

Multimessenger signals from core collapse of massive stars

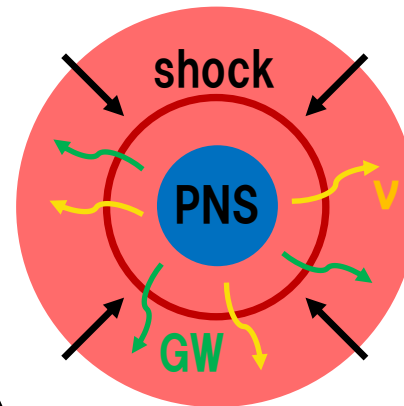
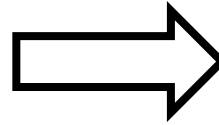
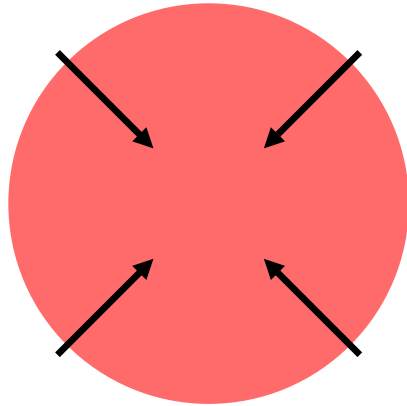
Shota Shibagaki (University of Wroclaw)

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Kei Kotake (Fukuoka U.)
Tomoya Takiwaki (NAOJ)
Tobias Fischer (UWr)**

Fate of massive stars

collapse of massive star

protoneutron star (PNS) formation

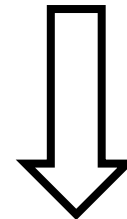


**ν / GW
emission**

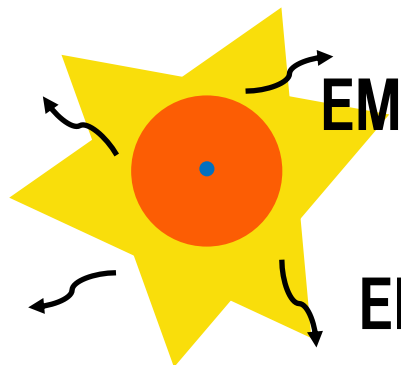
success



successful explosion

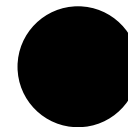


failed



EM emission

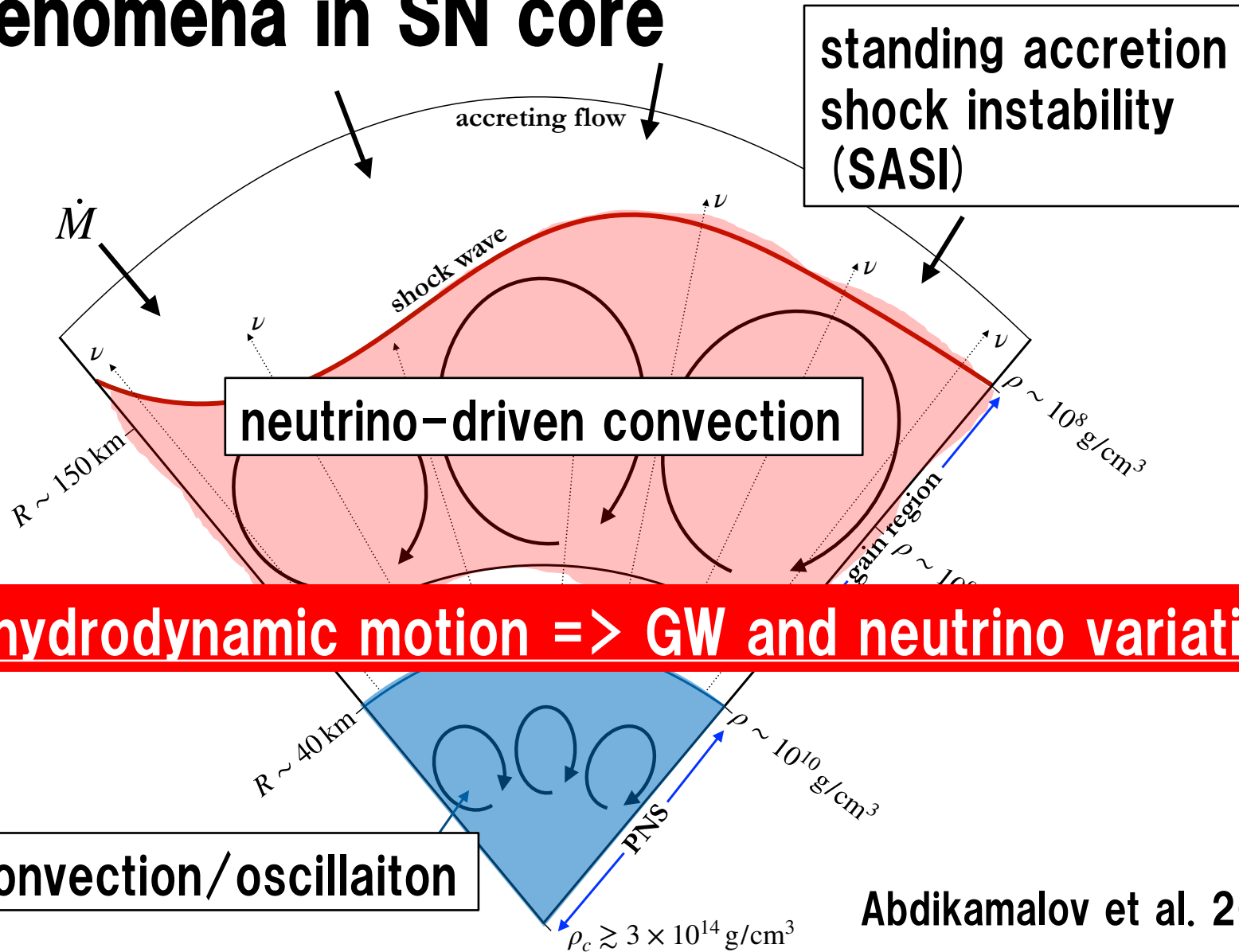
black hole (BH) formation



No/weak
EM emission

GW and neutrinos: Unique probes of supernovae core

Multidimensional hydrodynamic phenomena in SN core



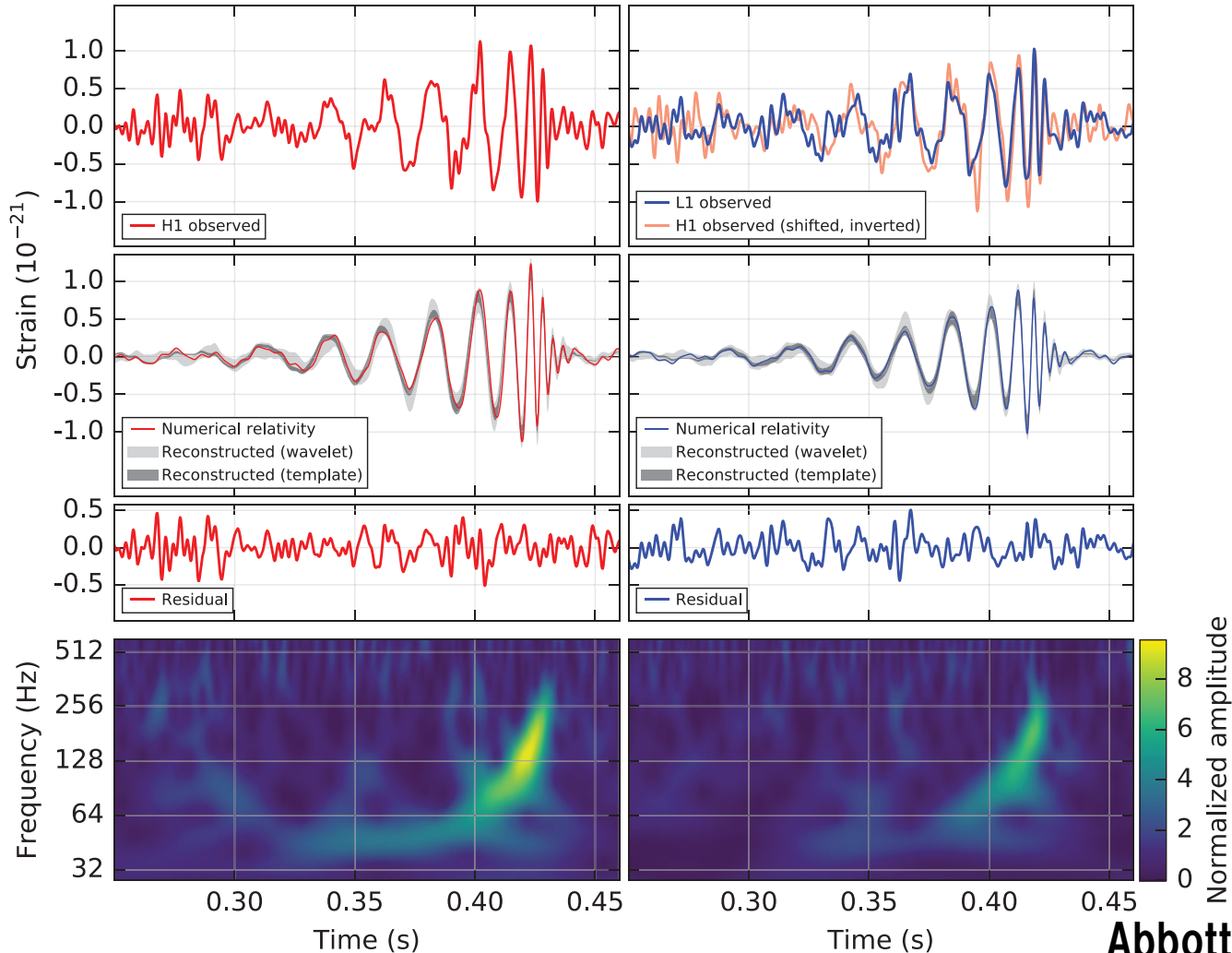
3D hydrodynamic motion => GW and neutrino variation

PNS convection/oscillation

Abdikamalov et al. 2020

Short-Term Fourier Transform

$$\tilde{S}(f, \tau) = \int_{-\infty}^{\infty} \underbrace{A(t)}_{\text{GW}} \underbrace{H(t - \tau)}_{\text{window function}} e^{-2\pi i f t} dt$$



Abbott et al. 2016

Multi-messengers from SNe: GW

- Imprints of standing accretion shock instability (SASI) & g-mode of protoneutron star may be found in observed GW.

ex.) Kuroda et al. 2017

Andresen et al. 2017, 2019

O' Connor et al. 2018

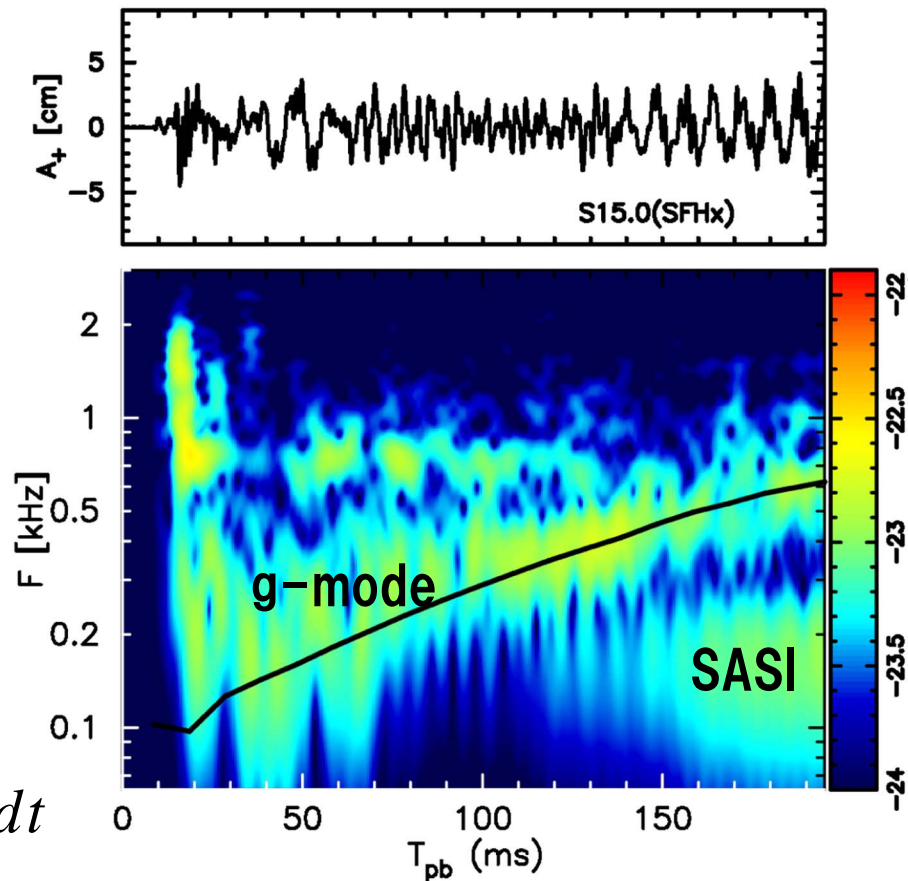
Vartanyan et al. 2019

Powell & Muller 2020

Mezzacappa et al. 2020

Short term Fourier trans.

$$\tilde{S}(f, \tau) = \int_{-\infty}^{\infty} \underbrace{A(t)}_{\text{GW}} \underbrace{H(t - \tau)}_{\text{window function}} e^{-2\pi i f t} dt$$



Kuroda et al. 2017

Multi-messengers from SNe: ν

- Imprints of standing accretion shock instability (SASI) may be found in observed neutrinos.

ex.) Tamborra et al. 2014

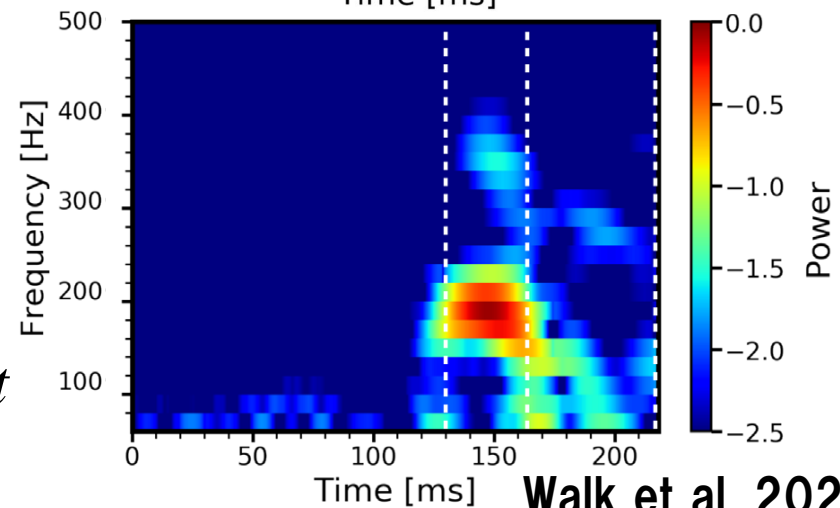
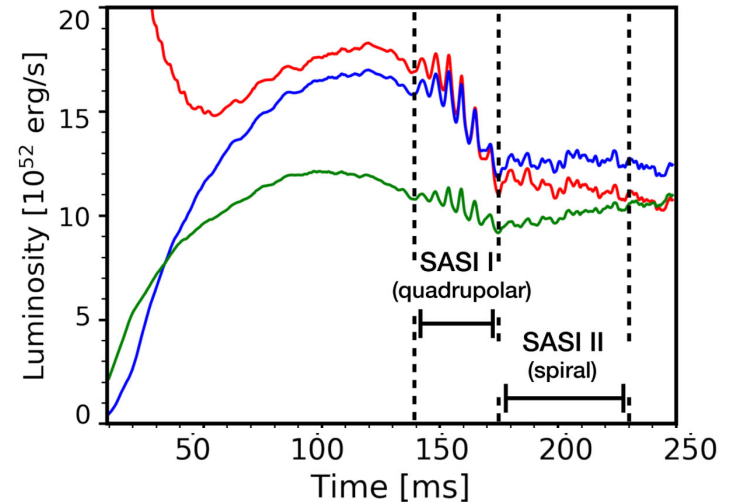
Kuroda et al. 2017

O' Connor et al. 2018

Walk et al. 2018, 2020

Vartanyan et al. 2019

Nagakura et al. 2020

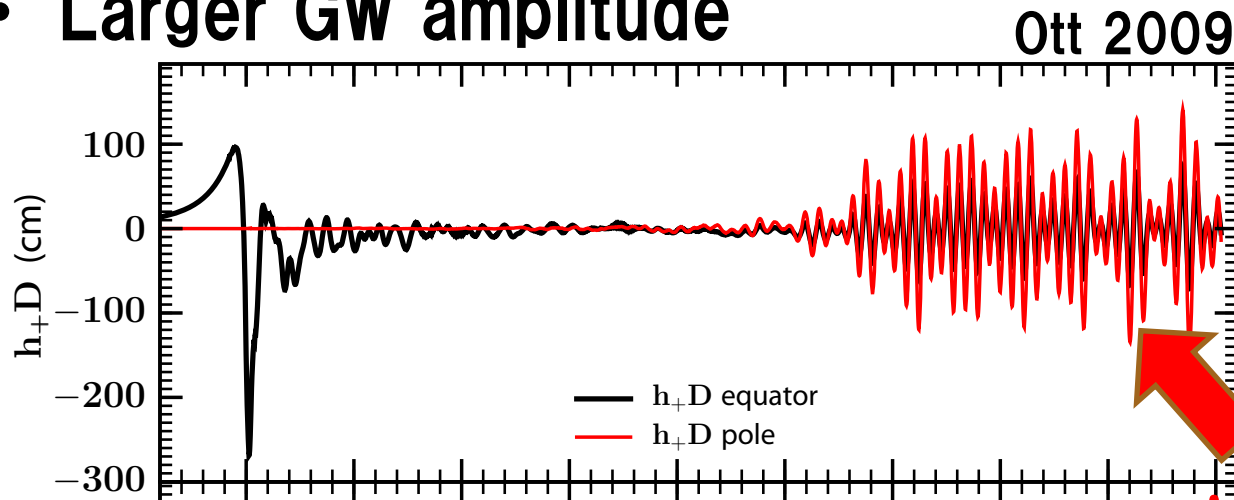


Short term Fourier trans.

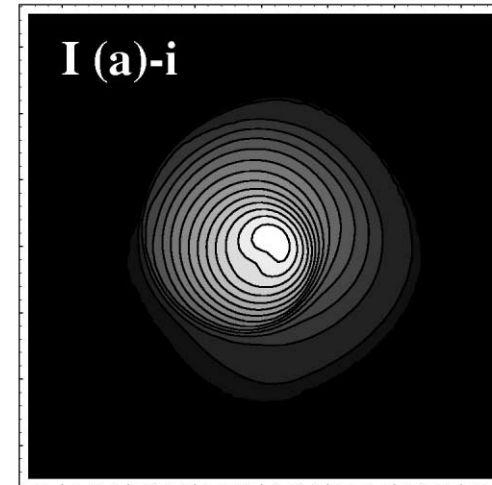
$$\tilde{S}(f, \tau) = \int_{-\infty}^{\infty} \underbrace{A(t)}_{\nu} \underbrace{H(t - \tau)}_{\text{window function}} e^{-2\pi i f t} dt$$

Rapidly rotating cases

- Larger GW amplitude



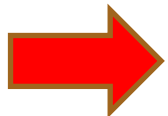
Saijo et al. 2003



Previous 3D simulations:

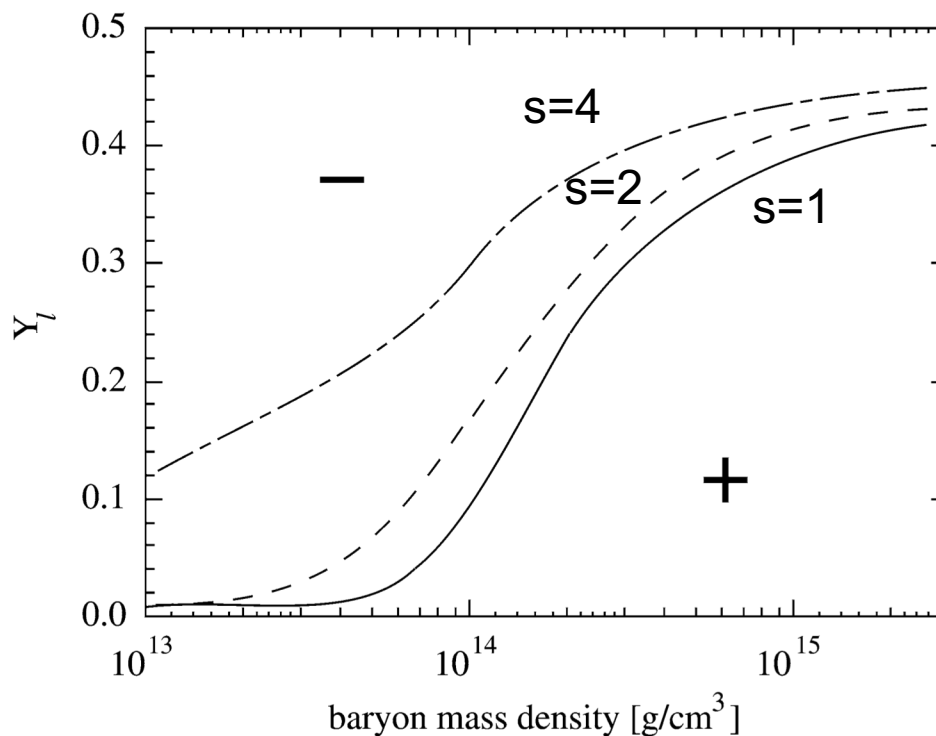
- Ott et al. 2005 Newtonian + no neutrino
- Ott et al. 2007 full GR + Ye prescription
- Scheidegger et al. 2008, 2010 effective GR + leakage
- Takiwaki et al. 2016, 2018 Newtonian + IDSA

**non-axisymmetric instability
(low- $T/|W|$ instability)**



Full GR v radiation-hydrodynamics simulations

PNS Convection



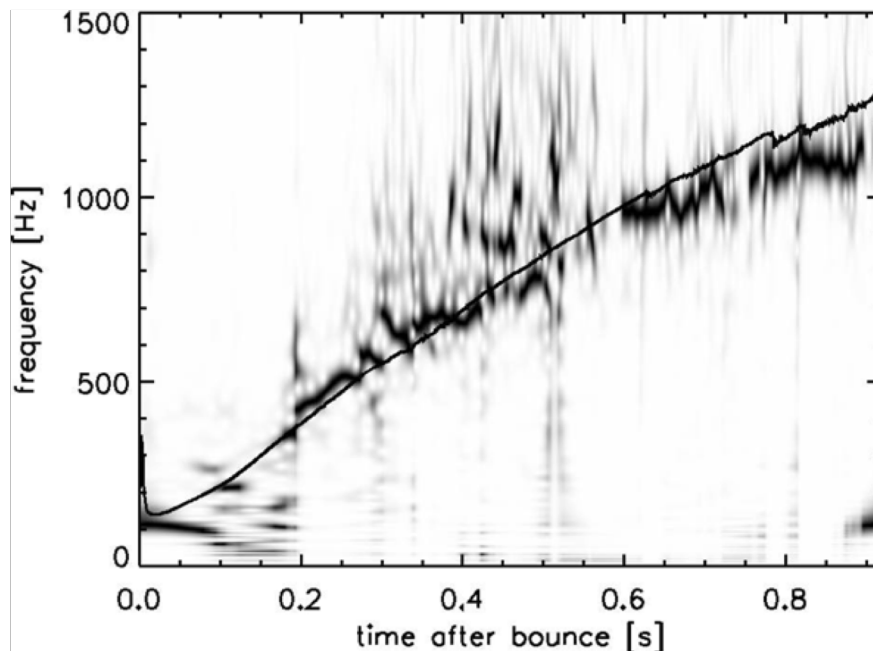
The Ledoux criterion depends on the property of EOS:

$$\left(\frac{\partial \rho}{\partial Y_l} \right)_{P,S} \left(\frac{dY_l}{dr} \right) + \left(\frac{\partial \rho}{\partial S} \right)_{P,Y_l} \left(\frac{dS}{dr} \right) \geq 0$$

stable against convection

Sumiyoshi et al. 2004

GW from PNS Oscillation



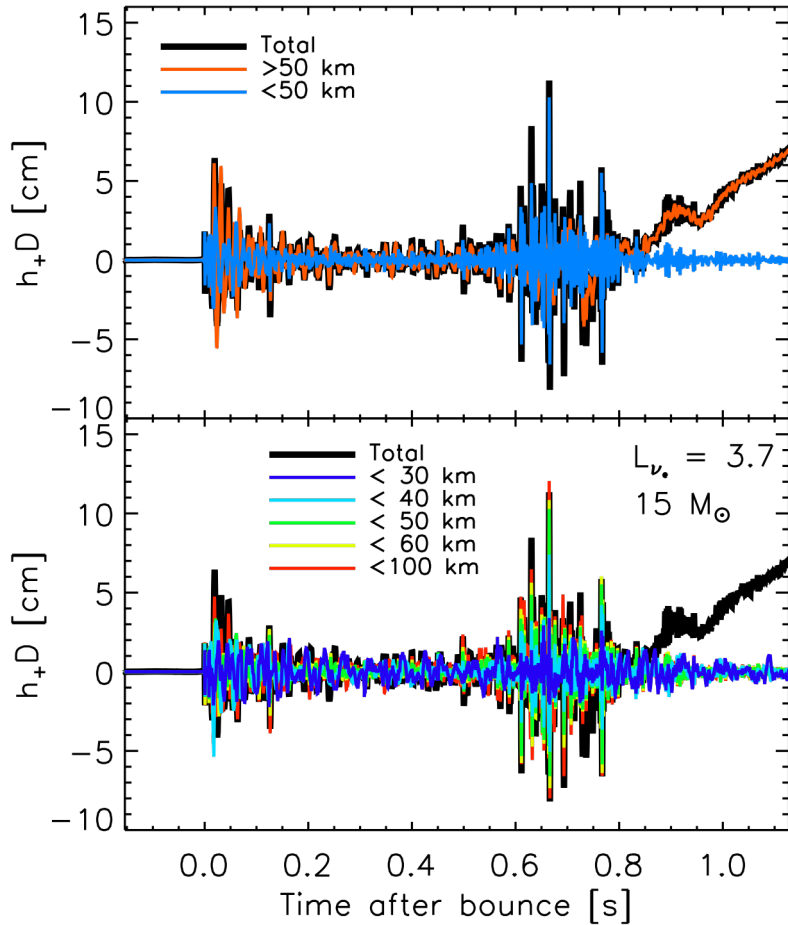
$$f_p = \frac{N}{2\pi} \approx \frac{1}{2\pi} \frac{GM}{R^2} \sqrt{1.1 \frac{m_n}{\langle E_{\bar{\nu}_e} \rangle}} \left(1 - \frac{GM}{Rc^2}\right)^2$$

$$N^2 = \frac{\alpha C_L}{\rho h \phi^4} \frac{\partial \alpha}{\partial r} \quad C_L = \frac{\partial \rho(1 + \epsilon)}{\partial r} - \left(\frac{d\rho(1 + \epsilon)}{dP} \right)_{s, Y_e = \text{const.}} \frac{\partial P}{\partial r}$$

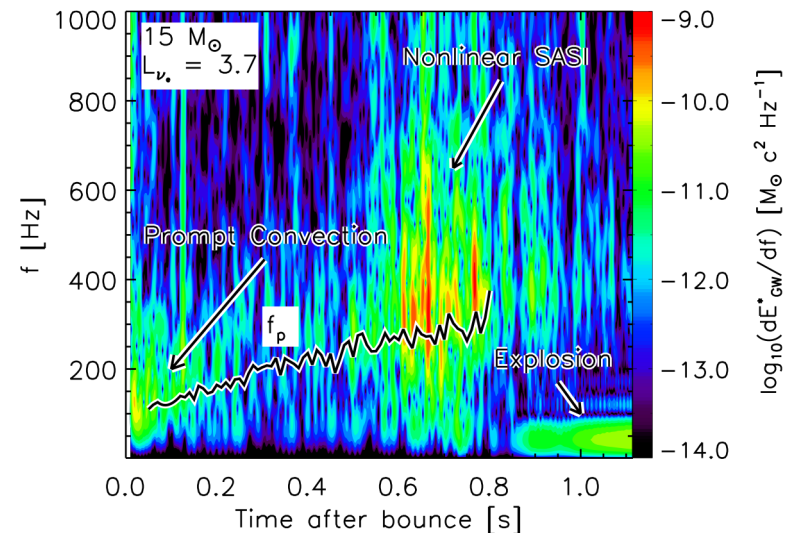
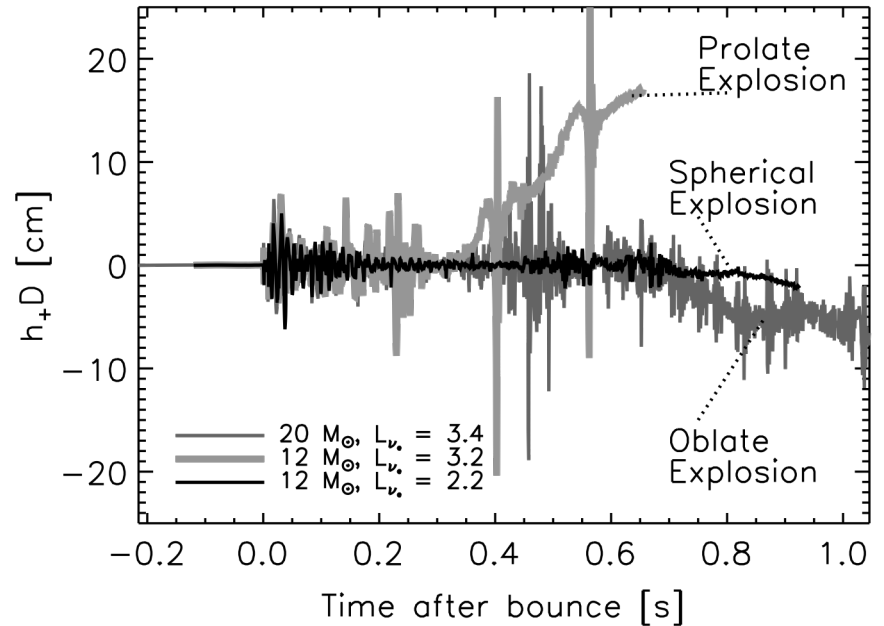
Brunt-Vaisala frequency

Muller et al. 2013

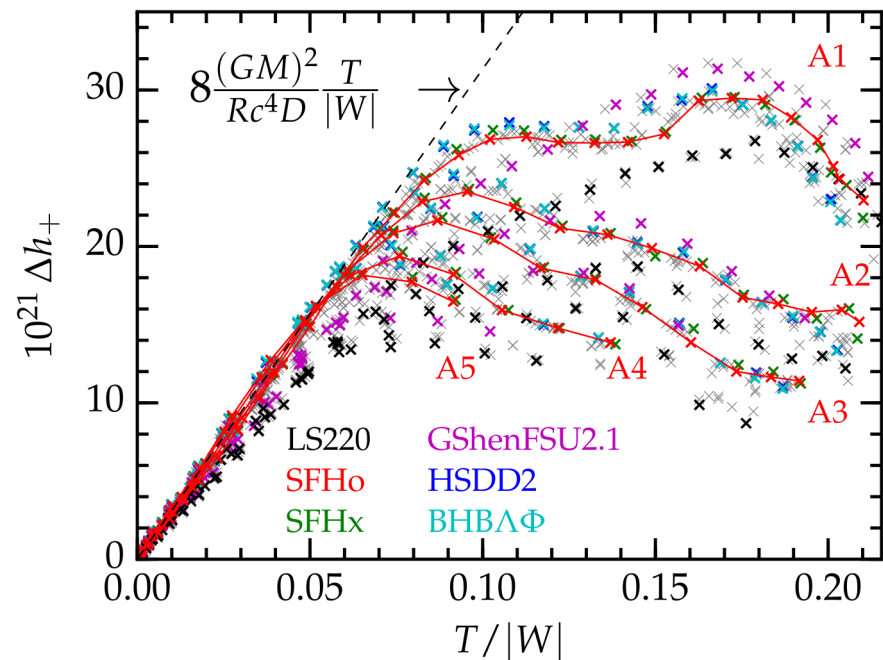
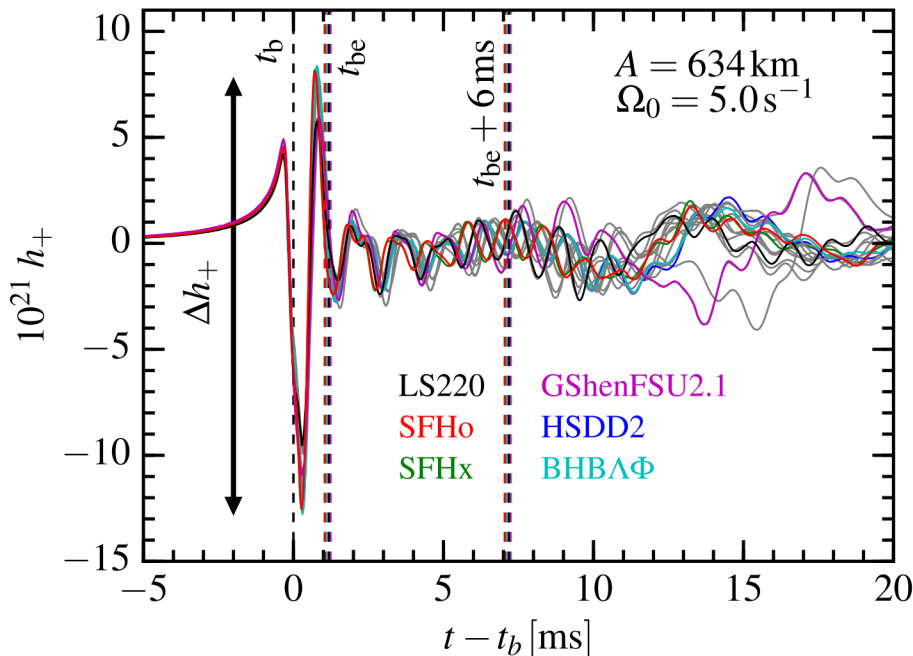
GW from Aspherical Explosion



Murphy et al. 2009



Effect of EOS on GW (rot. case)

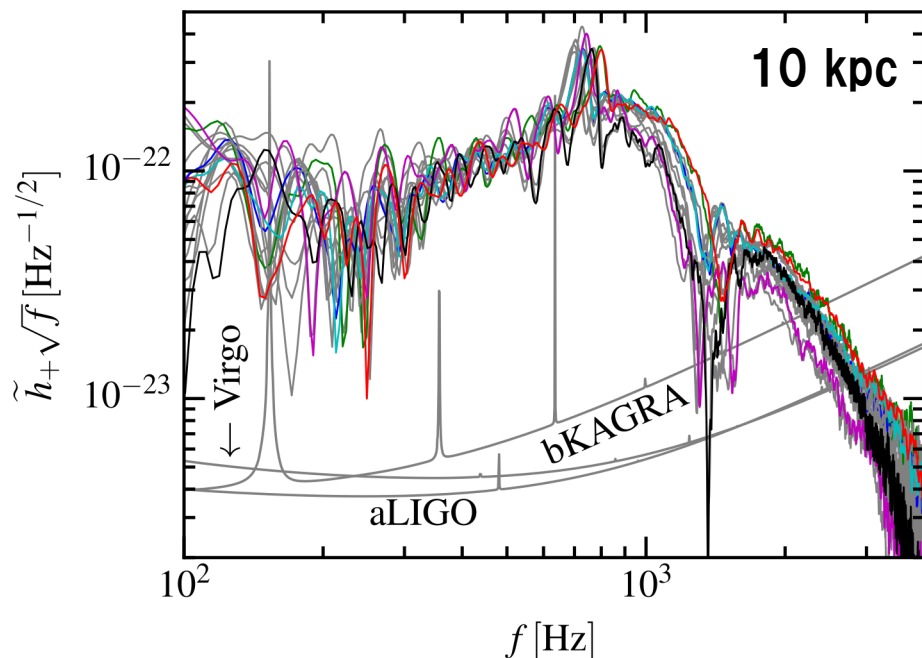
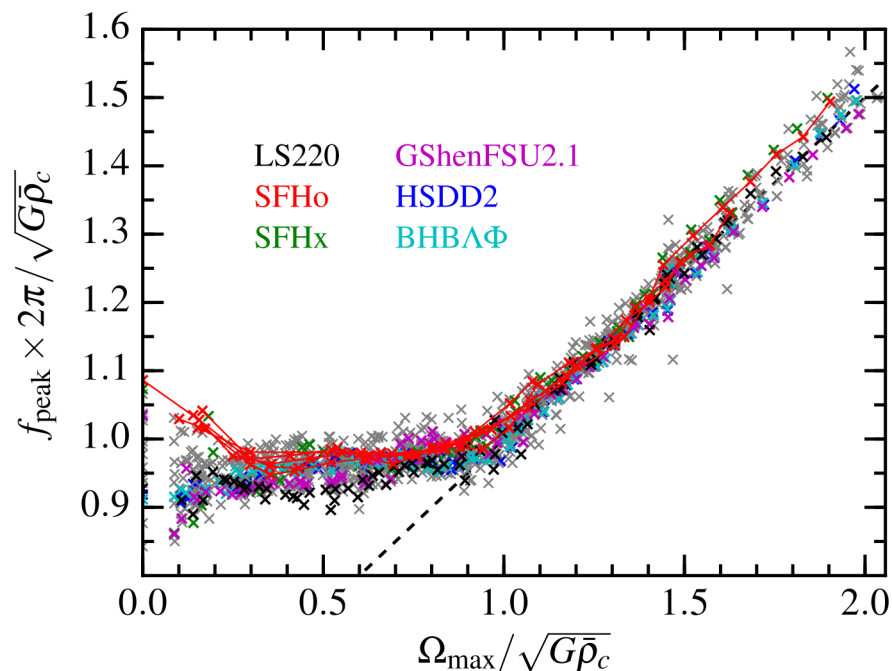


Systematic 2D simulations (1824 models) revealed the two universal relationships.

$$h_+ \sim \frac{GM\Omega^2 R^2}{c^4 D} \sim \frac{T}{|W|} \frac{(GM)^2}{Rc^4 D}$$

Abdikamalov et al. 2014, Richers et al. 2017

Effect of EOS on GW (rot. case)



Systematic 2D simulations (1824 models) revealed the two universal relationships.

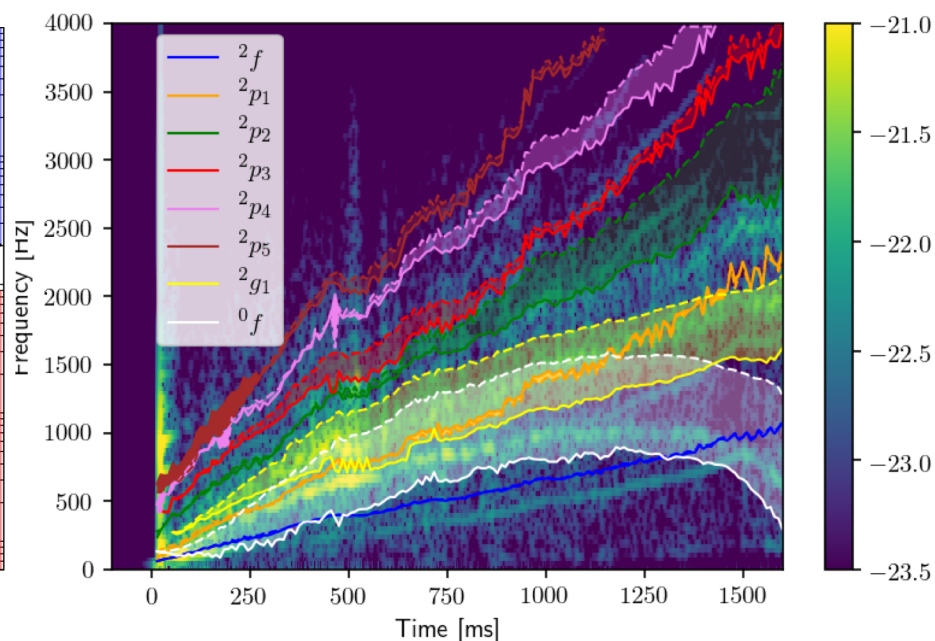
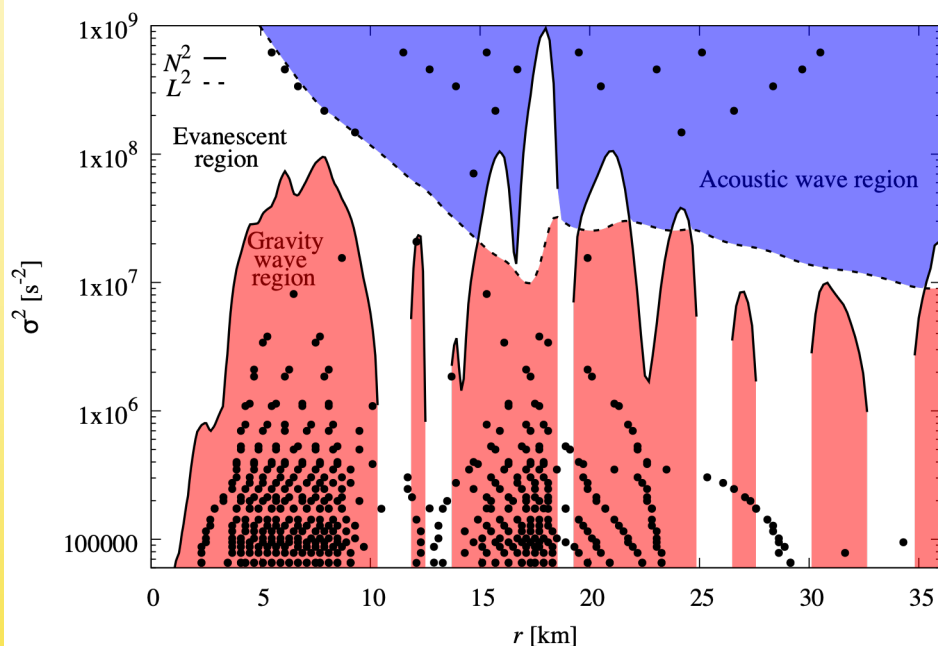
$$2\pi f_{\text{peak}} / \sqrt{G\bar{\rho}_c} = 0.5(1 + \Omega_{\text{max}} / \sqrt{G\bar{\rho}_c})$$

Abdikamalov et al. 2014, Richers et al. 2017

Mode analysis

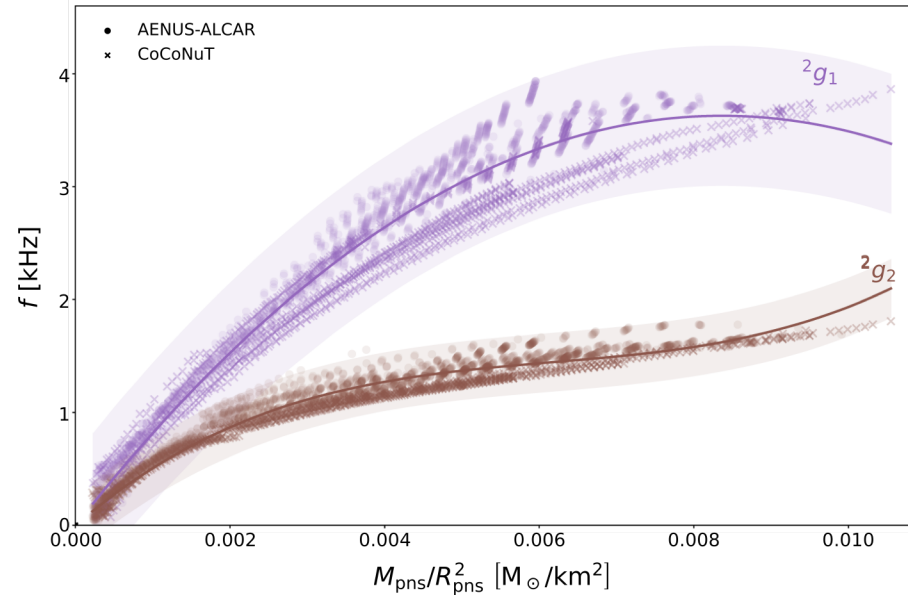
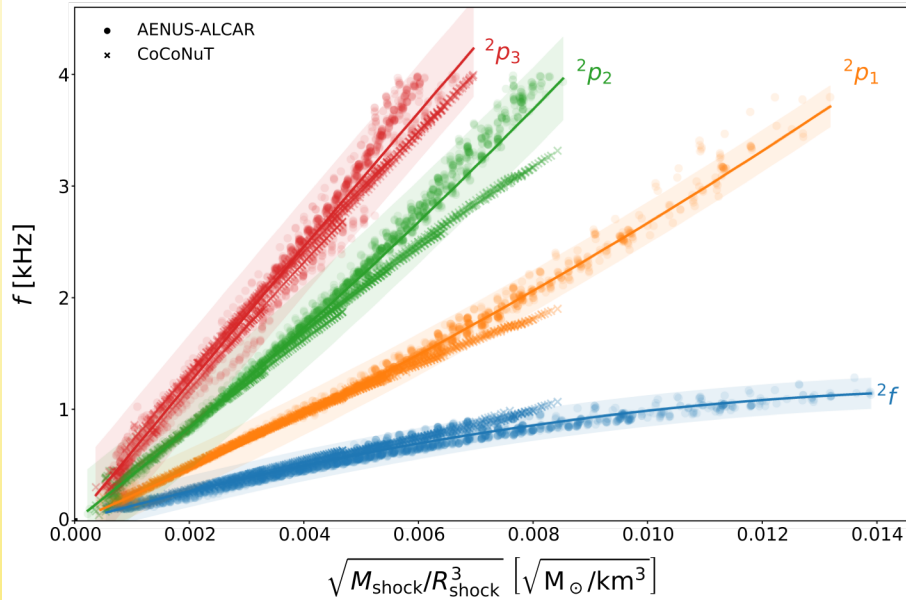
$$\mathcal{L}^2 \equiv \frac{\alpha^2}{\psi^4} c_s^2 \frac{l(l+1)}{r^2} \quad \text{Lamb freq.}$$

$$\mathcal{N}^2 \equiv \frac{\alpha^2}{\psi^4} \mathcal{G}^i \mathcal{B}_i \quad \text{Brunt-Vaisala freq.}$$

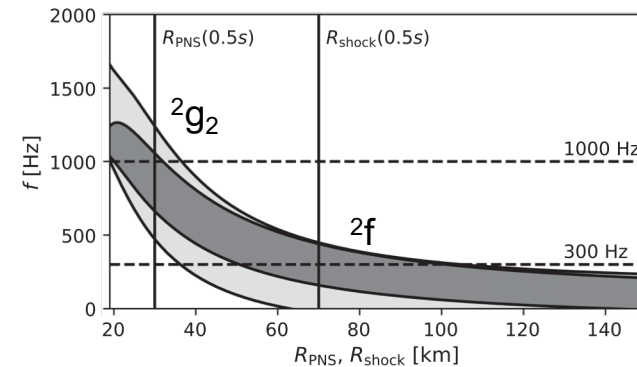


Torres-Forne et al. 2018, 2019a, 2019b

Universal Relation



Mode	x	a	$b/10^5$	$c/10^6$	$d/10^9$	R^2	σ
$2f$	$\sqrt{M_{\text{shock}}/R_{\text{shock}}^3}$...	1.410 ± 0.004	-4.23 ± 0.06	...	0.966	45
$2p_1$	$\sqrt{M_{\text{shock}}/R_{\text{shock}}^3}$...	2.205 ± 0.007	4.63 ± 0.09	...	0.991	61
$2p_2$	$\sqrt{M_{\text{shock}}/R_{\text{shock}}^3}$...	4.02 ± 0.02	7.4 ± 0.3	...	0.983	123
$2p_3$	$\sqrt{M_{\text{shock}}/R_{\text{shock}}^3}$...	6.21 ± 0.03	-1.9 ± 0.6	...	0.979	142
$2g_1$	$M_{\text{PNS}}/R_{\text{PNS}}^2$...	8.67 ± 0.03	-51.9 ± 0.5	...	0.958	205
$2g_2$	$M_{\text{PNS}}/R_{\text{PNS}}^2$...	5.88 ± 0.03	-86.2 ± 1.0	4.67 ± 0.08	0.956	85
$2g_3$	$\sqrt{M_{\text{shock}}/R_{\text{shock}}^3} \rho_c / \rho_c^{2.5}$	905 ± 3	-79.9 ± 1.7	-11000 ± 2000	...	0.925	41

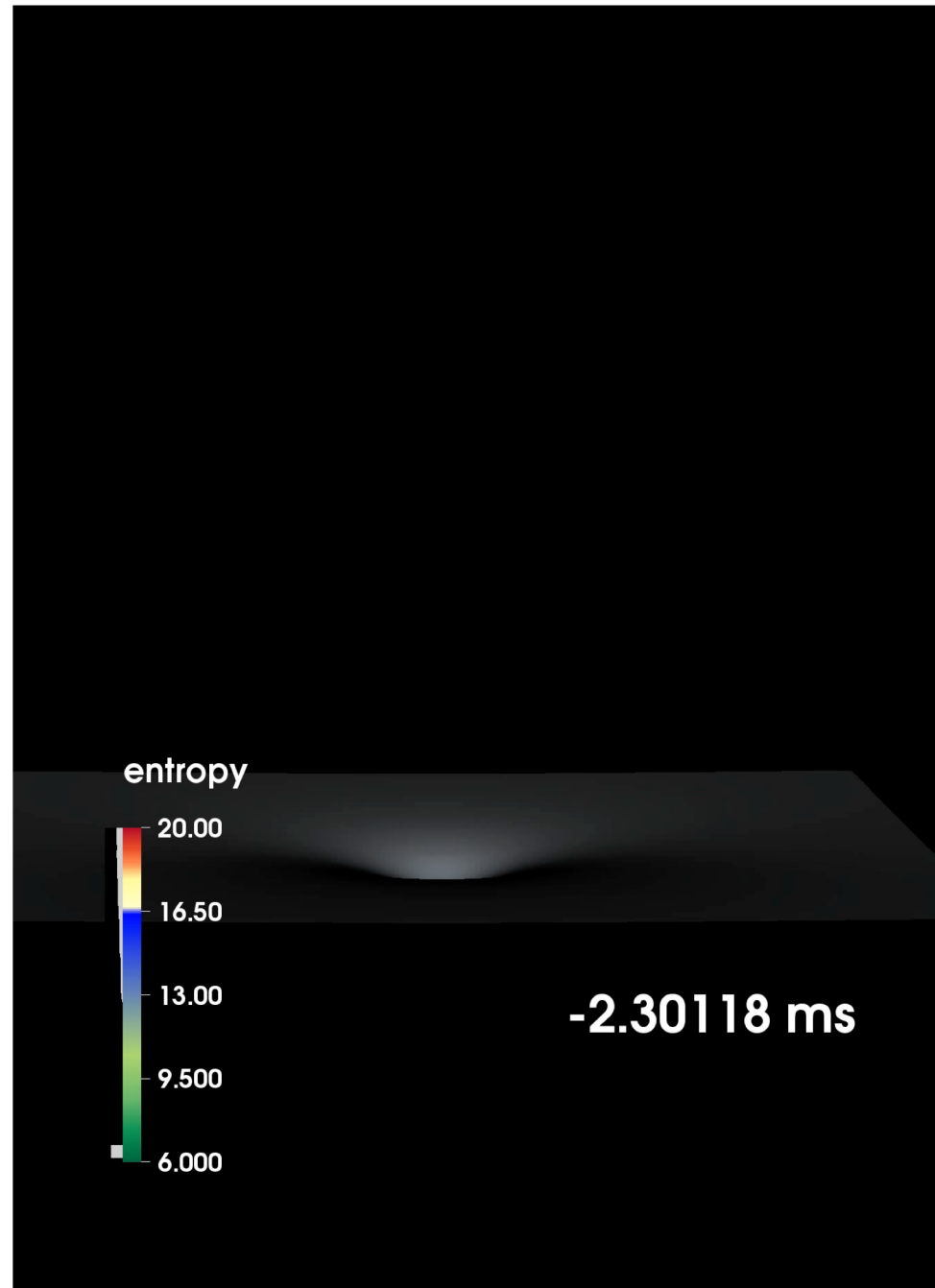
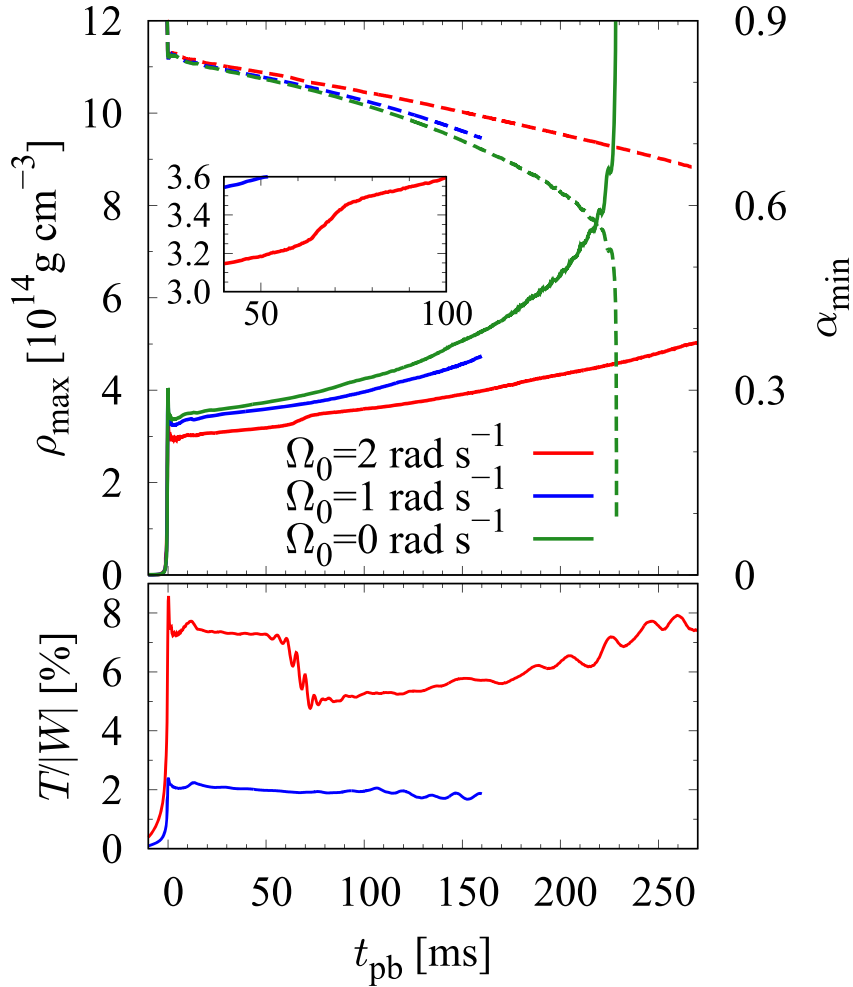


Torres-Forne et al. 2018, 2019a, 2019b

Method

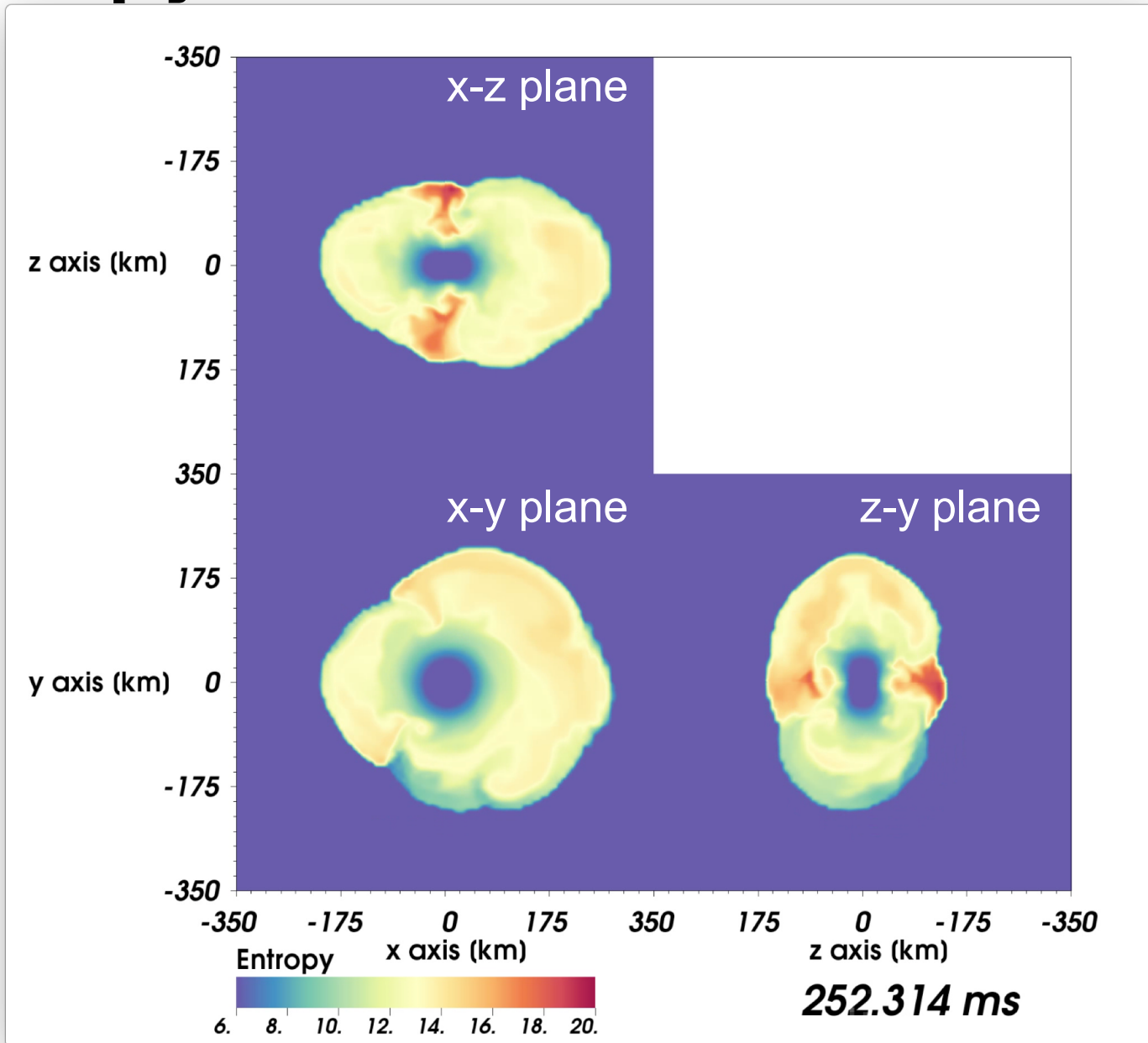
- Fully general relativistic neutrino radiation hydrodynamics code (Kuroda et al. 2016)
 - BSSN formalism for general relativity
 - Multi-energy neutrino transport with M1 scheme
 - Lattimer & Swesty EOS ($K = 220$ MeV)
 - $70 M_{\text{sun}}$ zero-metallicity star (Takahashi et al. 2014)
 - initial central rotation rate: $\Omega_0 = \underline{2.1}, 0$ rad/sec
c.f.) non rot. sim. showed BH formation at $t_{\text{pb}} \sim 230$ ms

$\Omega_0=0$ rad/sec model



Entropy Evolution

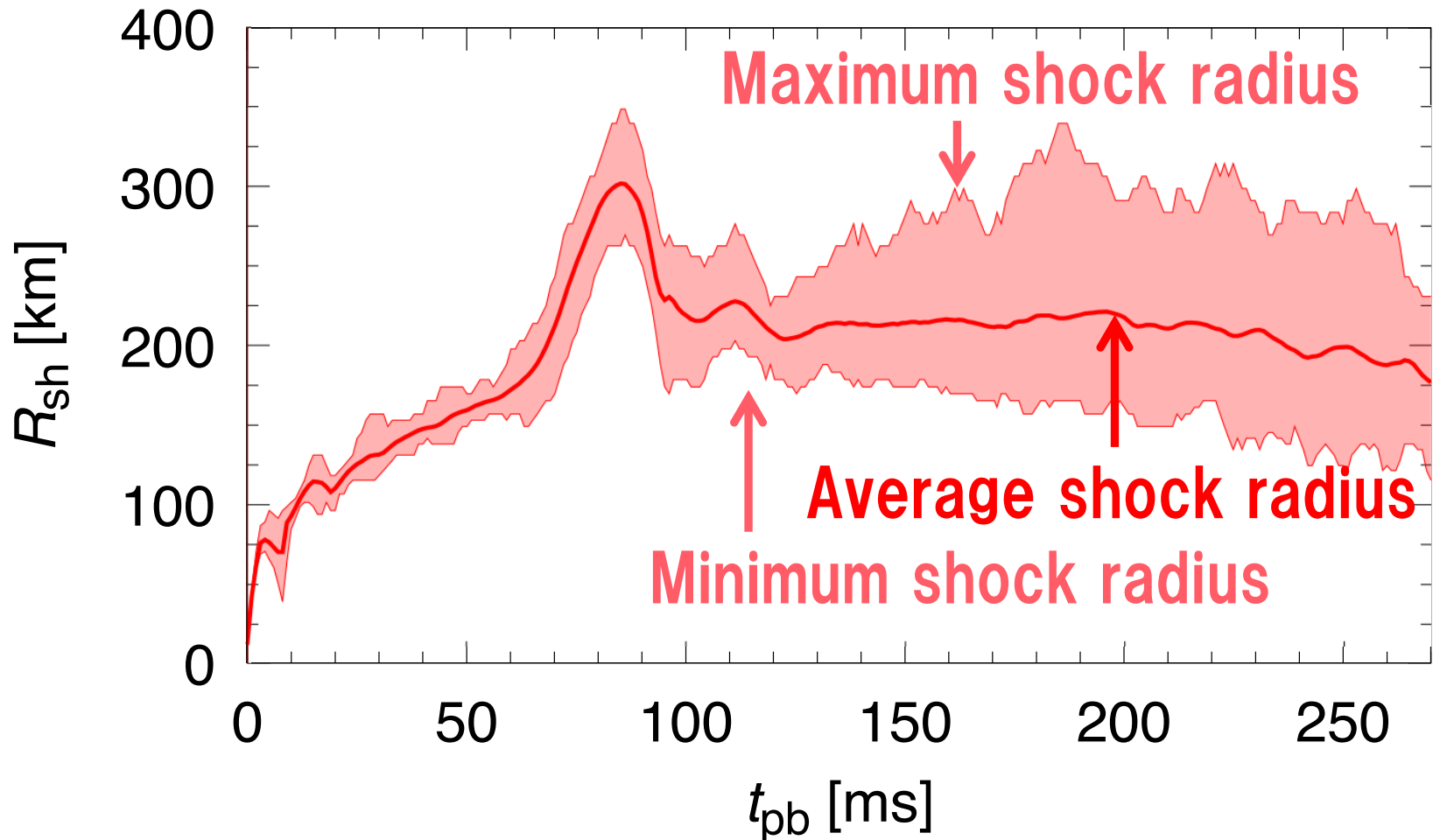
$$\Omega_0 = 2 \text{ rad/sec}$$



Shock Radius

$$\Omega_0 = 2 \text{ rad/sec}$$

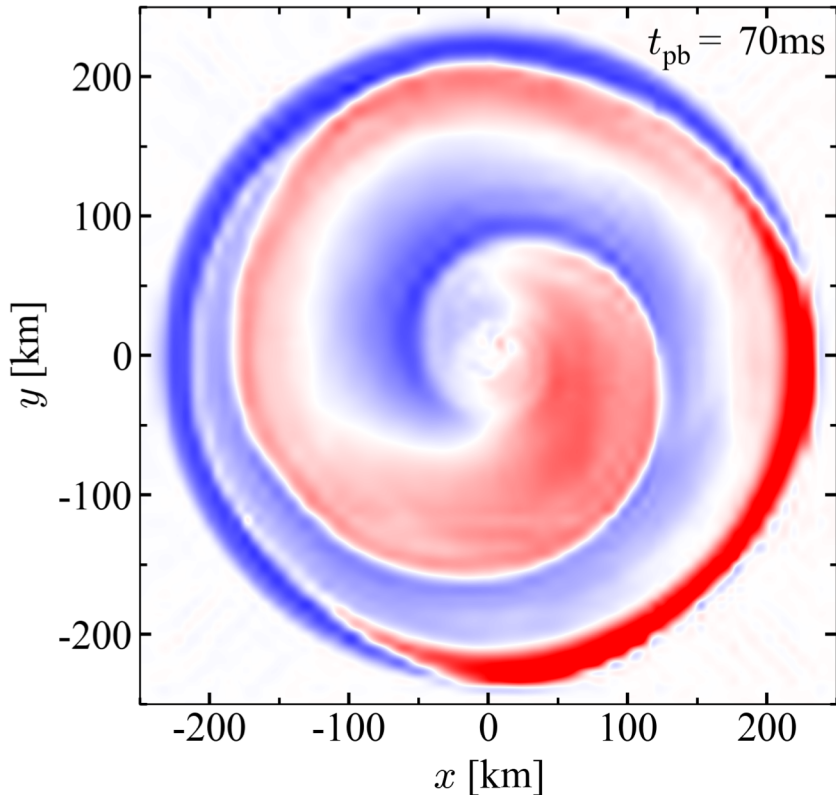
What is happening?



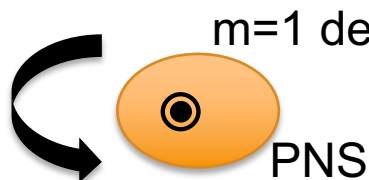
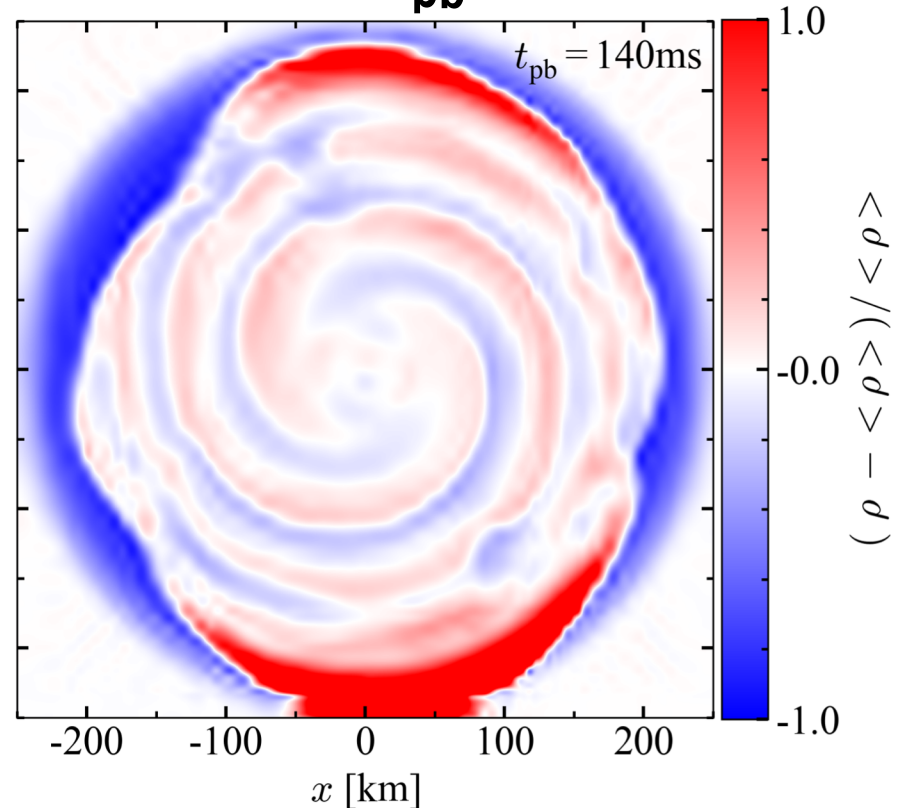
$$\Omega_0 = 2 \text{ rad/sec}$$

Density Distribution

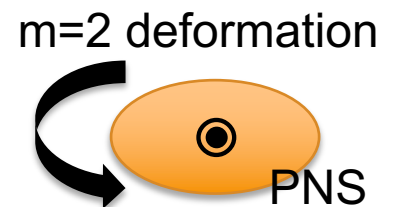
one arm ($t_{pb} = 70 \text{ms}$)



two arms ($t_{pb} = 140 \text{ms}$)



low T/|W| instability

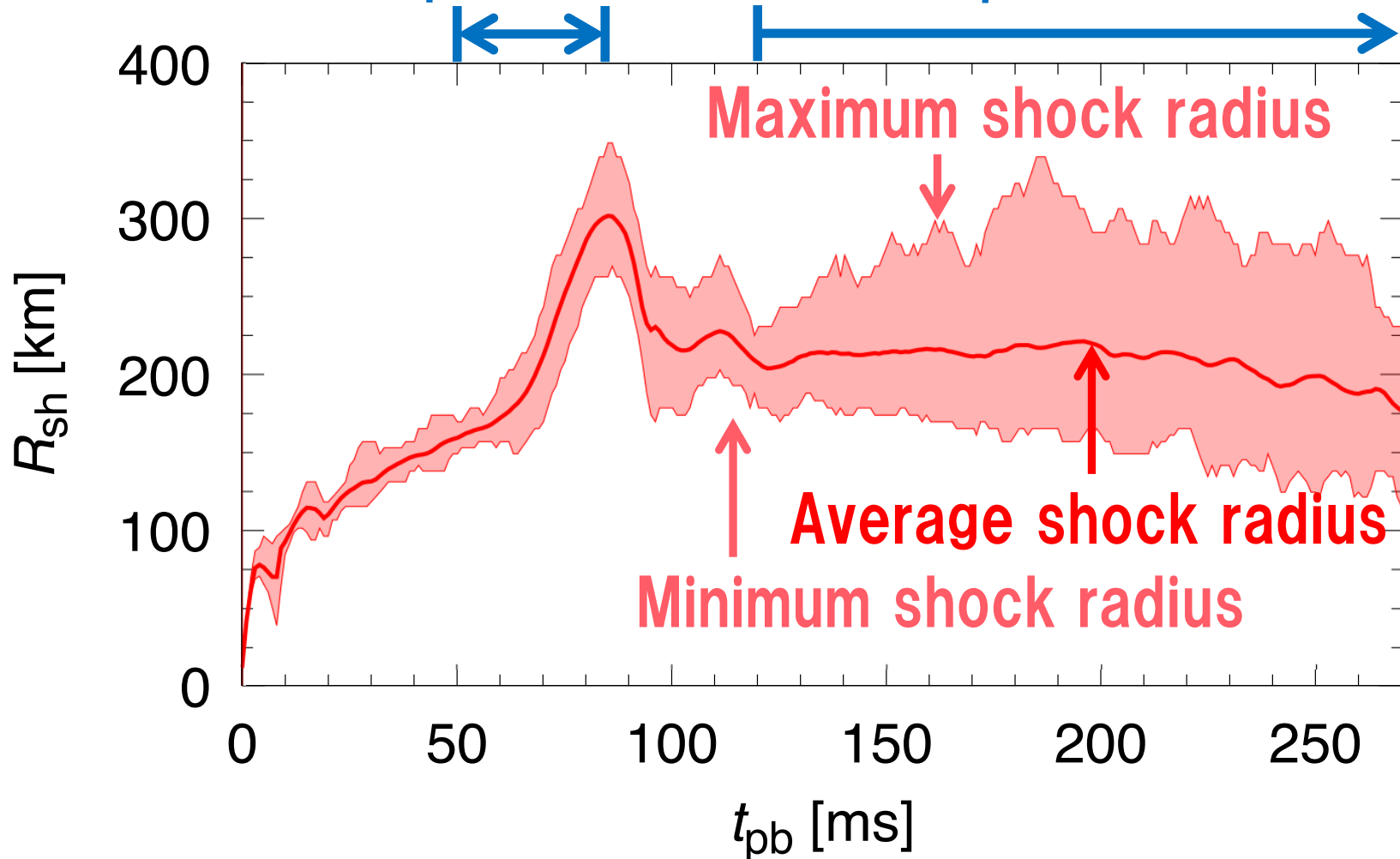


Shock Radius

$$\Omega_0 = 2 \text{ rad/sec}$$

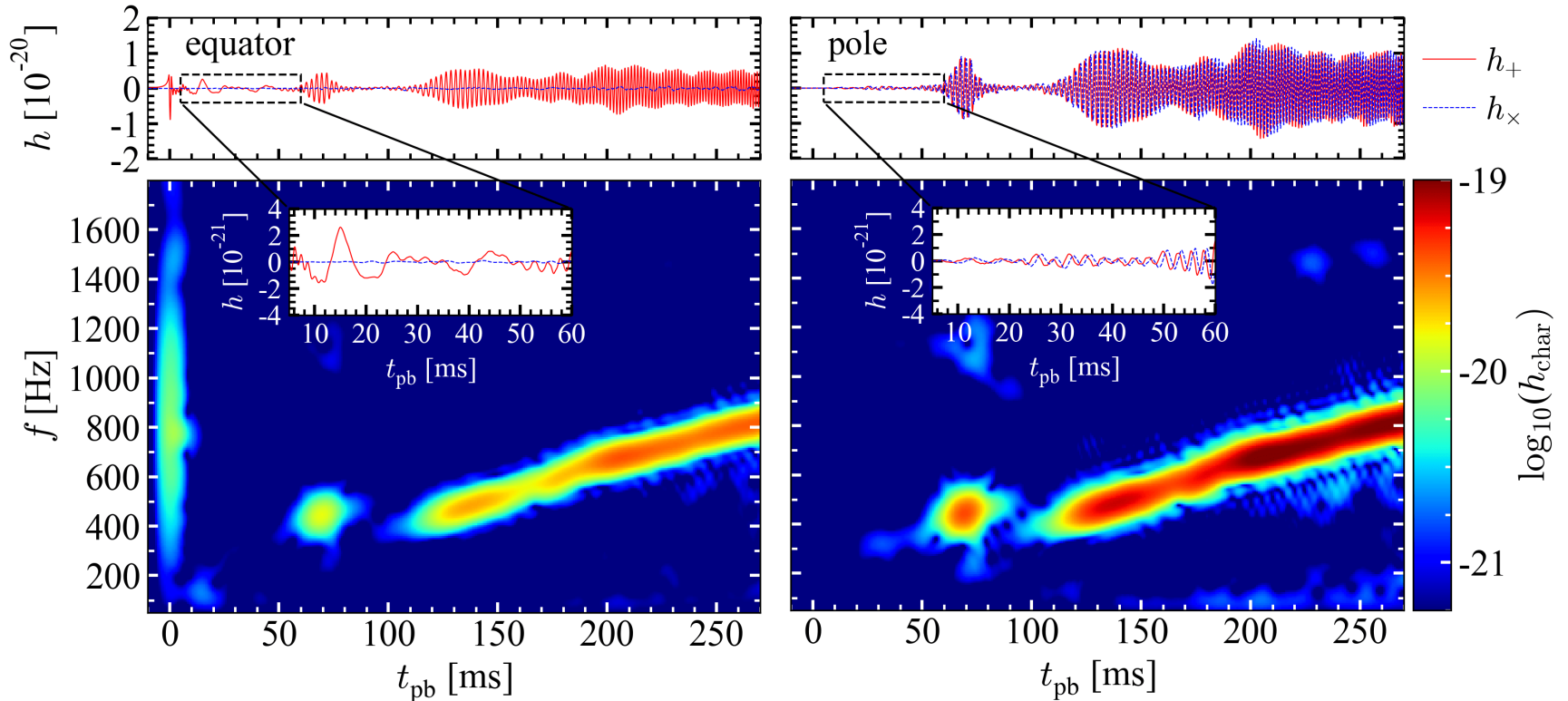
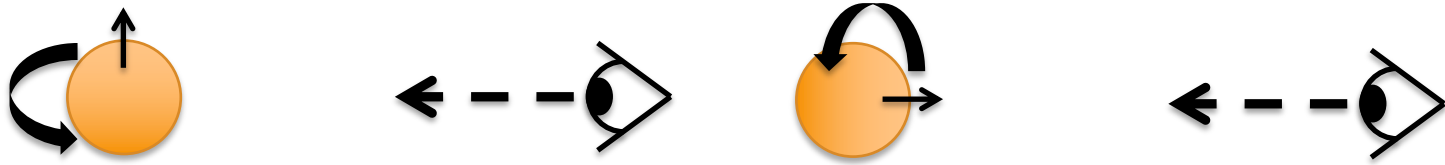
development of
one-armed
spiral wave

development of
two-armed
spiral wave



GW Spectrogram

$\Omega_0 = 2 \text{ rad/sec}$

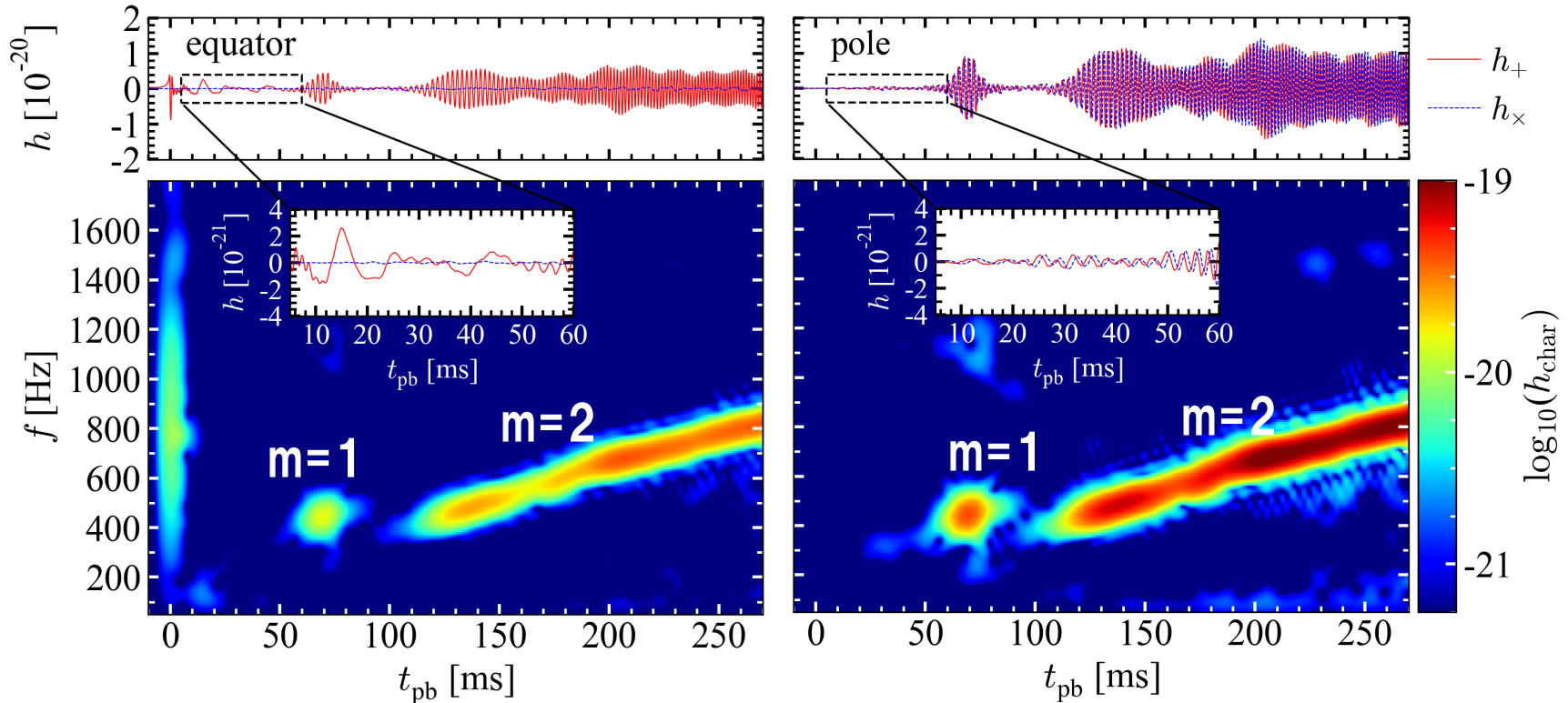
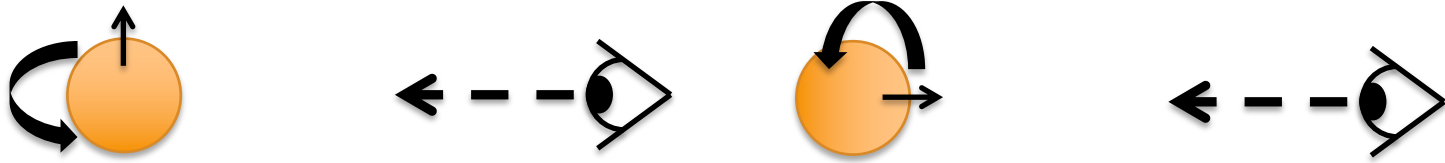


Short term Fourier trans.

$$\tilde{S}(f, \tau) = \int_{-\infty}^{\infty} \underbrace{A(t)}_{\text{GW}} \underbrace{H(t - \tau)}_{\text{window function}} e^{-2\pi i f t} dt$$

GW Spectrogram

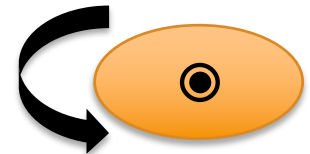
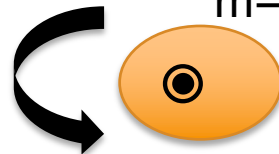
$$\Omega_0 = 2 \text{ rad/sec}$$



low $T/|W|$ instability

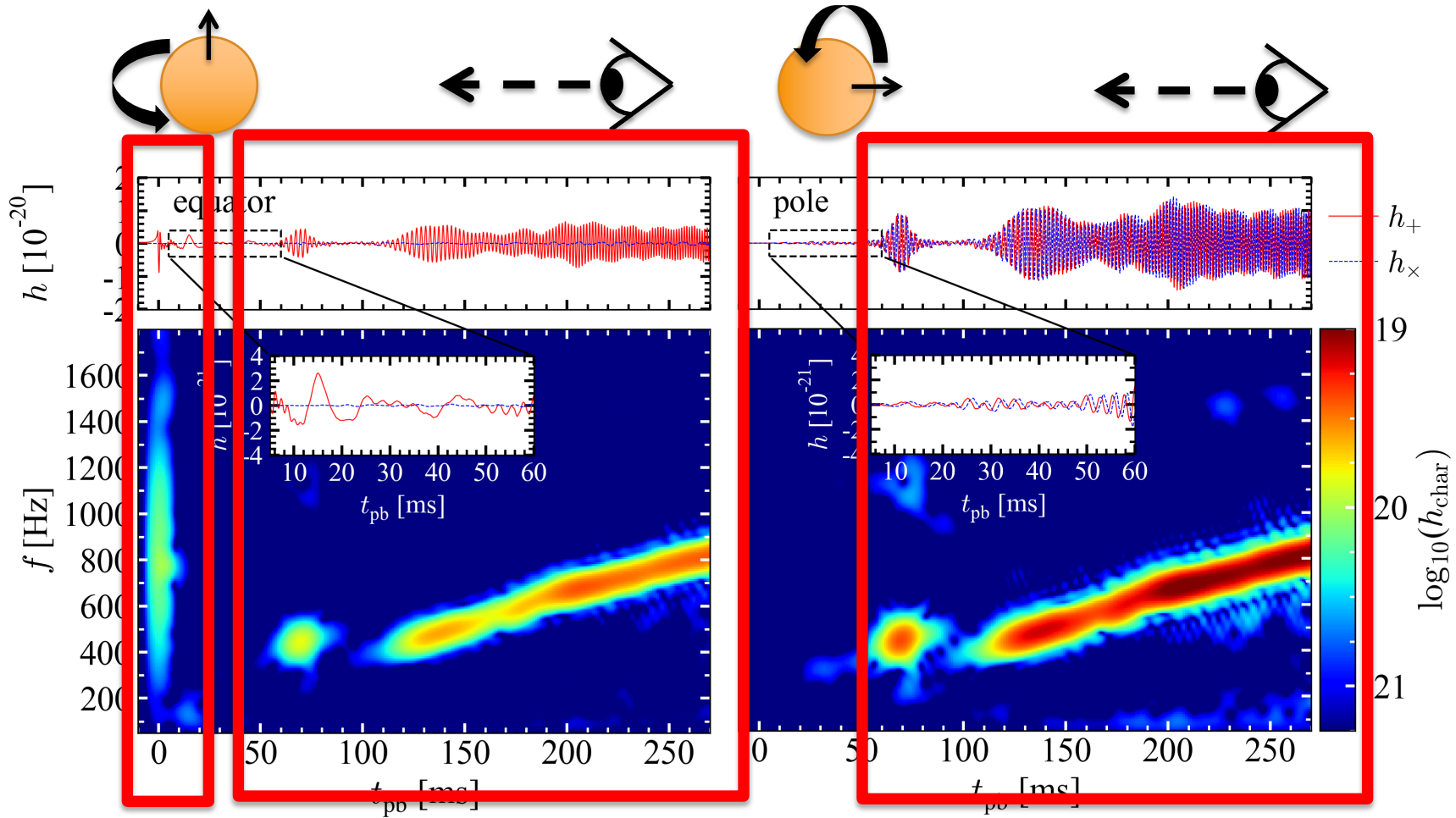
$m=1$ deformation

$m=2$ deformation



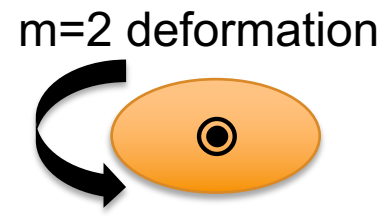
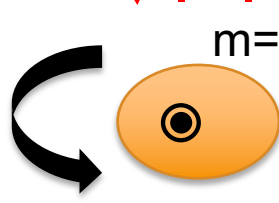
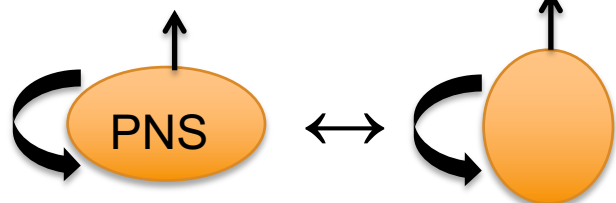
GW Spectrogram

$\Omega_0 = 2 \text{ rad/sec}$



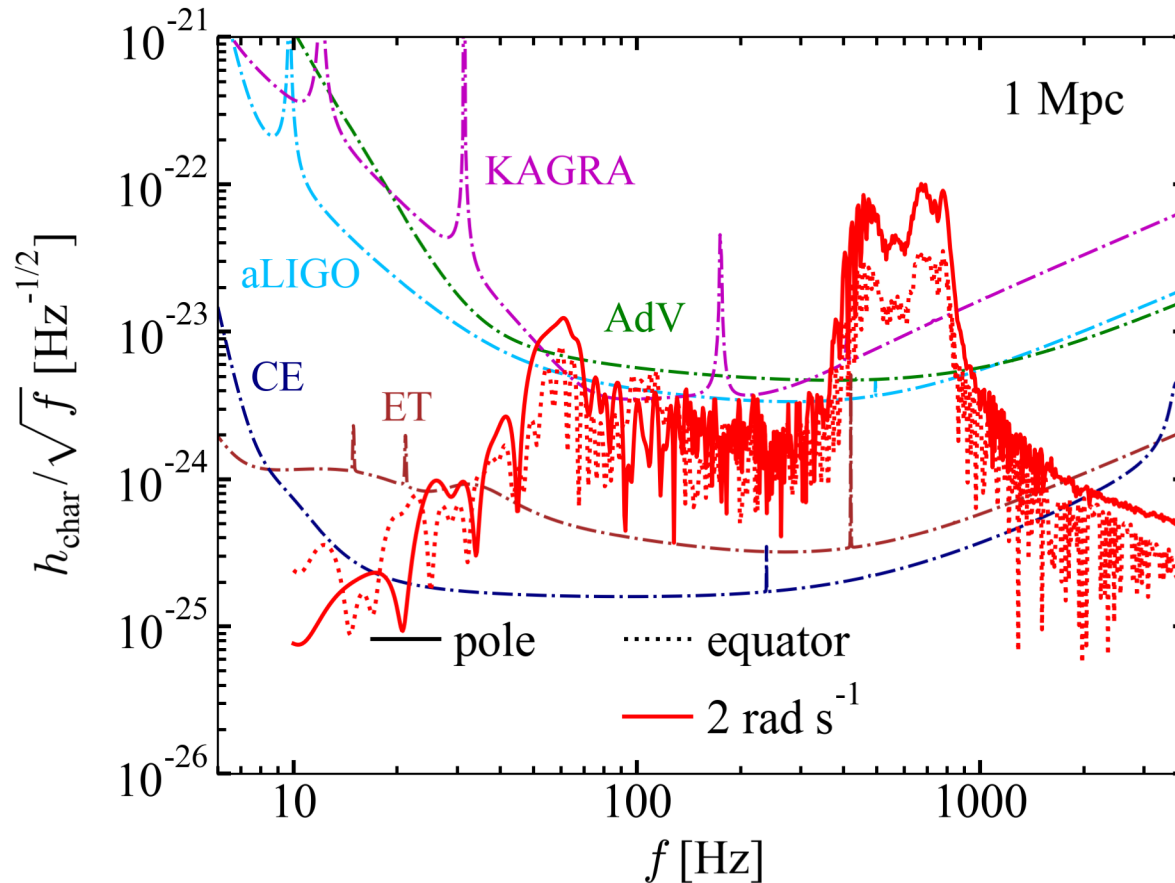
type I waveform

low $T/|W|$ instability



GW Detectability

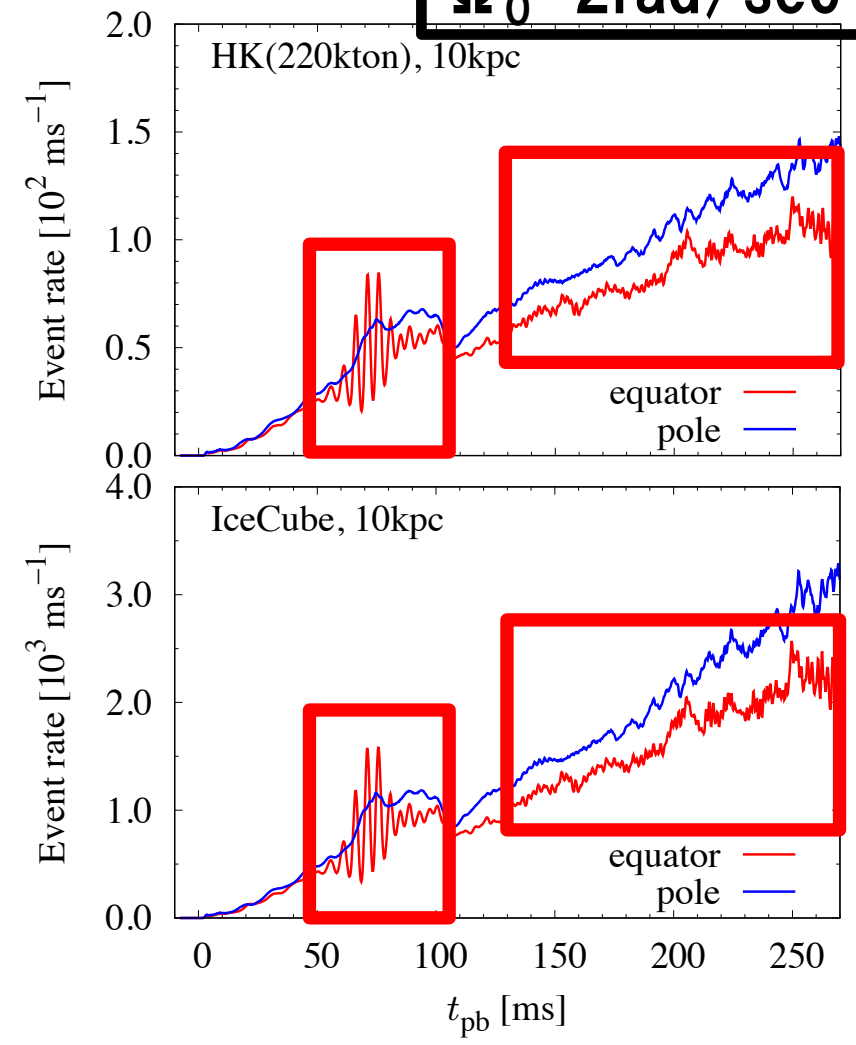
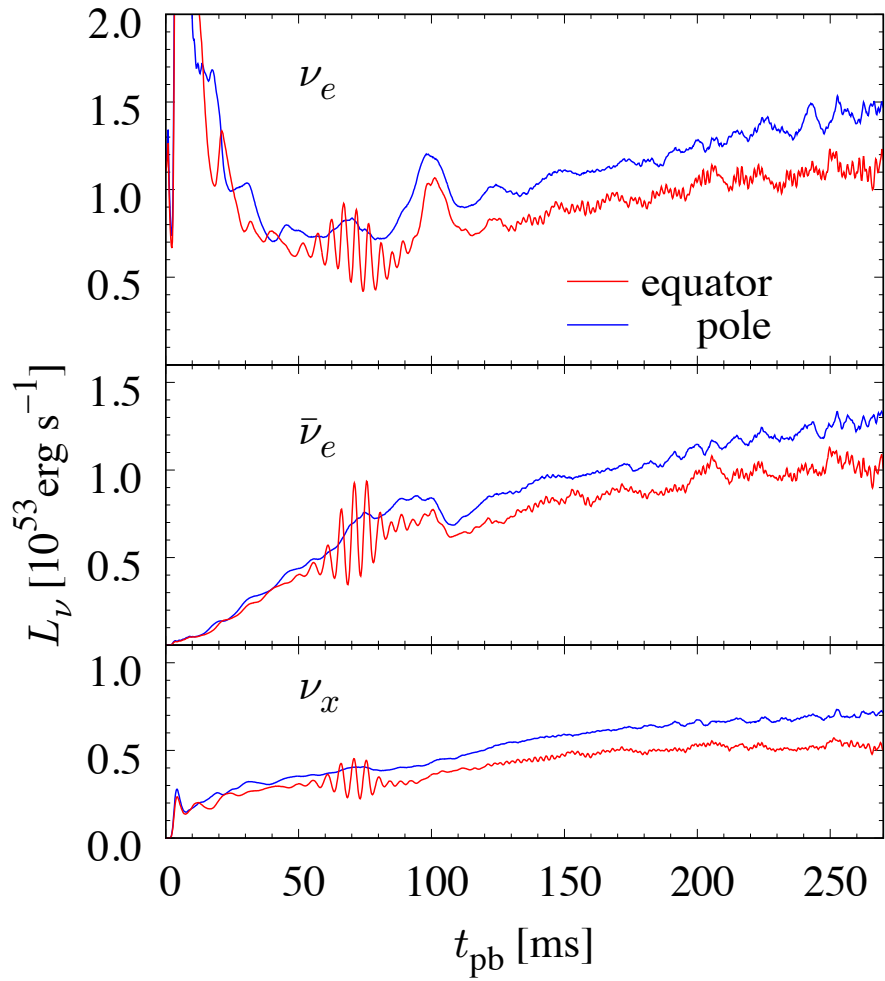
$$\Omega_0 = 2 \text{ rad/sec}$$



Current GW detectors have a potential to detect this GW up to \sim Mpc scale!!

Neutrino luminosity and event rate

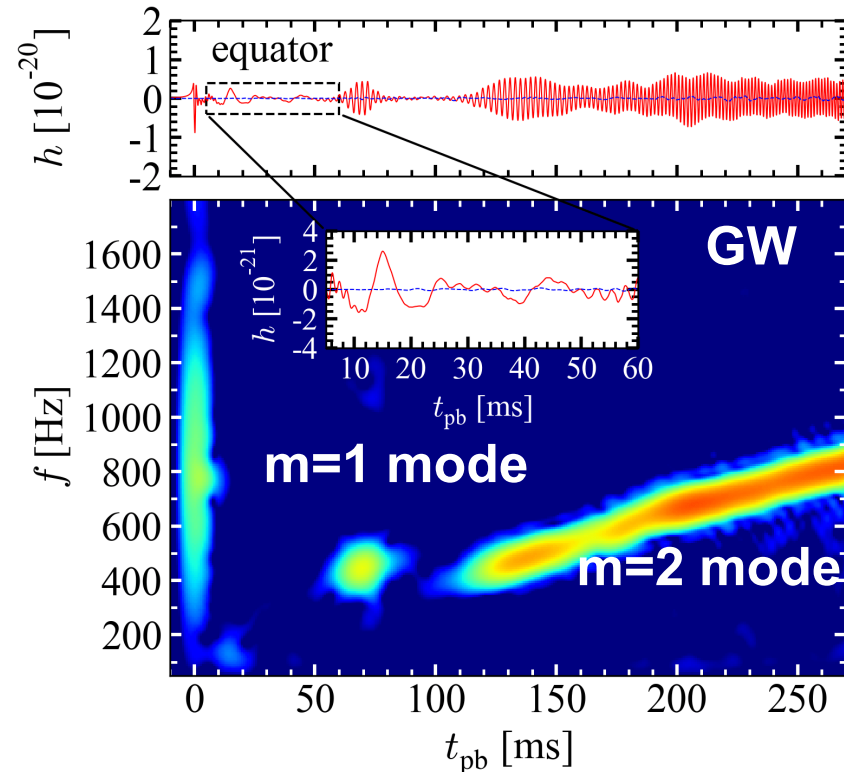
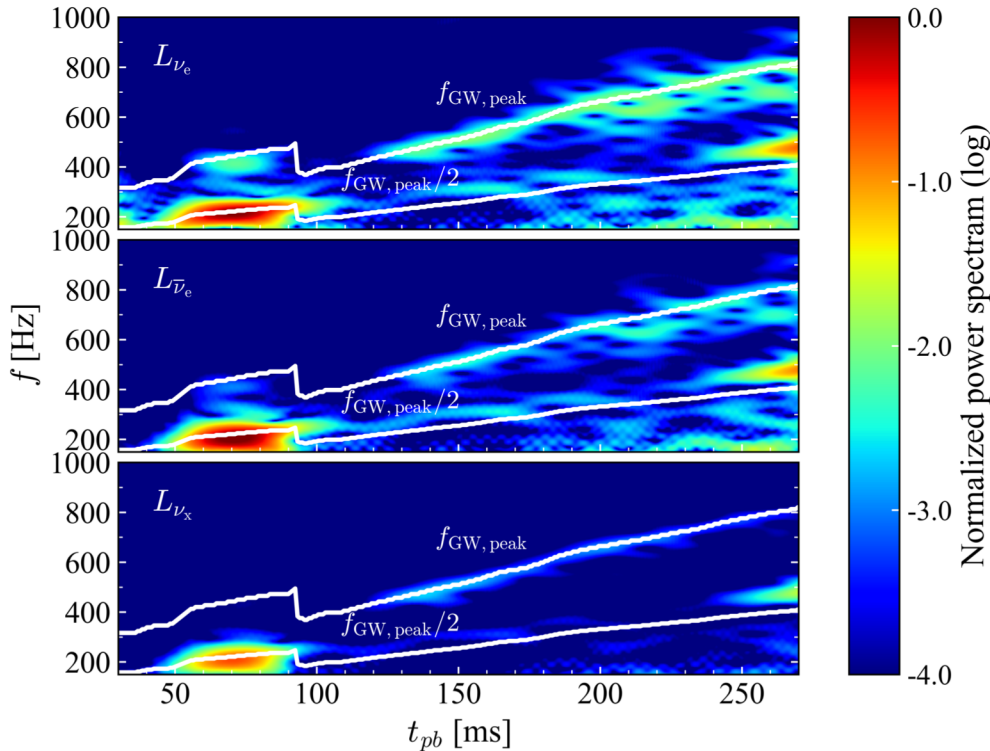
$\Omega_0 = 2 \text{ rad/sec}$



Oscillation in event rate found for equatorial observer

Neutrino spectrogram (equator)

$\Omega_0 = 2 \text{ rad/sec}$

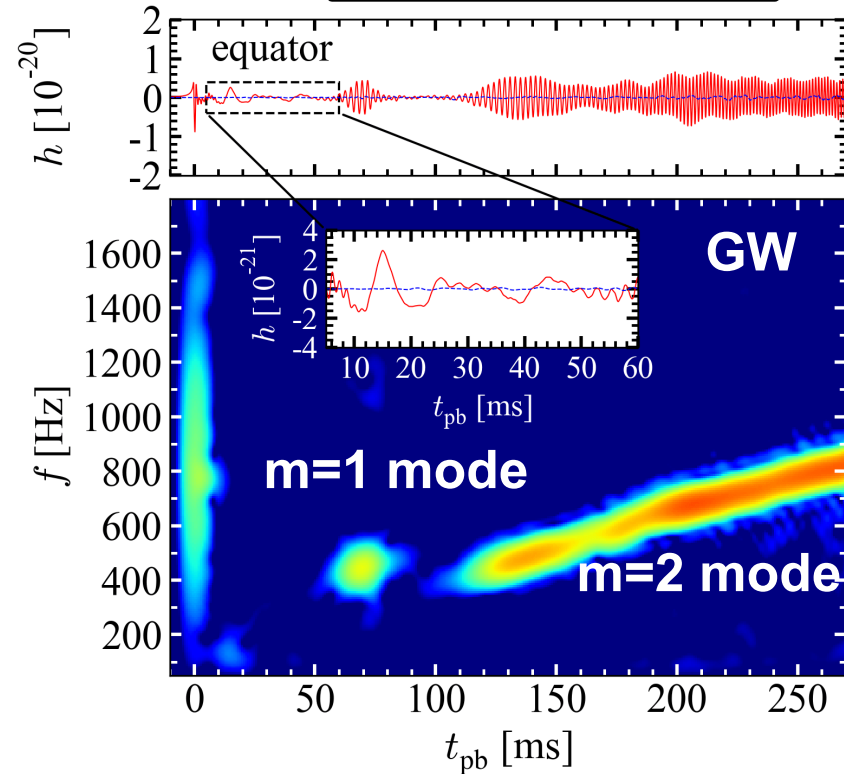
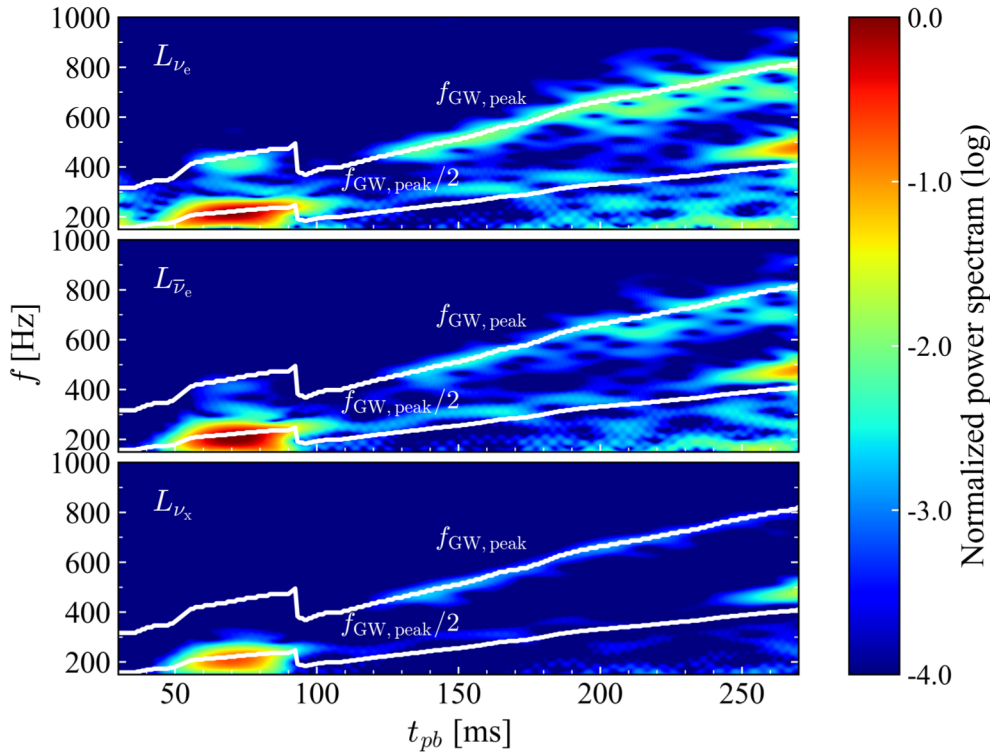


Correlation between GW and neutrino!!

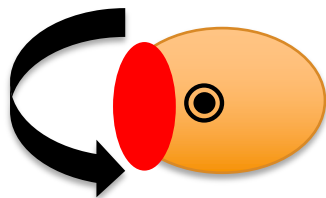
m=1 spiral arm ($50 < t_{pb} < 100$ ms): $f_{\nu} \sim f_{\text{GW}}/2$
m=2 spiral arm ($120 < t_{pb} < 270$ ms): $f_{\nu} \sim f_{\text{GW}}$

Neutrino spectrogram (equator)

$\Omega_0 = 2 \text{ rad/sec}$

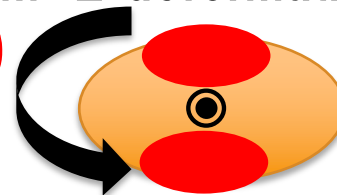


m=1 deformation



hot spot (s)

m=2 deformation

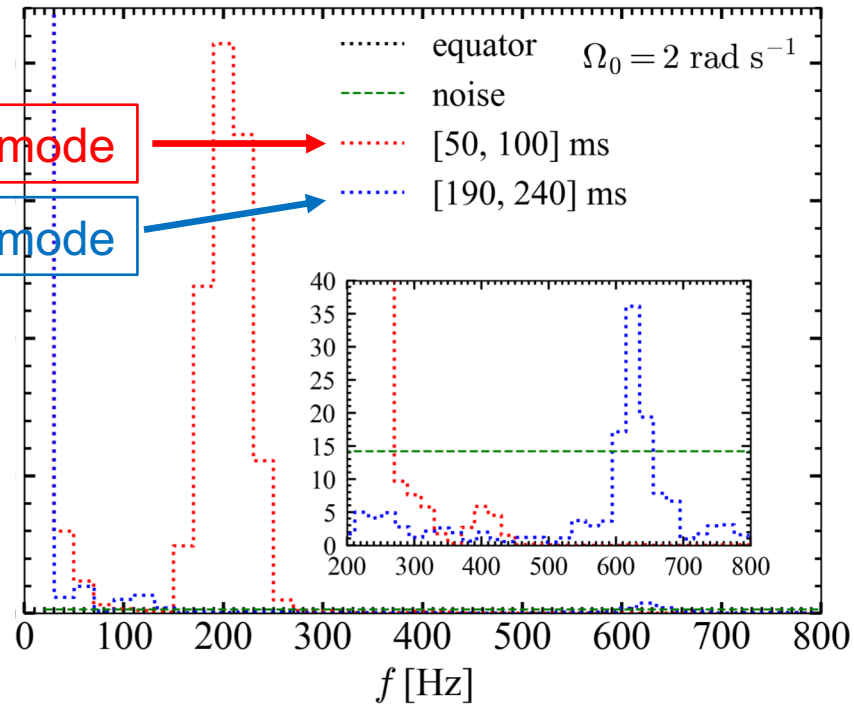
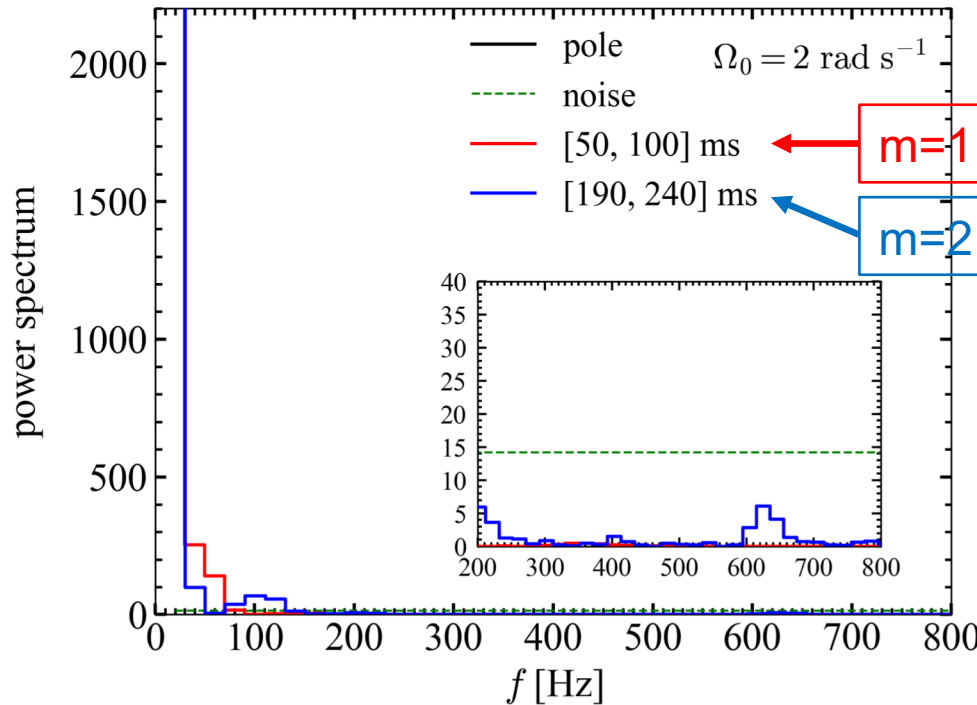
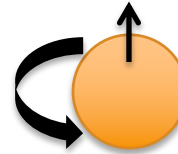
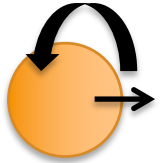


neutrino sphere

Neutrino event rate (spectrum)

IceCube @10kpc

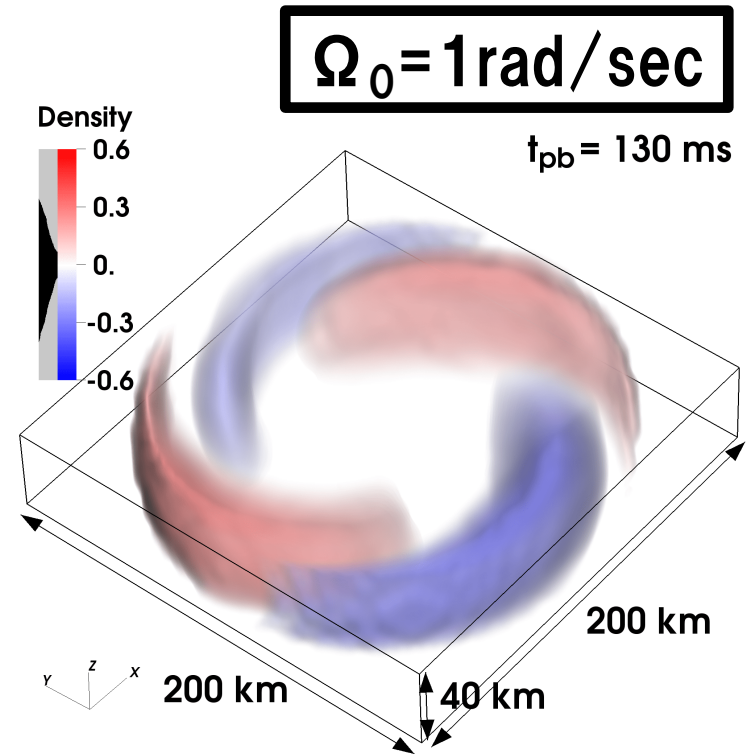
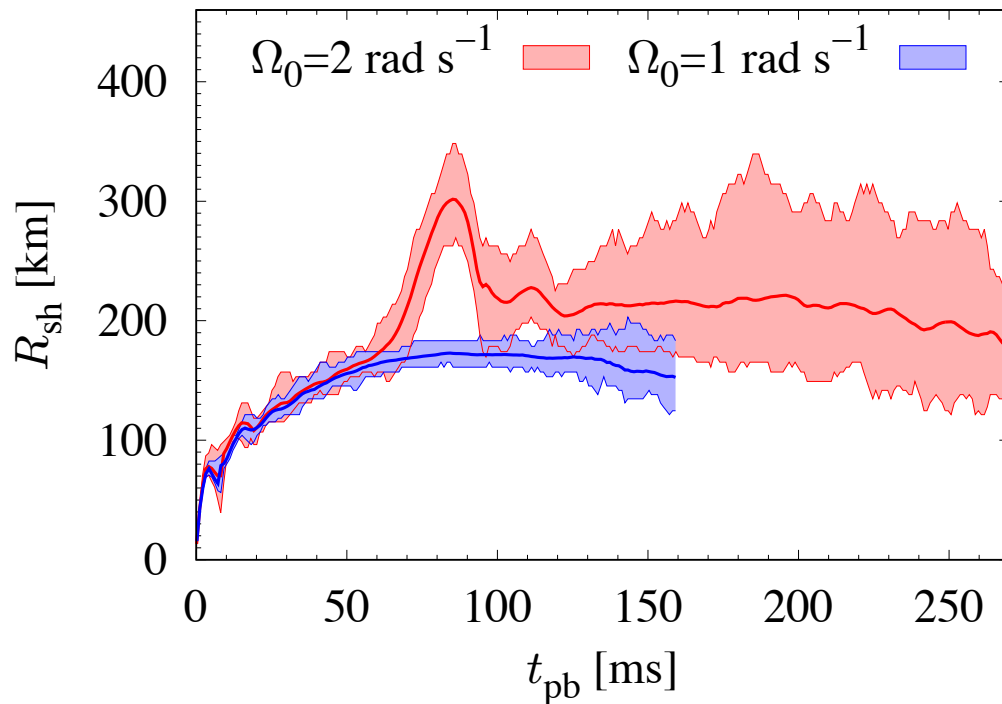
$\Omega_0 = 2 \text{ rad/sec}$



**Polar observer:
no clear oscillation**

**Equatorial observer:
oscillation observed**

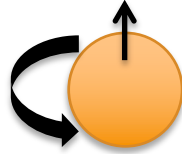
Comparison with $\Omega_0=1\text{rad/sec}$ model



**Shock is stalled like normal non-rotating core-collapse.
Two spiral arms are generated (m=2 mode).**

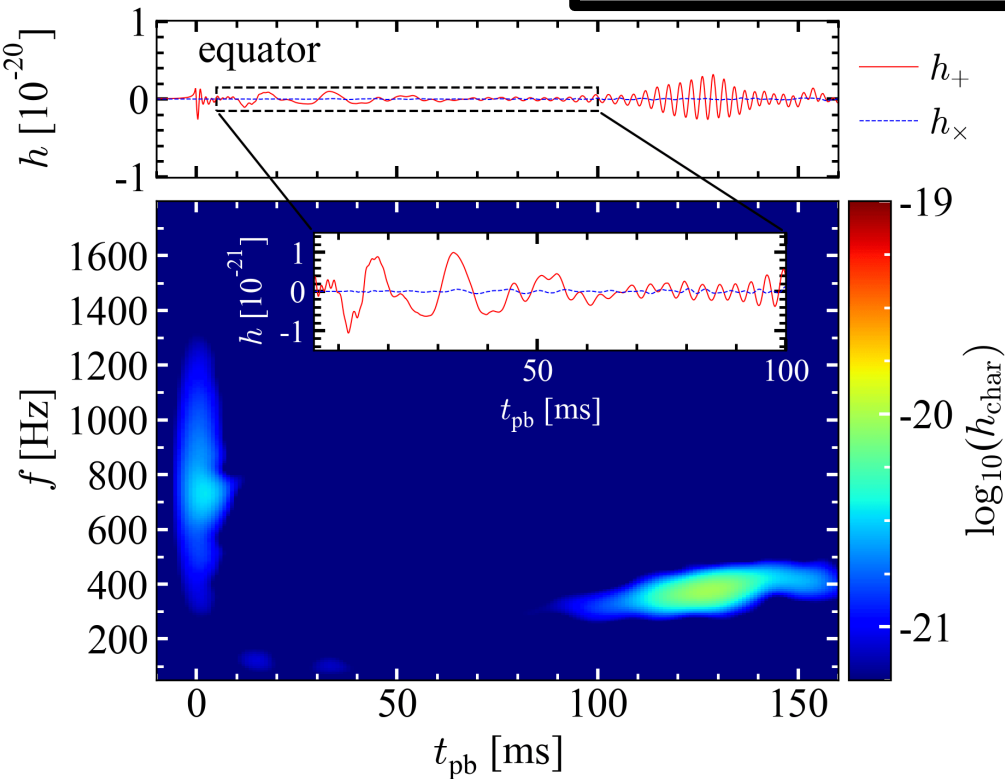
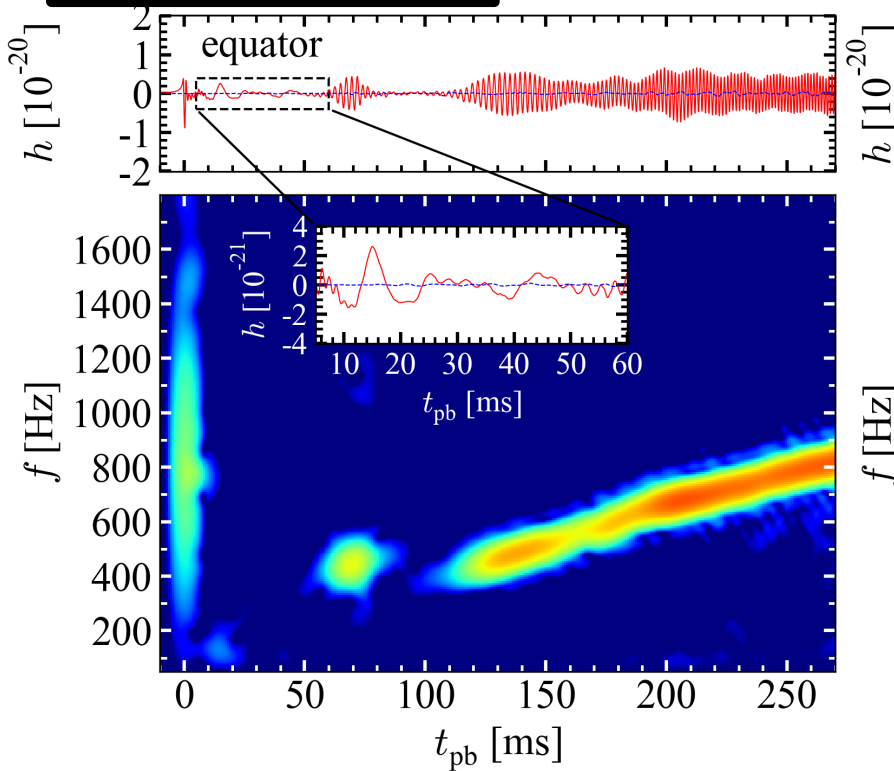
Comparison with $\Omega_0=1\text{rad/sec}$ model

@10kpc



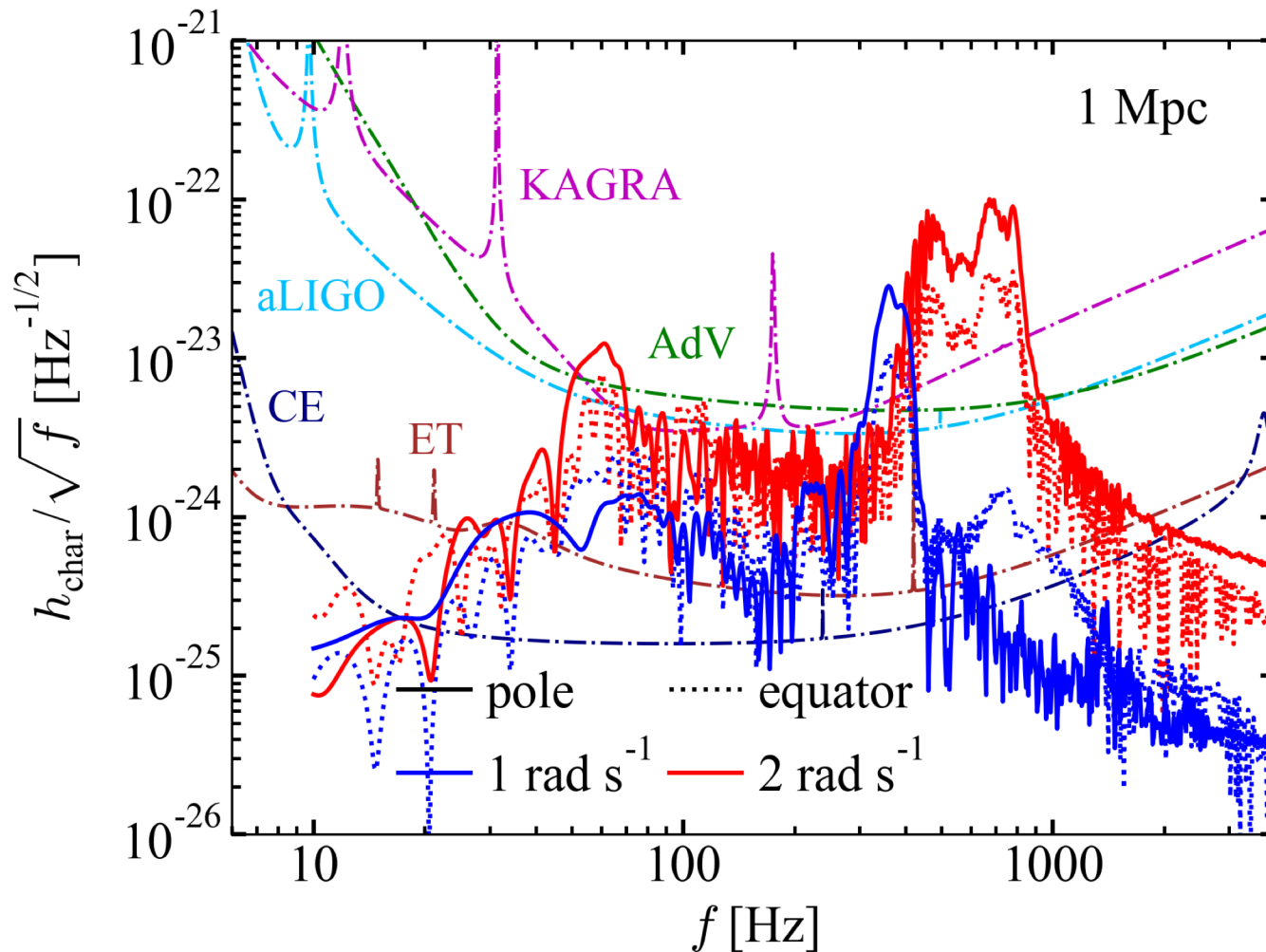
$\Omega_0=2\text{rad/sec}$

$\Omega_0=1\text{rad/sec}$



Weaker low-frequency GW signal in $\Omega_0=1\text{rad/sec}$ model

GW Detectability

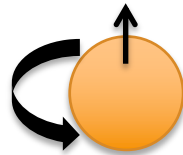


Current GW detectors have a potential to detect these GWs up to \sim Mpc scale!!

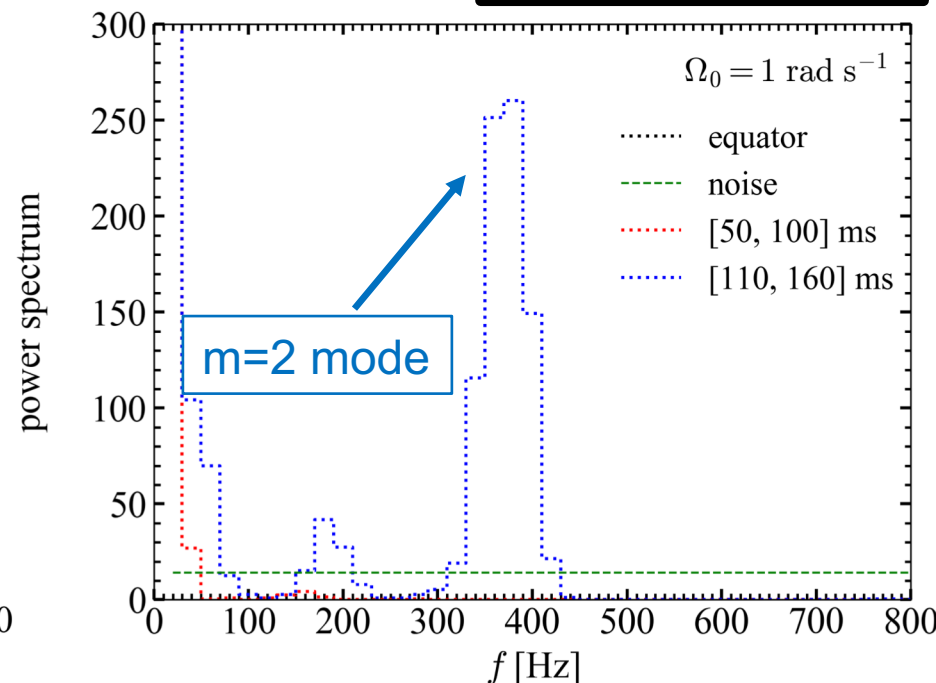
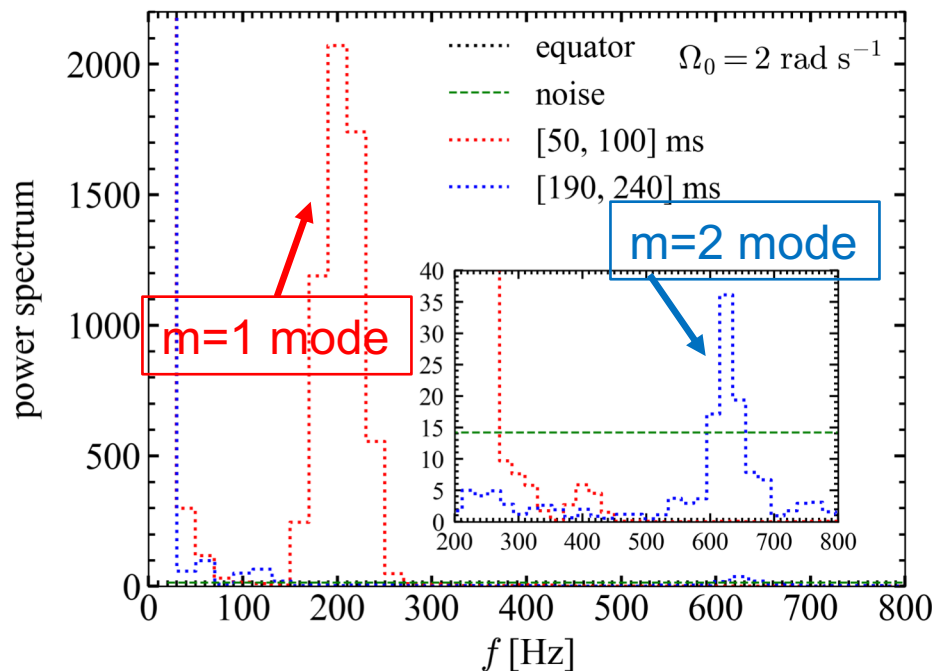
Neutrino event rate (spectrum)

@10kpc

$\Omega_0 = 2 \text{ rad/sec}$

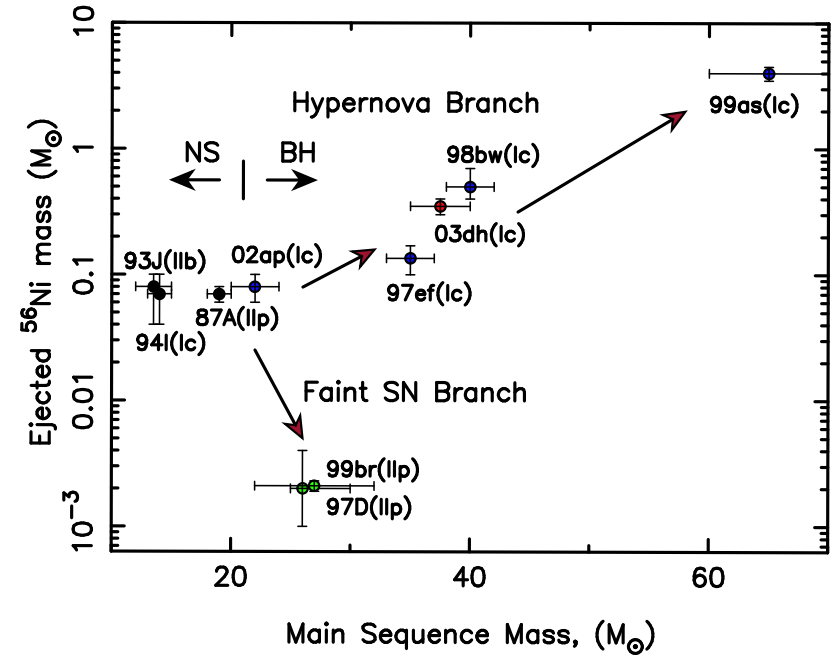
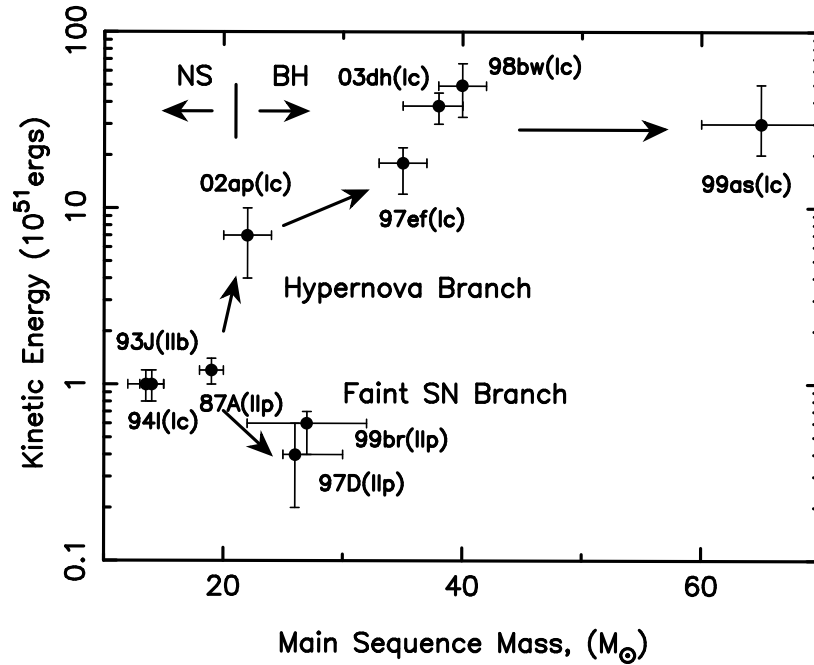


$\Omega_0 = 1 \text{ rad/sec}$



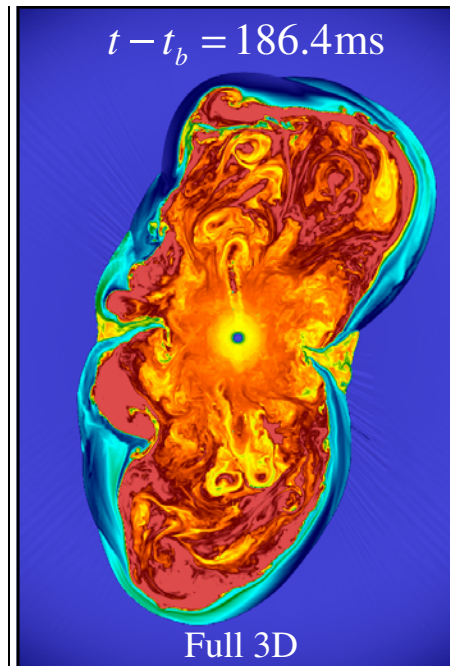
**Lower peak amplitude in $\Omega_0 = 1 \text{ rad/sec}$,
but it still exceeds the noise level!!**

Energetic supernova

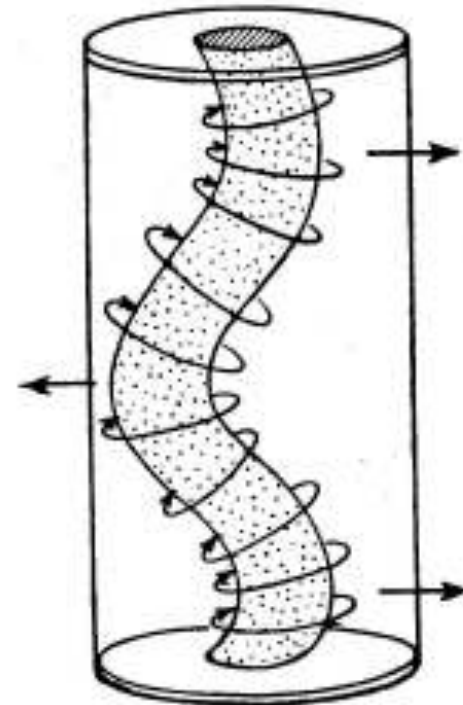


Nomoto et al. 2005

3D MHD Jet SN



Moesta et al. 2014



**Kink
instability**

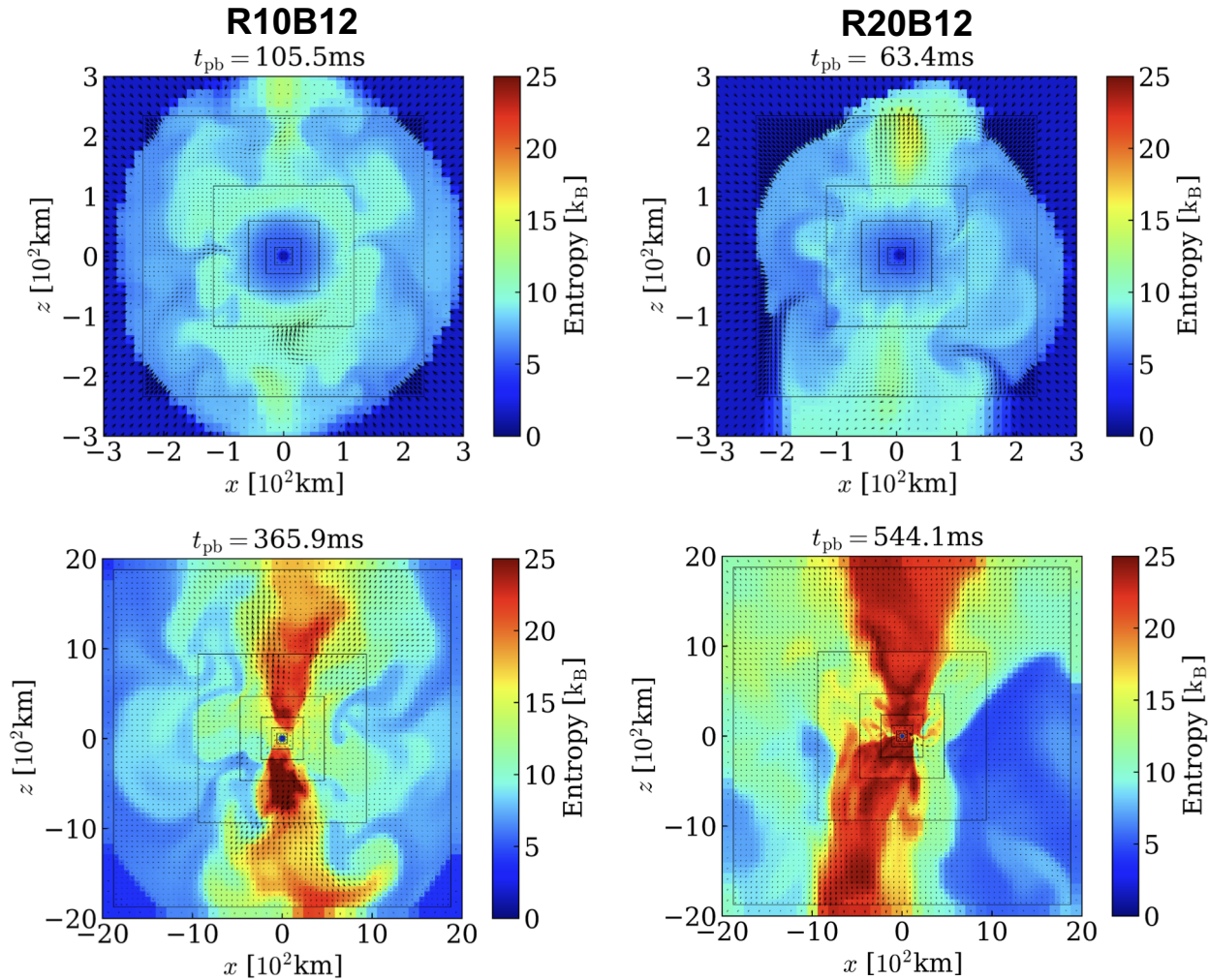
Setup

- Progenitor: s20 (Woosley & Heger2007)
- full GR RMHD code (Kuroda et al. 2020, 2021)
- neutrino transport: M1 scheme
- EOS: SFHo (Steiner et al. 2013)
- cylindrical rotation
- dipole magnetic field

Model	Ω_0 [rad s ⁻¹]	$\frac{B_0}{\sqrt{4\pi}}$ [10 ¹² G]
R05B12	0.5	1
R10B12	1.0	1
R10B13	1.0	10
R20B12	2.0	1

Entropy

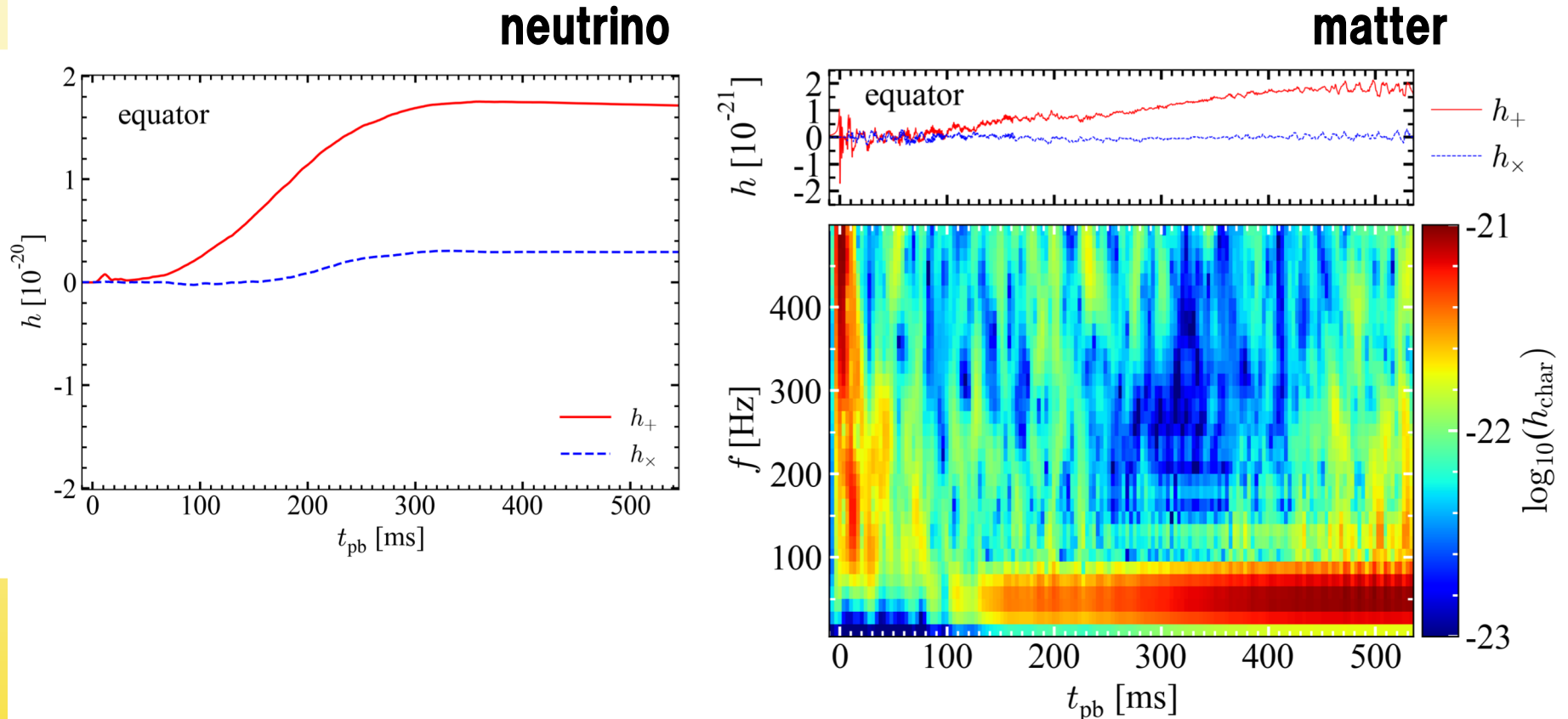
Model	Ω_0 [rad s ⁻¹]	$\frac{B_0}{\sqrt{4\pi}}$ [10 ¹² G]
R05B12	0.5	1
R10B12	1.0	1
R10B13	1.0	10
R20B12	2.0	1



Shibagaki, Kuroda, Kotake, Takiwaki, Fischer (2024)

GW Spectrogram

R20B12
equatorial observer

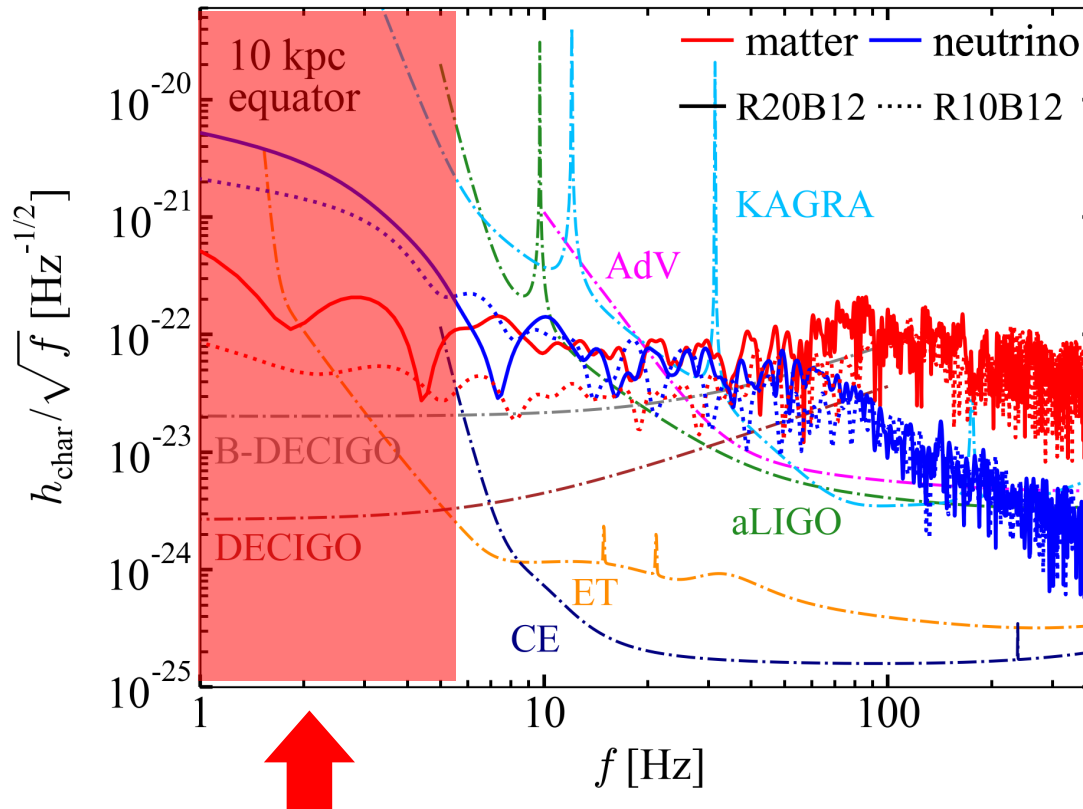


Both MHD jets and asymmetric neutrino emissions contribute to the generation of low-frequency GW.

Shibagaki, Kuroda, Kotake, Takiwaki, Fischer (2024)

GW Detectability

equatorial observer



The neutrino component is dominated over the jet component at low frequencies.

Shibagaki, Kuroda, Kotake, Takiwaki, Fischer, accepted (2024)

Summary

- **3D GR ν -radiation hydrodynamics simulation of 70 solar mass rapidly rotating stellar core collapse**
- The protoneutron star deformation due to rotation changes relationship between GW and neutrinos on their spectrograms.
 - $m=1$ deformation : $f_{\nu} \sim f_{\text{GW}}/2$
 - $m=2$ deformation : $f_{\nu} \sim f_{\text{GW}}$
- This indicates that joint observation of GW and neutrino could give us a hint of the protoneutron star deformation.
- **Fully general relativistic 3D neutrino radiation-magnetohydrodynamics simulations of rotating magnetized core collapse**
- GW from anisotropic neutrino emission may hide GW from hydrodynamic motion.