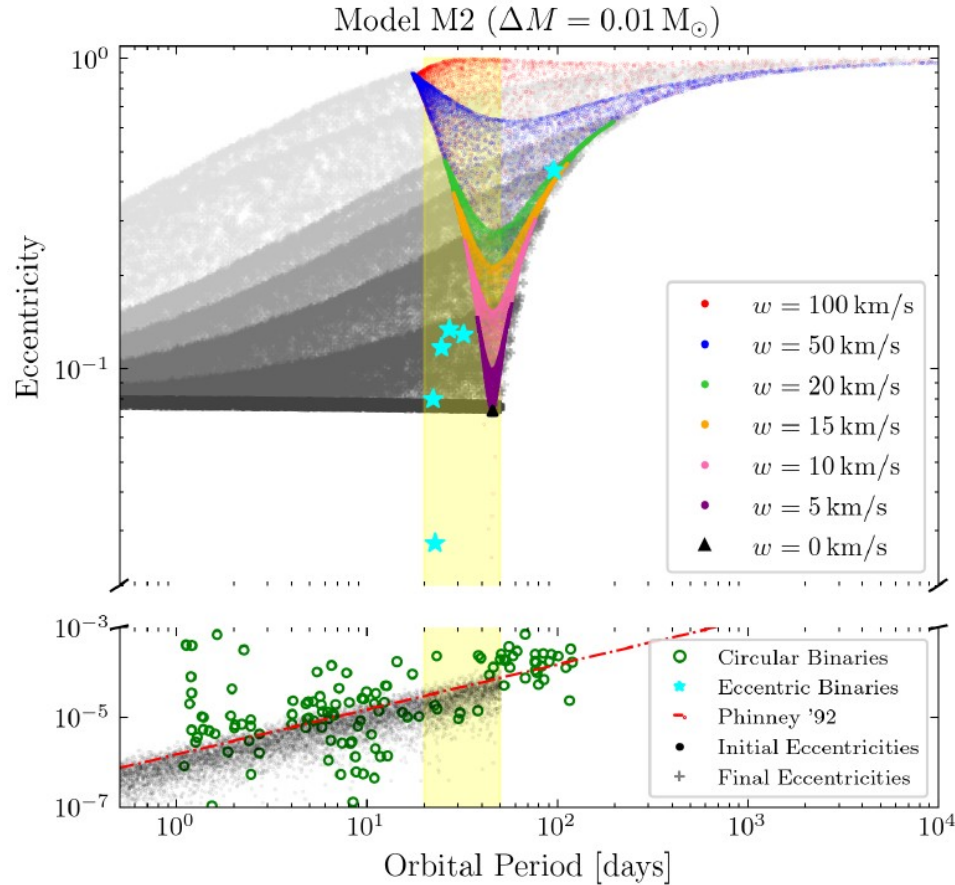
$$e = \sqrt{1 + \frac{2E_{\text{orb},f} L_{\text{orb},f}^2}{\mu_f G^2 M_{f,1}^2 M_{f,2}^2}},$$

$$L_{\text{orb},f} = a_i \mu_f \sqrt{(v_{\text{rel}} + w \cos \theta)^2 + (w \sin \theta \sin \phi)^2}$$

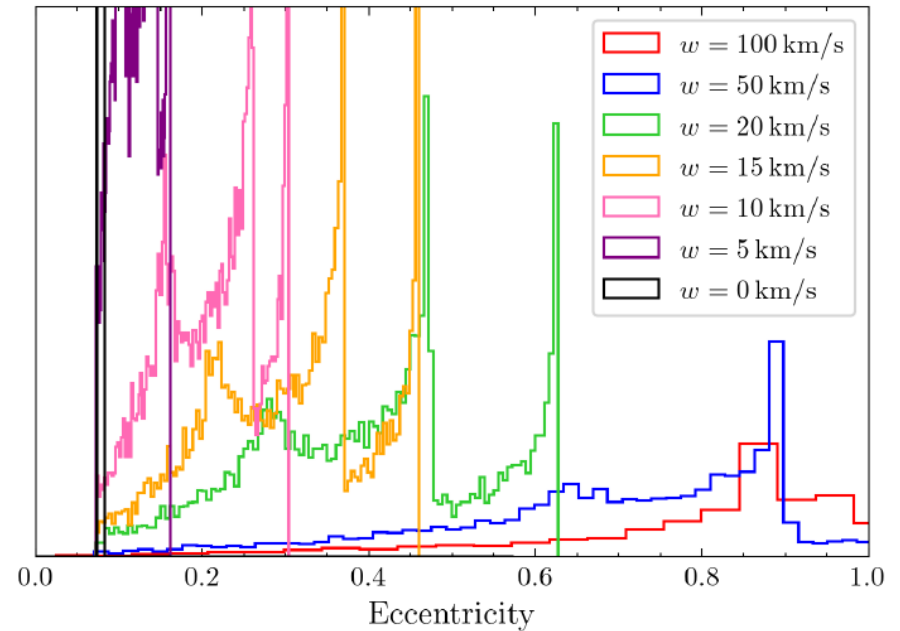
$$E_{\text{orb},f} = -GM_{f,1} M_{f,2} / 2a_f$$

Model	$M_{\text{don}} [M_{\odot}]$	$M_{\text{ns}} [M_{\odot}]$	$P_{\text{orb}} [\text{days}]$
m1	1.0	1.0	8
m2	1.0	1.2	8
m3	1.0	1.2	22.627

# Simulation of binary evolution

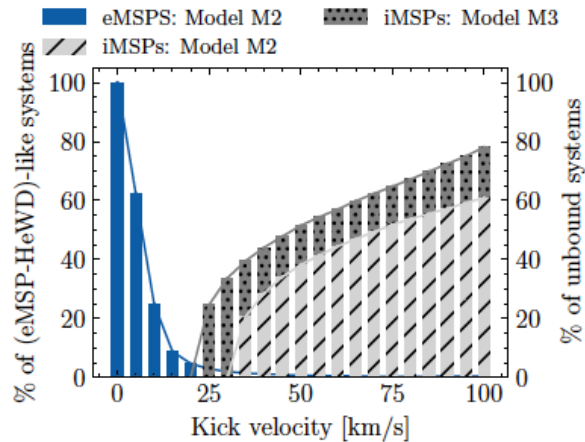


Monte-Carlo simulation of posttransition distribution orbital parameters for a mass defect of 1% solar mass due to the transition.

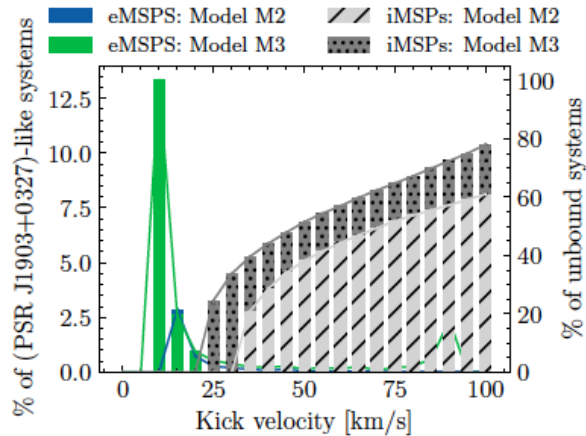


S. Chanlaridis, D. Ohse, J. Antoniadis, D. Blaschke, D.E. Alvarez-Castillo, V. Danchev, D. Misra and N. Langer:  
„Formation of twin stars in low-mass X-ray binaries“ (in preparation for A&A)

# Results for T=0 twin signals in LMXB's



- First results are promising:
- Period gap 20 – 50 d, with  $e \sim 10^{-1}$  can be addressed
- One binary with a main sequence star (J1903+0327) with larger period, 100 d, and  $e \sim 1$  can also be met
- Appearance of unbound systems → isolated MSPs

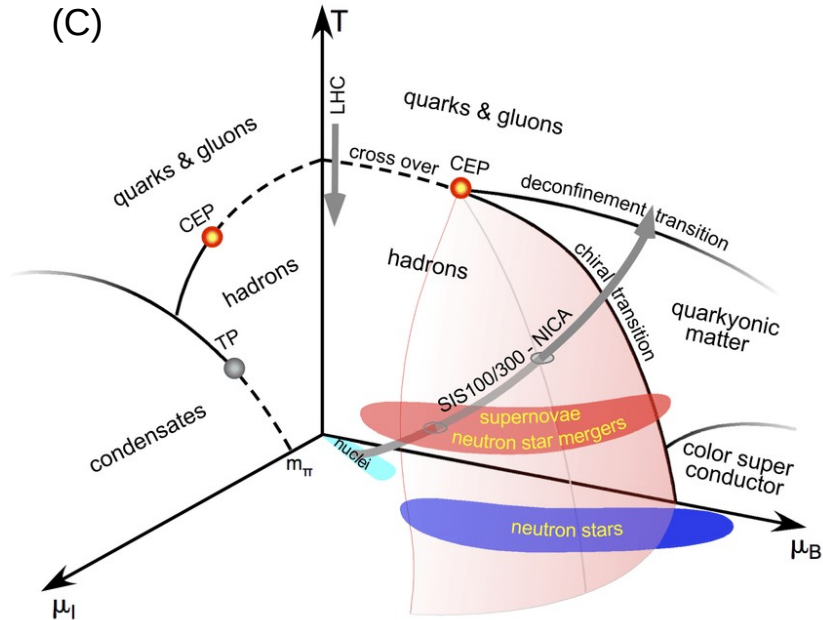


S. Chanlaridis, D. Ohse, J. Antoniadis, D. Blaschke, D.E. Alvarez-Castillo, V. Danchev, D. Misra, N. Langer:  
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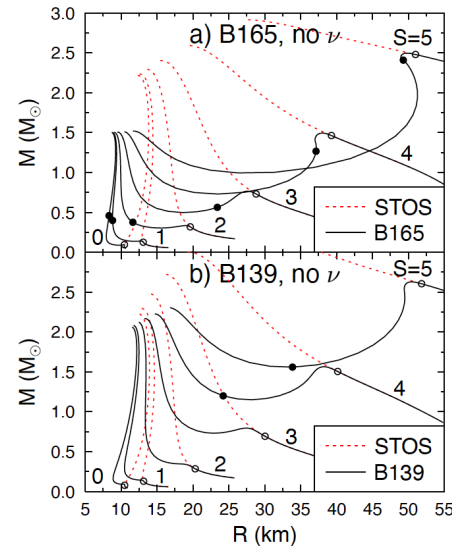
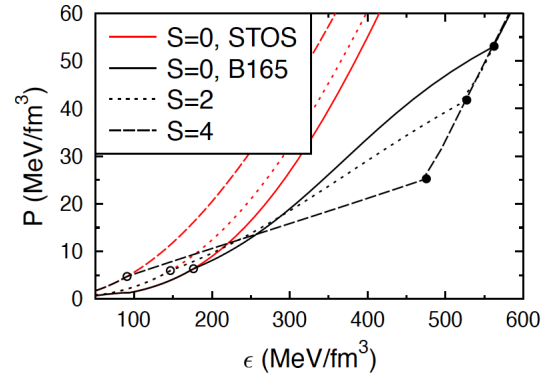
# Thermal twin stars

Observation\*:

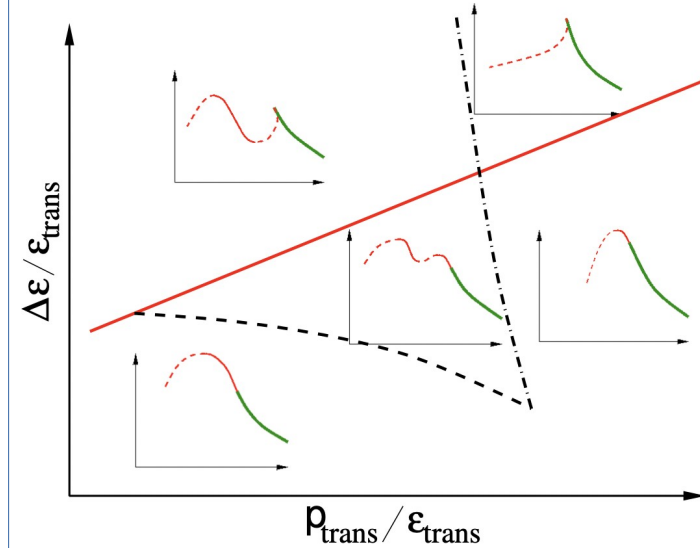
When the transition at  $T=0$  is weak, with a connected hybrid star branch, At finite  $T$  ( $s/n > 0$ ) a third family (thermal twin stars) can emerge !!



\*) M. Hempel et al., PRD 94 (2016) 103001



Disconnected HS branch indicates a Strong (1st-order) phase transition

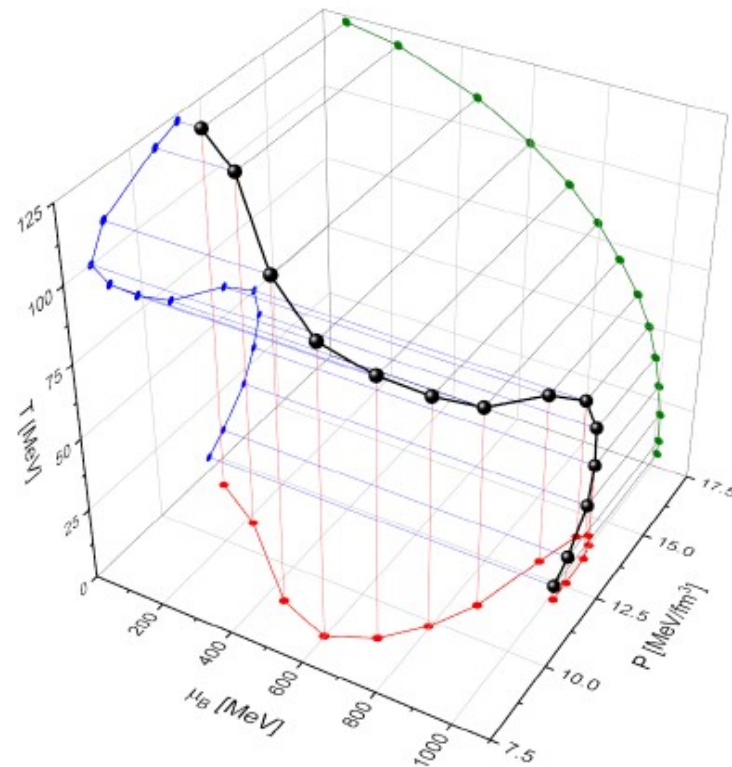
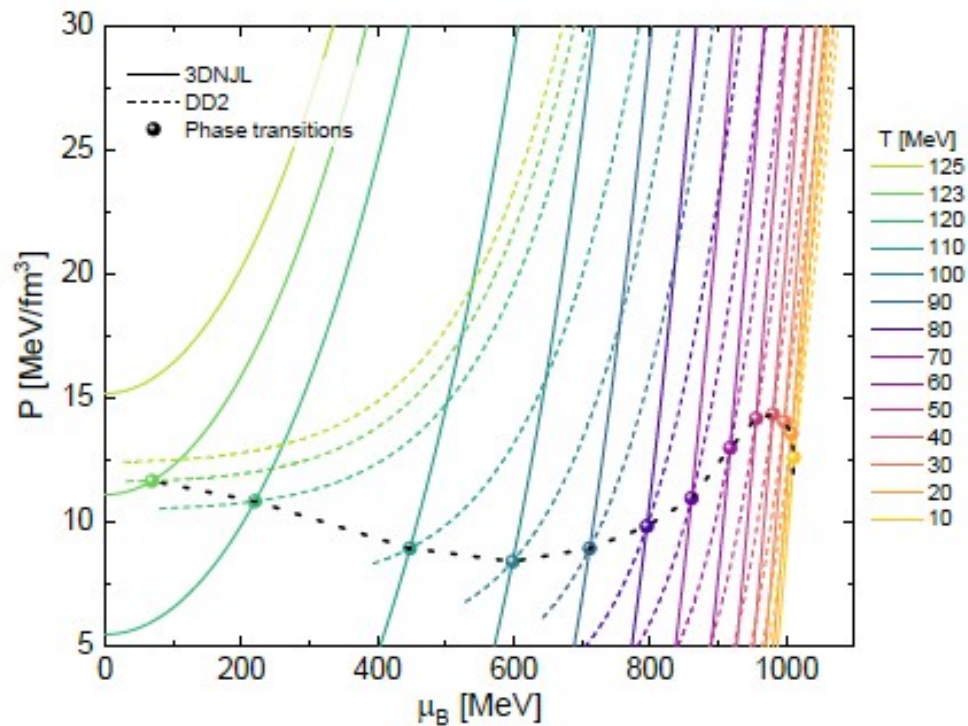


Seidov criterion for gravitational Instability (red line):

$$\frac{\Delta\epsilon_{\text{crit}}}{\epsilon_{\text{trans}}} = \frac{1}{2} + \frac{3 p_{\text{trans}}}{2 \epsilon_{\text{trans}}}$$

# Thermal twin stars

Investigation within a color superconducting, nonlocal chiral quark model\*:

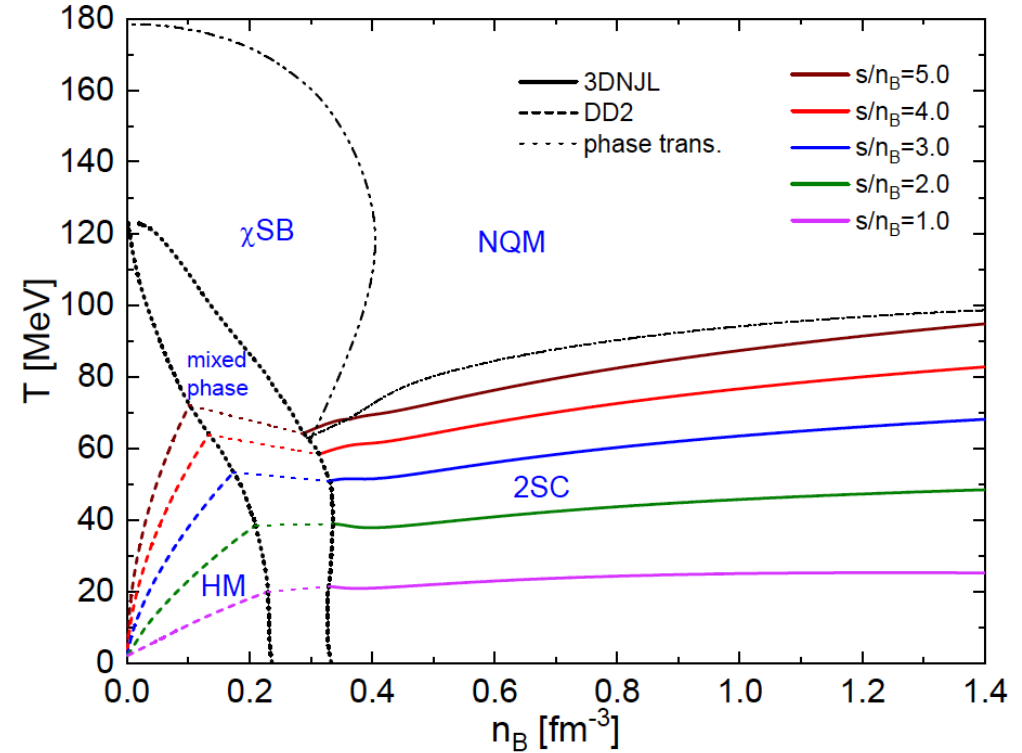
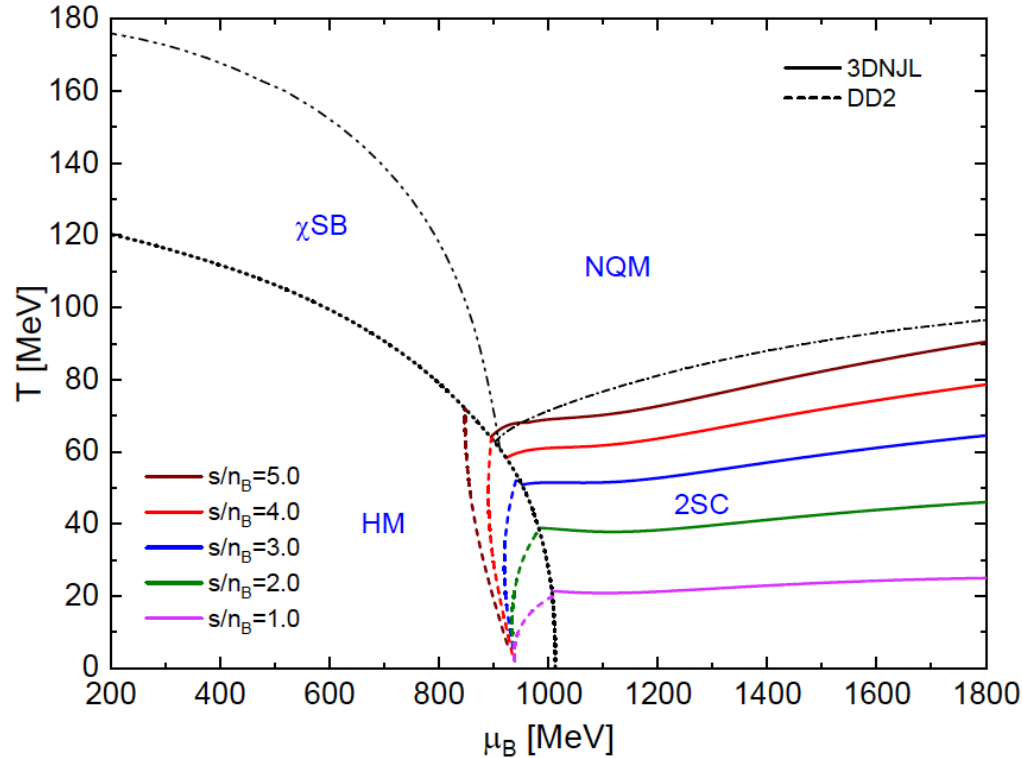


\*) G. Contrera, D.B., J.P. Carlomagno, A.G. Grunfeld, PRC 105 (2022) 045808  
J.P. Carlomagno, G. Contrera, A.G. Grunfeld, D.B., PRD 109 (2024) 043050; arXiv:2406.17193



# Thermal twin stars

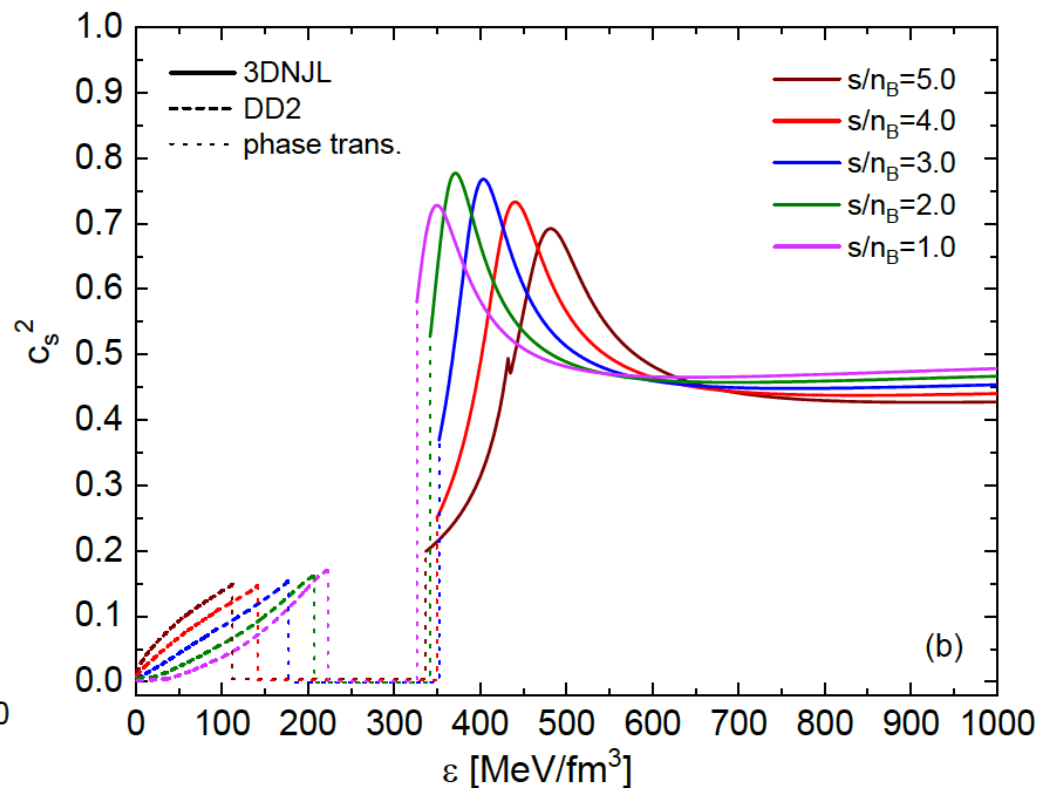
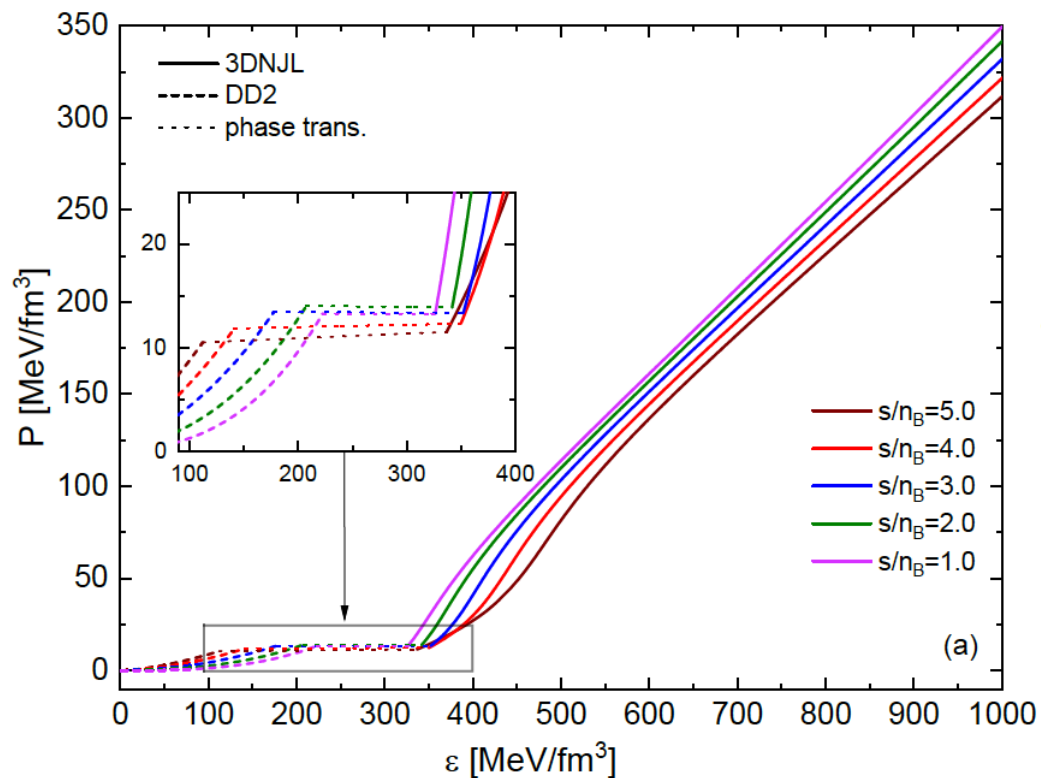
Investigation within a color superconducting, nonlocal chiral quark model\*:



\*) G. Contrera, D.B., J.P. Carlomagno, A.G. Grunfeld, PRC 105 (2022) 045808  
 J.P. Carlomagno, G. Contrera, A.G. Grunfeld, D.B., PRD 109 (2024) 043050; arXiv:2406.17193

# Thermal twin stars

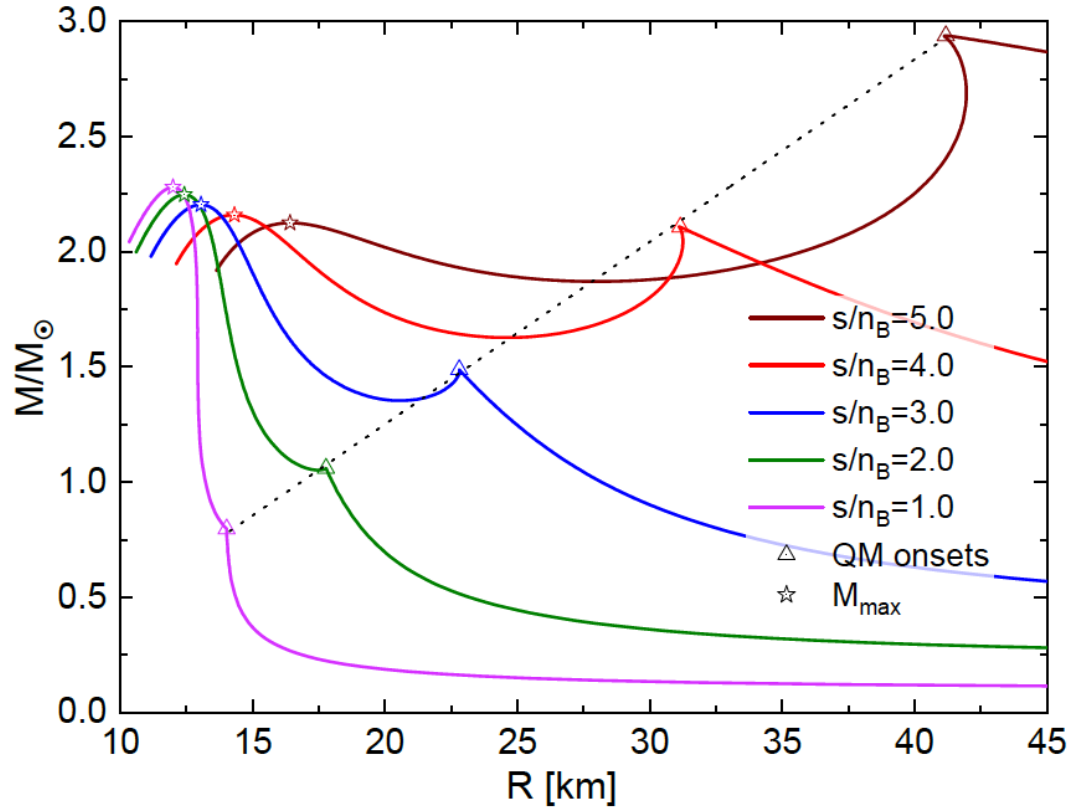
Investigation within a color superconducting, nonlocal chiral quark model\*:



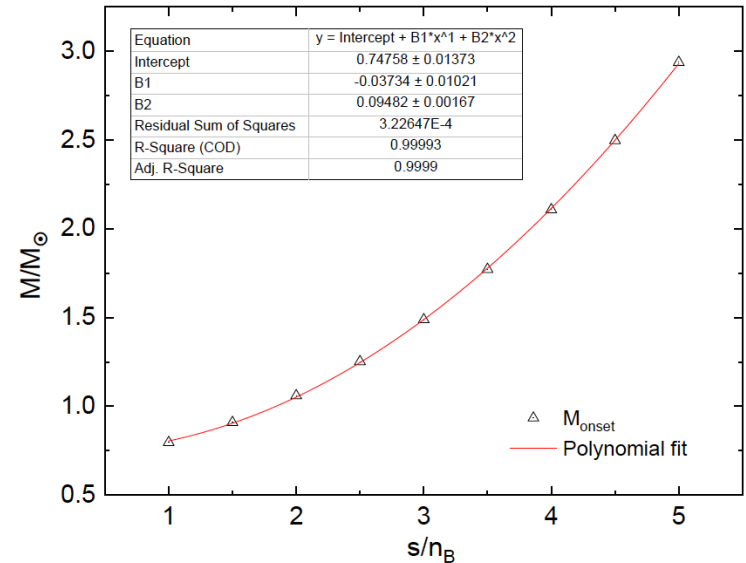
\*) G. Contrera, D.B., J.P. Carlomagno, A.G. Grunfeld, PRC 105 (2022) 045808  
J.P. Carlomagno, G. Contrera, A.G. Grunfeld, D.B., PRD 109 (2024) 043050; arXiv:2406.17193

# Thermal twin stars

Investigation within a color superconducting, nonlocal chiral quark model\*:



Systematics for the onset:  $M = C(R - R_0)$ ,  
 where  $R_0 = 4.20 \pm 0.35$  km is the radius offset  
 and  $C = dM_{\text{onset}}/dR = 0.0792 \pm 0.0009 M_{\odot}/\text{km}$   
 is the critical compactness of the star



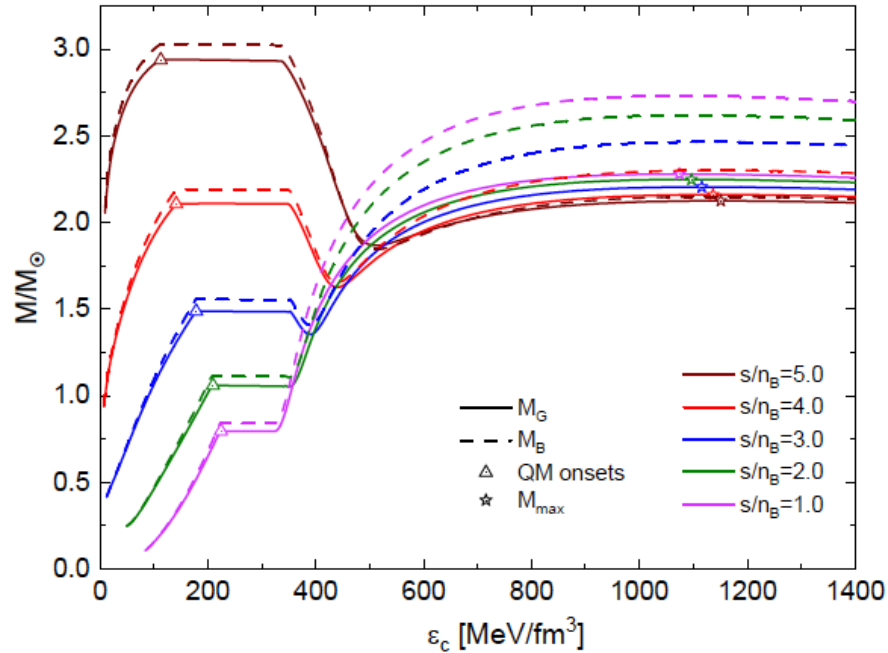
\*) G. Contrera, D.B., J.P. Carlomagno, A.G. Grunfeld, PRC 105 (2022) 045808  
 J.P. Carlomagno, G. Contrera, A.G. Grunfeld, D.B., PRD 109 (2024) 043050; arXiv:2406.17193

$$\frac{M_{\text{onset}}}{M_{\odot}} = 0.747 - 0.0373 \frac{s}{n_B} + 0.0948 \left( \frac{s}{n_B} \right)^2$$

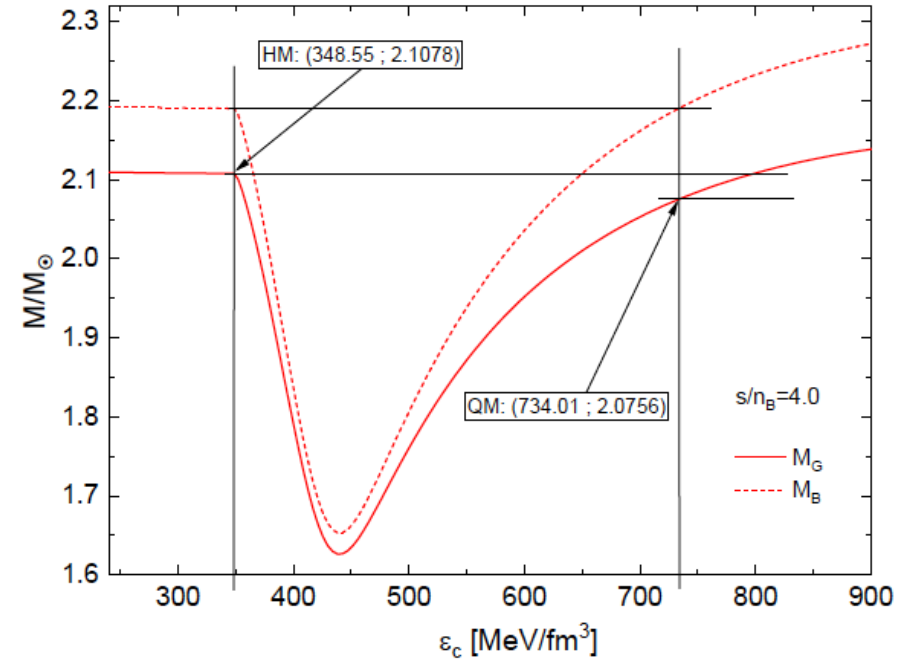
# Thermal twin stars

Investigation within a color superconducting, nonlocal chiral quark model\*:

Gravitational mass (solid) and baryon mass (dashed)



Extraction of the mass defect (energy release)

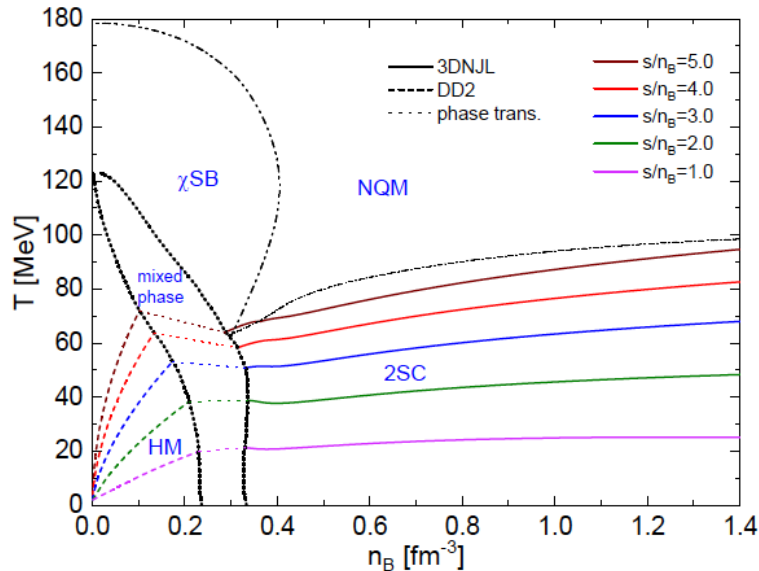


\*) G. Contrera, D.B., J.P. Carlomagno, A.G. Grunfeld, PRC 105 (2022) 045808  
J.P. Carlomagno, G. Contrera, A.G. Grunfeld, D.B., PRD 109 (2024) 043050; arXiv:2406.17193

# Thermal twin stars

Characterization of the accretion-induced transition to the thermal twin star\*

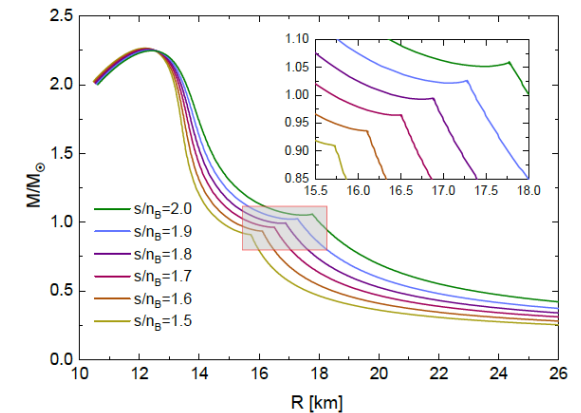
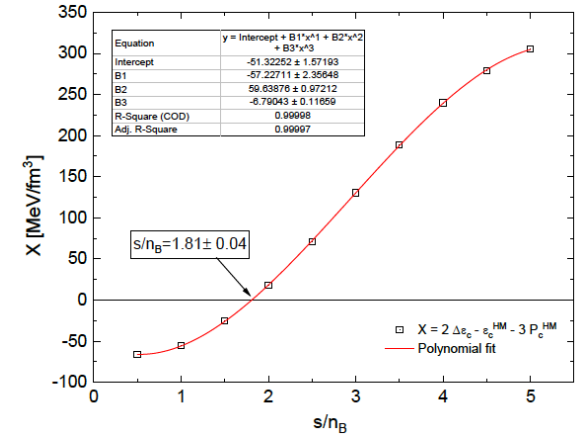
$s/n_B$	$M_{B,tr}$	$M_{G,HM}$	$M_{G,QM}$	$\Delta M$	$T(0)_{HM}$	$T(0)_{QM}$	$\Delta T(0)$	character
2.0	1.114	1.0582	1.0582	0.0000	38.36	38.87	0.51	enthalpic
2.5	1.311	1.2490	1.2487	0.0003	46.33	45.57	-0.76	entropic
3.0	1.557	1.4878	1.4853	0.0025	53.16	50.84	-2.32	entropic
3.5	1.849	1.7726	1.7621	0.0105	58.89	55.01	-3.88	entropic
4.0	2.190	2.1078	2.0756	0.0322	63.74	58.28	-5.46	entropic



\*) J.P. Carlomagno, G. Contrera, A.G. Grunfeld, D.B., arXiv:2406.17193

Seidov criterion for instability:

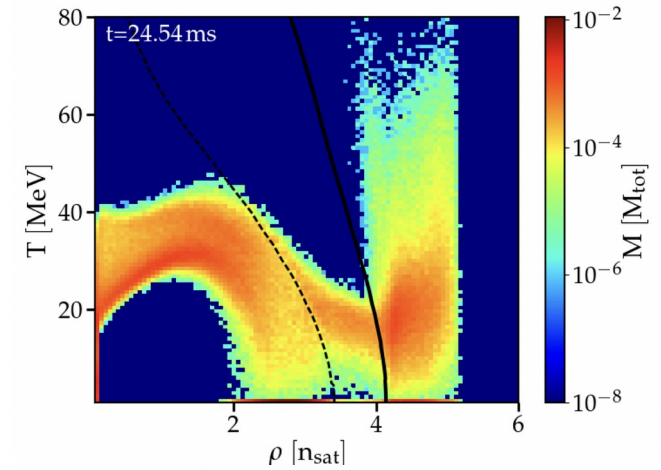
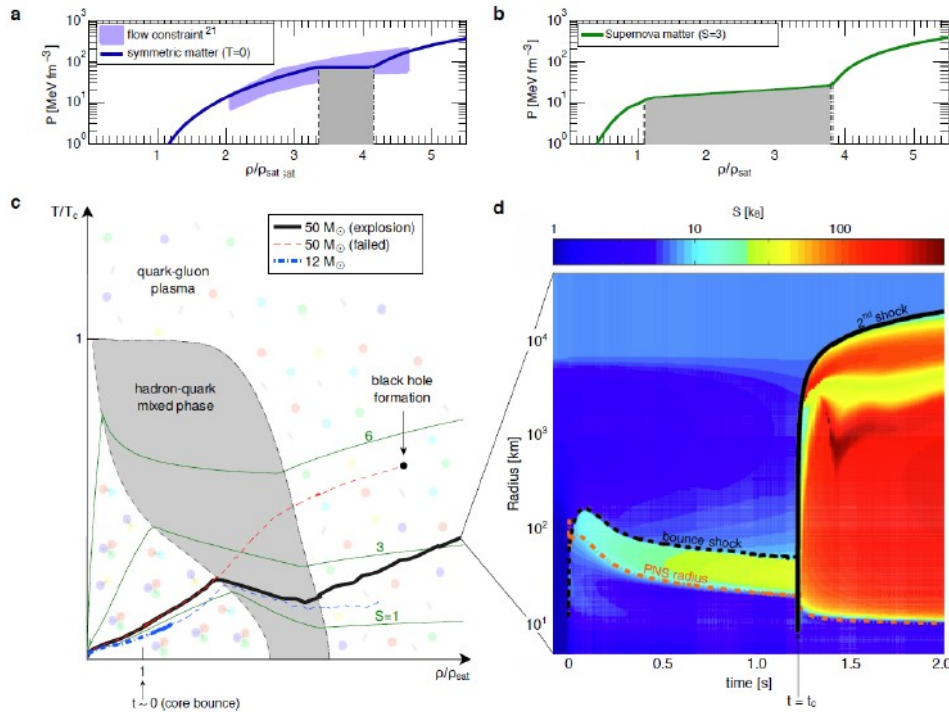
$$X = 2\Delta\epsilon - \epsilon_c^{HM} - 3P_c^{HM} > 0$$



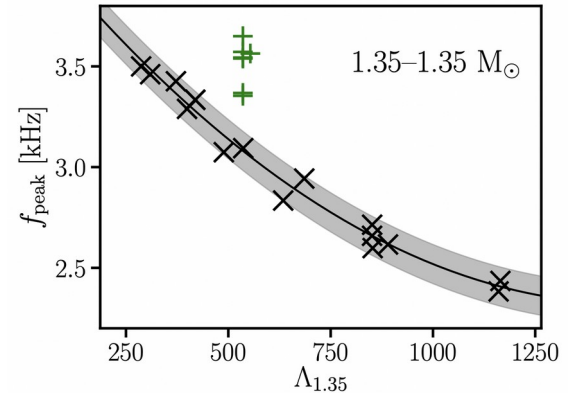


# Thermal twin stars – Indicators of CCSN explodability ?

Successful application of hybrid EoS with entropic first-order transition (thermal twin stars) as an explosion mechanism for massive blue supergiant stars\* and for a GW signal from binary neutron star mergers\*\*:



Progenitor:  
M = 50 M<sub>⊙</sub>



\*) T. Fischer et al., Nature Astron. (2018)

\*\*\*) A. Bauswein et al., PRL (2019)



